## CHAPTER 2 <br> Displaying Descriptive Statistics

2.1
a) $2^{7}=128>100$ therefore use 7 classes.
b) $2^{9}=512>300$ therefore use 9 classes.
c) $2^{10}=1,024>1,000$ therefore use 10 classes.
d) $2^{11}=2,048>2,000$ therefore use 11 classes.
$2.22^{6}=64>50$ therefore use 6 classes.
Estimated Class Width $=\frac{74-16}{6}=9.7 \approx 10$
a) $16-25,26-35,36-45,46-55,56-65,66-75$
b) 16 to under 26,26 to under 36,36 to under 46, 46 to under 56,56 to under 66,66 to under 76
2.3

|  | Frequency | Relative <br> Number | Frequency <br> Relative |
| :--- | :--- | :--- | :--- |
| 1 | 6 | 0.250 | Frequency |
| 2 | 6 | 0.250 | 0.250 |
| 3 | 5 | 0.208 | 0.500 |
| 4 | 4 | 0.167 | 0.708 |
| 5 | 3 | 0.125 | 0.875 |
| Total | $\mathbf{2 4}$ | $\mathbf{1 . 0 0}$ | 1.00 |
|  |  |  |  |

$2.42^{5}=32>30$ therefore use 5 classes.
Estimated Class Width $=\frac{42.8-13.9}{5}=5.8 \approx 6$

|  | Frequency | Relative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :--- | :--- | :--- | :--- |
| Class |  | 0.200 | 0.200 |
| 13 to less than 19 | 6 | 0.367 | 0.567 |
| 19 to less than 25 | 11 | 0.133 | 0.700 |
| 25 to less than 31 | 4 | 0.233 | 0.933 |
| 31 to less than 37 | 7 | 0.067 | 1.0 |
| 37 to less than 43 | 2 | $\mathbf{1 . 0 0}$ |  |
| Total | $\mathbf{3 0}$ |  |  |

$2.52^{6}=64>36$ therefore use 6 classes.
Estimated Class Width $=\frac{\$ 5,927-\$ 162}{6}=\$ 960 \approx \$ 1,000$
$a, b, c$ )

| Class | Frequency | Relative <br> Frequency |
| :--- | :--- | :--- |
| Less than $\$ 1,000$ | 12 | 0.333 |
| $\$ 1,000$ to less than $\$ 2,000$ | 8 | 0.222 |
| $\$ 2,000$ to less than $\$ 3,000$ | 3 | 0.083 |
| $\$ 3,000$ to less than $\$ 4,000$ | 2 | 0.056 |
| $\$ 4,000$ to less than $\$ 5,000$ | 6 | 0.167 |
| $\$ 5,000$ to less than $\$ 6,000$ | 5 | 0.139 |
| Total | $\mathbf{3 6}$ | $\mathbf{1 . 0 0 0}$ |

Cumulative<br>Relative<br>Frequency<br>0.333<br>0.555<br>0.638<br>0.694

0.056
$\$ 4,000$ to less than $\$ 5,000 \quad 6$
$0.167 \quad 0.861$
1.000
d) The following histogram was constructed using bins $\$ 999, \$ 1,999, \$ 2,999, \$ 3,999, \$ 4,999$, and $\$ 5,999$.

$2.62^{5}=32>25$ therefore use 5 classes.
Estimated Class Width $=\frac{46-18}{5}=5.6 \approx 6$
$a, b, c)$

|  | Frequency | Relative <br> Frequency <br> Class | Relative <br> Frequency |
| :--- | :--- | :--- | :--- |
| $18-23$ | 2 | 0.08 | 0.08 |
| $24-29$ | 6 | 0.24 | 0.32 |
| $30-35$ | 5 | 0.20 | 0.52 |
| $36-41$ | 5 | 0.20 | 0.72 |
| $42-47$ | 7 | 0.28 | 1.00 |
| Total | $\mathbf{2 5}$ | $\mathbf{1 . 0 0}$ |  |

d) The following histogram was constructed using bins 22.9, 28.9, 34.9, 40.9, and 46.9.

a, b, c)

| Number | Frequency | Relative <br> Frequency | Relative <br> Frequency |
| :--- | :--- | :--- | :--- |
| 0 | 3 | 0.043 | 0.043 |
| 1 | 21 | 0.300 | 0.343 |
| 2 | 23 | 0.329 | 0.672 |
| 3 | 15 | 0.214 | 0.886 |
| 4 | 8 | 0.114 | 1.000 |
| Total | $\mathbf{7 0}$ | $\mathbf{1 . 0 0 0}$ |  |

d) The following histogram was constructed using bins $0,1,2,3$, and 4 .

2.8 $2^{6}=64>40$ therefore use 6 classes.

Estimated Class Width $($ Current $)=\frac{76-19}{6}=9.5 \approx 10$
Results would be similar using the laid-off ages.

| Class | Bins | Midpoint |
| :--- | :--- | :--- |
| 19 to less than 29 | 28.9 | 24 |
| 29 to less than 39 | 38.9 | 34 |
| 39 to less than 49 | 48.9 | 44 |
| 49 to less than 59 | 58.9 | 54 |
| 59 to less than 69 | 68.9 | 64 |
| 69 to less than 79 | 78.9 | 74 |

An extra bin (18.9) was added to Excel to provide the open-ended class required by PHStat2.
a)

b)

c) According to these polygons, it appears that the current workforce is younger than the laid-off employees. It appears that the laid-off employees may have a case for age discrimination.
$2.92^{9}=512>350$ therefore use 9 classes.
Estimated Class Width $=\frac{\$ 349.99-\$ 2.19}{9}=\$ 38.64 \approx \$ 40$
$a, b, c)$

## Class

Less than $\$ 40$
$\$ 40$ to less than $\$ 80$
$\$ 80$ to less than $\$ 120$
$\$ 120$ to less than $\$ 160$
$\$ 160$ to less than \$200
\$200 to less than \$240
\$240 to less than \$280
$\$ 280$ to less than \$320
\$320 to less than \$360
Total

Frequency Relative Frequency
0.149
0.294
0.260
0.186
0.043
0.031
0.014
0.014
0.009
1.000

## Cumulative

## Relative

Frequency
0.149
0.443
0.703
0.889
0.932
0.963
0.977
0.991
1.000
d) The following histogram was constructed using bins 39.999, 79.999, 119.999, 159.999, 199.999, 239.999, 279.999, 319.999, and 359.999.

2.10 $2^{7}=128>125$ therefore use 7 classes.

Estimated Class Width $=\frac{83.2-71.0}{7}=1.7 \approx 2$
$a, b, c)$

## Class

71 to less than 73
73 to less than 75
75 to less than 77
77 to less than 79
79 to less than 81
81 to less than 83
83 to less than 85
Total

| Frequency | Relative <br> Frequency |
| :--- | :--- |
| 5 | 0.040 |
| 37 | 0.296 |
| 44 | 0.352 |
| 31 | 0.248 |
| 6 | 0.048 |
| 1 | 0.008 |
| 1 | 0.008 |
| $\mathbf{1 2 5}$ | $\mathbf{1 . 0 0 0}$ |

## Cumulative

Relative
Frequency
0.040
0.336
0.688
0.936
0.984
0.992
1.000
d) The following histogram was constructed using bins $72.99,74.99,76.99,78.99,80.99,82.99$, and 84.99.

e) For $68.8 \%$ of the days, ocean temps were lower than 70 degrees.
2.11
$a, b, c$ )

|  | Frequency | Relative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :--- | :--- | :--- | :--- |
| Category |  | 0.667 | 0.667 |
| Google | 20 | 0.167 | 0.833 |
| Yahoo | 5 | 0.067 | 0.900 |
| Bing | 2 | 0.067 | 0.967 |
| Baidu | 2 | 0.033 | 1.000 |
| Other | 1 | $\mathbf{1 . 0 0 0}$ |  |
| Total | $\mathbf{3 0}$ |  |  |

d)

2.12
$\mathrm{a}, \mathrm{b}, \mathrm{c})$

|  | Frequency | Relative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :--- | :--- | :--- | :--- |
| Category |  | 0.267 | 0.267 |
| Excellent | 16 | 0.517 | 0.783 |
| Good | 31 | 0.133 | 0.917 |
| Fair | 8 | 0.083 | 1.000 |
| Poor | 5 | $\mathbf{1 . 0 0 0}$ |  |
| Total | $\mathbf{6 0}$ |  |  |

d)

e) $78.3 \%$ rated their dining experience as either Excellent or Good.
2.13

2.14


### 2.15


2.16


### 2.17


2.18

2.19 Because all the possible categories appear to be included in the data, a pie chart would be a good choice to display this data.

2.20 Because we are comparing data from a sample of countries over different time periods, a clustered bar chart would be a good choice to display this data. A stacked bar chart would not be the best choice because adding the GDPs for 2 time periods that are 10 years apart is not very meaningful.

2.21

| Grade | Female | Male | Total |
| :--- | :--- | :--- | :--- |
| A | 5 | 2 | 7 |
| B | 5 | 7 | 12 |
| C | 2 | 3 | 5 |
| Total | $\mathbf{1 2}$ | $\mathbf{1 2}$ | $\mathbf{2 4}$ |

$71 \%$ (5/7) of the As were earned by females even though they comprise of $50 \%(12 / 24)$ of the students in the class. The females appear to have done better grade-wise than the males.
2.22

| Rating | Darby | Exton | Media | Total |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 2 | 3 | 5 |
| 2 | 2 | 3 | 8 | 13 |
| 3 | 6 | 7 | 7 | 20 |
| 4 | 7 | 3 | 2 | 12 |
| Total | $\mathbf{1 5}$ | $\mathbf{1 5}$ | $\mathbf{2 0}$ | $\mathbf{5 0}$ |

Darby received $58 \%$ (7/12) of the 4-star ratings even though they were only $30 \%$ (15/50) of the surveyed customers. Darby appears to have higher customer satisfaction when compared to the other two locations.
2.23

$$
\begin{aligned}
& 7 \mid 12345889 \\
& 8 \mid 036677 \\
& 9 \mid 00479 \\
& 10 \mid 0177 \\
& 11 \mid 0112568 \\
& 12 \mid 00256 \\
& 13 \mid 04479
\end{aligned}
$$

2.24

$$
\begin{aligned}
& 10 \mid 025889 \\
& 11 \mid 01233445 \\
& 12 \mid 11123356779 \\
& 13 \mid 02267779 \\
& 14 \mid 00256 \\
& 15 \mid 0
\end{aligned}
$$

### 2.25 a)

$$
\begin{aligned}
& 1 \mid 36 \\
& 2 \mid 123479 \\
& 3 \mid 57778 \\
& 4 \mid 00123344557889 \\
& 5 \mid 0011224589 \\
& 6 \mid 47
\end{aligned}
$$

b)

$$
\begin{aligned}
& 1(0) \mid 3 \\
& 1(5) \mid 6 \\
& 2(0) \mid 1234 \\
& 2(5) \mid 79 \\
& 3(0) \mid \\
& 3(5) \mid 57778 \\
& 4(0) \mid 00123344 \\
& 4(5) \mid 557889 \\
& 5(0) \mid 0011224 \\
& 5(5) \mid 589 \\
& 6(0) \mid 4 \\
& 6(5) \mid 7
\end{aligned}
$$

2.26 a)

$$
\begin{aligned}
& 1 \mid 6 \\
& 2 \mid 166778889 \\
& 3 \mid 11235556679 \\
& 4 \mid 005 \\
& 5 \mid 9
\end{aligned}
$$

b)

$$
\begin{aligned}
& 1(0) \mid \\
& 1(5) \mid 6 \\
& 2(0) \mid 1 \\
& 2(5) \mid 66778889 \\
& 3(0) \mid 1123 \\
& 3(5) \mid 5556679 \\
& 4(0) \mid 00 \\
& 4(5) \mid 5 \\
& 5(0) \mid \\
& 5(5) \mid 9
\end{aligned}
$$

2.27 It appears that the number of Netflix subscribers is increasing significantly during this time period.

2.28 It appears that the demand for TVs decreases as price increases.


### 2.29


$2.302^{6}=64>40$ therefore use 6 classes.
Estimated Class Width $=\frac{23-0}{6}=3.8 \approx 4$
$a, b, c)$

| Class | Frequency | Relative <br> Frequency <br> Relative |  |
| :--- | :--- | :--- | :--- |
| $0-3$ | 8 | 0.200 | Frequency |
| $4-7$ | 5 | 0.125 | 0.200 |
| $8-11$ | 15 | 0.375 | 0.325 |
| $12-15$ | 3 | 0.075 | 0.700 |
| $16-19$ | 6 | 0.150 | 0.775 |
| $20-23$ | 3 | 0.075 | 0.925 |
| Total | $\mathbf{4 0}$ | $\mathbf{1 . 0 0 0}$ | 1.000 |

d) The following histogram was constructed using bins $2.9,6.9,10.9,14.9,18.9$, and 22.9.

2.31
a, b, c)

|  | Frequency | Relative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :--- | :--- | :--- | :--- |
| Number |  | 0.32 | 0.32 |
| 0 | 16 | 0.18 | 0.50 |
| 1 | 9 | 0.14 | 0.64 |
| 2 | 7 | 0.22 | 0.86 |
| 3 | 11 | 0.10 | 0.96 |
| 4 | 5 | 0.04 | 1.00 |
| 5 | 2 | $\mathbf{1 . 0 0}$ |  |
| Total | $\mathbf{5 0}$ |  |  |

d) The following histogram was constructed using bins $0,1,2,3,4$, and 5 .

e) $50 \%$
$2.322^{6}=64>48$ therefore use 6 classes.
Estimated Class Width $=\frac{1,187-43}{6}=190.7 \approx 200$
$a, b, c$ )

## Class

0 to under 200
200 to under 400
400 to under 600
600 to under 800
800 to under 1,000
1,000 to under 1,200
Total

Frequency

15
13
11
4
4
1
48

Relative
Frequency
0.313
0.271
0.229
0.083
0.083
0.021
1.000

## Cumulative

Relative
Frequency
0.313
0.584
0.813
0.896
0.979
1.000
d) The following histogram was constructed using bins 199.9, 399.9, 599.9, 799.9, 999.9, and 1,199.9.

$2.332^{7}=128>72$ therefore use 7 classes.
Estimated Class Width $=\frac{795-190}{7}=86.4 \approx 100$ $a, b, c)$

## Class

101-200
201-300
301-400
401-500
501-600
601-700
701-800
Total

Frequency Relative
Frequency
0.028
0.028
0.125
0.208
0.431
0.125
0.056
1.001

Cumulative
Relative
Frequency
0.028
0.056
0.181
0.389
0.820
0.945
1.001
d) The following histogram was constructed using bins 200, 300, 400, 500, 600, 700, and 800 .

$2.342^{5}=32>30$ therefore use 5 classes.
Estimated Class Width $($ Day $)=\frac{100-66}{5}=6.8 \approx 7$
Results would be similar using the evening grades.

| Class | Bins | Midpoint |
| :--- | :--- | :--- |
| $66-72$ | 72 | 69 |
| $73-79$ | 79 | 76 |
| $80-86$ | 86 | 83 |
| $87-93$ | 93 | 90 |
| $94-100$ | 100 | 97 |

An extra bin (65) was added to Excel to provide the open-ended class required by PHStat2.
a)

b)

c) The evening class grades appear to be noticeably higher than the day class grades.
$2.352^{9}=512>300$ therefore use 9 classes.
Estimated Class Width $=\frac{39-(-14)}{9}=5.9 \approx 6$
$a, b, c)$

Class
-14 to under -8.1 6
-8 to under -2.1
-2 to under 4
4 to under 10
10 to under 16
16 to under 22
22 to under 28
28 to under 34
34 to under 40
Total

Frequency Relative
Frequency
0.020
0.093
0.133
0.193
0.227
0.203
0.090
0.030
0.010
0.999

Relative
Cumulative
Frequency
0.020
0.113
0.246
0.439
0.666
0.869
0.959
0.989
0.999
d) The following histogram was constructed using bins $-8.1,-2.1,3.9,9.9,15.9,21.9,27.9,33.9$, and 39.9.

e) Approximately 74 out of 300 flights were not late ( $24.7 \%$ ).
2.36 a)

b)

$2.372^{7}=128>100$ therefore use 7 classes.
Estimated Class Width $($ Wayne $)=\frac{259-12}{7}=35.3 \approx 40$
Results would be similar using the Dover data.

| Class | Bins | Midpoint |
| :--- | :--- | :--- |
| $1-40$ | 40 | 20.5 |
| $41-80$ | 80 | 60.5 |
| $81-120$ | 120 | 100.5 |
| $121-160$ | 160 | 140.5 |
| $161-200$ | 200 | 180.5 |
| $201-240$ | 240 | 220.5 |
| $241-280$ | 280 | 260.5 |

An extra bin (0) was added to Excel to provide the open-ended class required by PHStat2.

b)

c) It appears that the days on the market for homes sold in Wayne are longer than for homes sold in Dover.
2.38 a)

b)

2.39


| Reason | Frequency | Relative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :--- | :---: | :---: | :---: |
| Too long on hold | 47 | 0.392 | 0.392 |
| Not knowledgeable | 22 | 0.183 | 0.575 |
| Not courteous | 18 | 0.150 | 0.725 |
| Hard to understand | 15 | 0.125 | 0.850 |
| Too many transfers | 10 | 0.083 | 0.933 |
| Other | 8 | 0.067 | 1.000 |
| Total | 120 |  |  |



### 2.41

| Reason | Frequency | Relative <br> Frequency | Cumulative <br> Relative Frequency |
| :--- | :---: | :---: | :---: |
| Transmission | 721 | 0.385 | 0.385 |
| Body | 437 | 0.233 | 0.619 |
| Wheels | 164 | 0.088 | 0.706 |
| Drivetrain | 139 | 0.074 | 0.780 |
| Windows | 89 | 0.048 | 0.828 |
| Engine | 55 | 0.029 | 0.857 |
| Interior | 45 | 0.024 | 0.881 |
| Electrical | 44 | 0.024 | 0.905 |
| Steering | 42 | 0.022 | 0.927 |
| Suspension | 41 | 0.022 | 0.949 |
| AC/heater | 26 | 0.014 | 0.963 |
| Brakes | 22 | 0.012 | 0.975 |
| Other | 47 | 0.025 | 1.000 |
| Total | 1872 |  |  |


2.42

2.43


### 2.44


2.45 A bar chart would be appropriate for categorical data. The time data needs to be converted to common units (minutes).

2.46 A clustered bar chart would be appropriate for this data. A stacked bar chart would also be an option.

2.47 A bar chart, either horizontal or vertical, is the best choice for this data. A pie chart would not be appropriate because all brands are not included. The total percentage does not equal $100 \%$.

2.48 A pie chart is the best choice because all categories are included and the percentage sums to $100 \%$.

2.49 A bar chart, either horizontal or vertical, is the best choice for this data.

2.50

| Brand | Diet | Regular | Total |
| :--- | :--- | :--- | :--- |
| Coke | 6 | 6 | 12 |
| Mt. Dew | 2 | 8 | 10 |
| Pepsi | 4 | 7 | 11 |
| Total | $\mathbf{1 2}$ | $\mathbf{2 1}$ | $\mathbf{3 3}$ |

$50 \%(6 / 12)$ of the Coke customers preferred Diet even though only $36 \%(12 / 33)$ of all the customers prefer Diet soda. Coke customers appear to have a higher percentage of customers who prefer diet soda than other brands.

| $\mathbf{2 . 5 1}$ |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Age | Callaway | Nike | Taylor Made | Total |
| $20-29$ | 4 | 2 | 19 | 25 |
| $30-39$ | 9 | 15 | 10 | 34 |
| $40-49$ | 16 | 6 | 8 | 30 |
| $50-59$ | 3 | 3 | 5 | 11 |
| Total | $\mathbf{3 2}$ | $\mathbf{2 6}$ | $\mathbf{4 2}$ | $\mathbf{1 0 0}$ |

Younger golfers seem to prefer Taylor Made clubs while older golfers seem to refer Callaway.
2.52 a)

$$
\begin{aligned}
& 1 \mid 899 \\
& 2 \mid 0002233555688889 \\
& 3 \mid 011112235556699 \\
& 4 \mid 13356 \\
& 5 \mid 1
\end{aligned}
$$

b)

$$
\begin{aligned}
& 1(5) \mid 899 \\
& 2(0) \mid 0002233 \\
& 2(5) \mid 555688889 \\
& 3(0) \mid 01111223 \\
& 3(5) \mid 5556699 \\
& 4(0) \mid 133 \\
& 4(5) \mid 56 \\
& 5(0) \mid 1
\end{aligned}
$$

2.53 a)

$$
\begin{aligned}
& 7 \mid 0022456777 \\
& 8 \mid 1258 \\
& 9 \mid 0122333457799 \\
& 10 \mid 01245 \\
& 11 \mid 289 \\
& 12 \mid 5 \\
& 13 \mid 0018
\end{aligned}
$$

b)
$7(0) \mid 00224$
$7(5) \mid 56777$
$8(0) \mid 12$
$8(5) \mid 58$
$9(0) \mid 01223334$
$9(5) \mid 57799$
$10(0) \mid 0124$
$10(5) \mid 5$
$11(0) \mid 2$
$11(5) \mid 89$
$12(0) \mid$
$12(5) \mid 5$
$13(0) \mid 001$
$13(5) \mid 8$
2.54


There does not appear to be a consistent relationship between payroll and wins during the 2010 season.


The trend in gasoline prices appear to rise consistently during this time period.

