# Chapter 2 Tabular and Graphical Methods 

## Solutions

1. 

a.

| Rating | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| 5 | 12 | $12 / 36=0.333$ |
| 4 | 9 | $9 / 36=0.250$ |
| 3 | 7 | $7 / 36=0.194$ |


| 2 | 5 | $5 / 36=0.139$ |
| :---: | :---: | :---: |
| 1 | 3 | $3 / 36=0.083$ |
| Total | 36 | 0.999 |

b. More than a third of the patrons are very satisfied with the entrees. Overall more than half of the customers gave a top rating of either 4 or 5. Only 8.3\% gave the lowest rating.
2.
a.

| Rating | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| Excellent | 5 | $5 / 24=0.208$ |
| Good | 12 | $12 / 24=0.500$ |
| Fair | 4 | $4 / 24=0.167$ |


| Poor | 3 | $3 / 24=0.125$ |
| :--- | :---: | :---: |
| Total | 24 | 1 |

b. The most common response is Good which comprises $50 \%$ of total responses. More than half of the patients reveal that they are in good or excellent health conditions.
3.
a.

| Expectation | Frequency | Relative <br> Frequency |
| :---: | :---: | ---: |
| Better | 5 | $5 / 25=0.20$ |
| Same | 16 | $16 / 25=0.64$ |
| Worse | 4 | $4 / 25=0.16$ |


b.

Most of the chief executives (64\%) believed that the economy would be the same in the next 12 months.
b.


4.
a.

| Delays | Frequency | Relative Frequency |
| :---: | :---: | :---: |
| PM Delays | 1 | $1 / 18=0.056$ |
| All Day Delays | 6 | $6 / 18=0.333$ |
| AM Delays | 4 | $4 / 18=0.222$ |


| None | 7 | $7 / 18=0.389$ |
| :--- | :---: | :---: |
| Total | 18 | 1 |

The most common delays were None, comprising $38.9 \%$ of all delays. The second most common were All Day Delays, comprising 33.3\% of all delays.
b.


5.
a. $22(18+4)$ out of 50 rookies received a rating of 4 or better; $14(10+4)$ out of 50 rookies received a rating of 2 or worse.
b.

| Rating | Relative <br> Frequency |
| :---: | :---: |
| 1 | $4 / 50=0.08$ |
| 2 | $10 / 50=0.2$ |
| 3 | $14 / 50=0.28$ |
| 4 | $18 / 50=0.36$ |
| 5 | $4 / 50=0.08$ |
| Total | 1 |

$8 \%$ of the rookies received a rating of 5 .
c.

6.
a.

| Response | Frequency |
| :---: | :---: |
| Good Jobs | $0.37 \times 5324=1970$ |
| Affordable homes | $0.15 \times 5324=799$ |
| Top schools | $0.11 \times 5324=586$ |
| Low crimes | $0.23 \times 5324=1225$ |
| Things to do | $0.14 \times 5324=745$ |
| Total | 5324 |

1225 respondents considered 'Low crimes' as the most important criteria.
b.

7.
a.

| Top Vacation Choice | Relative <br> Frequency |
| :---: | ---: |
| Cruises | $140 / 316=0.443$ |
| Beaches | $68 / 316=0.215$ |
| Amusement Parks | $68 / 316=0.215$ |
| Big Cities | $20 / 316=0.063$ |


| Lakes | $12 / 316=0.038$ |
| :---: | :---: |
| Summer Camp | $8 / 316=0.025$ |
| Total | 0.999 |

$44.3 \%$ of the children cited 'Cruises' as the perfect summer trip.
b.

8.
a.

| Company | Relative Frequency |
| :---: | ---: |
| Enterprise | $10.7 / 21.9=0.489$ |
| Hertz | $4.7 / 21.9=0.215$ |
| Avis Budget | $4 / 21.9=0.183$ |
| Dollar Thrifty | $1.5 / 21.9=0.068$ |
| Other | $1 / 21.9=0.046$ |
| Total | 1 |

b. Hertz accounted for $21.5 \%$ of sales.
c.

9.
a.


b. $\quad\left(0.4^{*} 829\right)=332$ respondents believe that a cure for cancer will be found.
10.
a. The number of responses for others is the difference between the total number of responses and the sum of responses in the table. That is, $(20825-15241)=5584$.
b. The proportion of respondents that felt that the Green Bay Packers would win Super Bowl XLV is $1076 / 20,825=0.052$.
c.

Relative frequencies are:

| Team | Relative Frequency |
| :---: | :---: |
| Falcons | $4040 / 20,825=0.194$ |
| Saints | $1880 / 20,825=0.090$ |
| Texans | $1791 / 20,825=0.086$ |
| Cowboys | $1631 / 20,825=0.078$ |


| Vikings | $1438 / 20,825=0.069$ |
| :---: | :--- |
| Colts | $1149 / 20,825=0.055$ |
| Steelers | $1141 / 20,825=0.055$ |
| Patriots | $1095 / 20,825=0.053$ |
| Packers | $1076 / 20,825=0.052$ |
| Others | $5584 / 20,825=0.268$ |


11. This graph does not correctly depict what has happened to Caterpillar's stock price over this period. The graph has been given a high value on the vertical axis. This compresses the data so that the increase of the stock price is not as apparent as it should be.
12. This graph does not correctly depict what has happened to sales over the most recent five-year period. The vertical axis has been stretched so that the increase in sales appears more pronounced than warranted.
13.
a.

| Class | Frequency |
| :--- | :---: |
| 3 up to 5 | 5 |
| 5 up to 7 | 5 |
| 7 up to 9 | 8 |
| 9 up to 11 | 4 |
| 11 up to 13 | 5 |
| 13 up to 15 | 3 |
|  | Total $=30$ |

b.

| Classes | Relative <br> Frequency | Cumulative Frequency | Cumulative Relative <br> Frequency |
| :---: | :---: | ---: | :---: |
| 3 up to 5 | $5 / 30=0.17$ | 5 | 0.17 |


| 5 up to 7 | $5 / 30=0.17$ | $5+5=10$ | $0.17+0.17=0.34$ |
| :---: | ---: | ---: | :---: |
| 7 up to 9 | $8 / 30=0.27$ | $5+5+8=18$ | $0.34+0.27=0.61$ |
| 9 up to 11 | $4 / 30=0.13$ | $5+5+8+4=22$ | $0.61+0.13=0.74$ |
| 11 up to 13 | $5 / 30=0.17$ | $5+5+8+4+5=27$ | $0.74+0.17=0.91$ |
| 13 up to 15 | $3 / 30=0.1$ | $5+5+8+4+5+3=30$ | $0.91+0.1 \approx 1$ |
|  | Total $=1$ |  |  |

c. 8 observations are at least 7 but less than $9 ; 18$ observations are less than 9
d. $27 \%$ of the observations are at least 7 but less than $9 ; 61 \%$ are less than 9
e.

f.

14.
a.

| Classes | Frequency |
| :---: | :---: |
| -10 up to 0 | 9 |
| 0 up to 10 | 31 |


| 10 up to 20 | 19 |
| :---: | :---: |
| 20 up to 30 | 8 |
| 30 up to 40 | 3 |
|  | Total $=70$ |

19 observations are at least 10 but less than 20 .
b.

| Classes | Relative <br> Frequency | Cumulative Relative Frequency |
| :---: | ---: | ---: |
| -10 up to 0 | $9 / 70=0.129$ | 0.129 |
| 0 up to 10 | $31 / 70=0.443$ | $0.129+0.443=0.572$ |
| 10 up to 20 | $19 / 70=0.271$ | $0.129+0.443+0.271=0.843$ |
| 20 up to 30 | $8 / 70=0.114$ | $0.129+0.443+0.271+0.114=0.957$ |
| 30 up to 40 | $3 / 70=0.043$ | $0.129+0.443+0.271+0.114+0.043=1$ |
|  | Total $=0.999$ |  |

$27.1 \%$ of the observations are at least 10 but less than 20; $84.3 \%$ are less than 20
c.


The distribution has a slight positive skew.
15.
a.

| Class | Relative <br> Frequency |
| :---: | ---: |
| 10 up to 20 | $12 / 56=0.214$ |
| 20 up to 30 | $15 / 56=0.268$ |
| 30 up to 40 | $25 / 56=0.446$ |
| 40 up to 50 | $4 / 56=0.071$ |
|  | Total $\approx 1$ |


b.

| Class | Cumulative Frequency | Cumulative Relative <br> Frequency |
| :---: | ---: | ---: |
| 10 up to 20 | 12 | $12 / 56=0.214$ |
| 20 up to 30 | $12+15=27$ | $27 / 56=0.482$ |
| 30 up to 40 | $12+15+25=52$ | $52 / 56=0.928$ |
| 40 up to 50 | $12+15+25+4=56$ | $56 / 56=1$ |

c. $44.6 \%$ of the observations are at least 30 but less than $40 ; 92.8 \%$ are less than 40
16.
a.

| Class | Relative <br> Frequency |
| :---: | ---: |
| 1000 up to 1100 | $2 / 16=0.125$ |
| 1100 up to 1200 | $7 / 16=0.4375$ |
| 1200 up to 1300 | $3 / 16=0.1875$ |
| 1300 up to 1400 | $4 / 16=0.25$ |

$$
\text { Total }=1
$$

$43.75 \%$ of the observations are at least 1100 but less than 1200 .
b.

| Class | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | ---: | :---: |
| 1000 up to 1100 | 2 | $2 / 16=0.125$ |
| 1100 up to 1200 | $2+7=9$ | $9 / 16=0.562$ |
| 1200 up to 1300 | $2+7+3=12$ | $12 / 16=0.75$ |
| 1300 up to 1400 | $2+7+3+4=16$ | $16 / 16=1$ |

12 of the observations are less than 1300 .
c.

17.
a.

| Class | Frequency |
| :---: | ---: |
| 15 up to 25 | 30 |
| 25 up to 35 | $50-30=20$ |
| 35 up to 45 | $120-50=70$ |
| 45 up to 55 | $130-120=10$ |

70 observations are at least 35 but less than 45 .
b.

c. $120 / 130=0.923$, so $92.3 \%$ of the observations are less than 45 .
18.
a.

| Class | Frequency |
| :---: | ---: |
| -20 up to -10 | $0.04 \times 50=2$ |
| -10 up to 0 | $0.28 \times 50=14$ |
| 0 up to 10 | $0.26 \times 50=13$ |
| 10 up to 20 | $0.22 \times 50=11$ |
| 20 up to 30 | $0.20 \times 50=10$ |
|  | Total $=50$ |

14 observations are at least -10 but less than 0 .
b.

| Class | Cumulative <br> Frequency |
| :---: | ---: |
| -20 up to -10 | $2+14=16$ |
| -10 up to 0 | $16+13=29$ |
| 0 up to 10 | $29+11=40$ |
| 10 up to 20 | $40+10=50$ |

40 observations are less than 20.
c.

19.
a.

| Class | Relative Frequency |
| :---: | ---: |
| 150 up to 200 | 0.10 |
| 200 up to 250 | $0.35-0.10=0.25$ |
| 250 up to 300 | $0.70-0.35=0.35$ |
| 300 up to 350 | $1-0.70=0.30$ |
|  | Total $=1$ |

$35 \%$ of the observations are at least 250 but less than 300.
b.

20.
a.

| Assets (in <br> billions) | Frequency |
| :---: | :---: |
| $\$ 40$ up to 70 | 9 |
| 70 up to 100 | 8 |
| 100 up to 130 | 2 |
| 130 up to 160 | 0 |
| 160 up to 190 | 1 |
|  | Total $=20$ |

b.

| Assets (in <br> billions) | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | ---: | ---: | ---: |
| $\$ 40$ up to 70 | $9 / 20=0.45$ | 9 | $9 / 20=0.45$ |
| 70 up to 100 | $8 / 20=0.40$ | $9+8=17$ | $17 / 20=0.85$ |
| 100 up to 130 | $2 / 20=0.10$ | $17+2=19$ | $19 / 20=0.95$ |
| 130 up to 160 | $0 / 20=0$ | $19+0=19$ | $19 / 20=0.95$ |
| 160 up to 190 | $1 / 20=0.05$ | $19+1=20$ | $20 / 20=1$ |

c. 2 funds had assets of at least $\$ 100$ but less than $\$ 130$ (in billions); 19 funds had assets less than $\$ 160$ billion.
d. $40 \%$ of the funds had assets of at least $\$ 70$ but less than $\$ 100$ (in billions); $95 \%$ of the funds had assets less than $\$ 130$ billion.
e.


The histogram is positively skewed.
Note: The histogram could have also been made with relative frequencies. It would have had the same positive skewness.
21.
a.

| Texts | Frequency |
| :---: | :---: |
| 500 up to 600 | 4 |
| 600 up to 700 | 7 |
| 700 up to 800 | 5 |
| 800 up to 900 | 4 |
| 900 up to 1000 | 5 |
|  | Total $=25$ |

b.

| Texts | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | :---: | ---: | ---: |
| 500 up to 600 | $4 / 25=0.16$ | 4 | $4 / 25=0.16$ |
| 600 up to 700 | $7 / 25=0.28$ | $4+7=11$ | $11 / 25=0.44$ |
| 700 up to 800 | $5 / 25=0.20$ | $11+5=16$ | $16 / 25=0.64$ |
| 800 up to 900 | $4 / 25=0.16$ | $16+4=20$ | $20 / 25=0.80$ |
| 900 up to 1000 | $5 / 25=0.20$ | $20+5=25$ | $25 / 25=1$ |
| Total | 1 |  |  |

c. 7 teens sent at least 600 but less than 700 texts; 16 sent less than 800 texts.
d. $16 \%$ of the teens sent at least 500 but less than 600 texts; $44 \%$ of them sent less than 700 texts.
e.


The distribution is not symmetric; it is slightly positively skewed.
22.
a.

| Temperature | Frequency |
| :---: | :---: |
| 60 up to 70 | 2 |
| 70 up to 80 | 7 |
| 80 up to 90 | 14 |
| 90 up to 100 | 10 |
|  | Total $=33$ |

b.

| Temperature | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | :---: | :---: | :---: |
| 60 up to 70 | $2 / 33=0.061$ | 2 | $2 / 33=0.061$ |
| 70 up to 80 | $7 / 33=0.212$ | $2+7=9$ | $9 / 33=0.273$ |
| 80 up to 90 | $14 / 33=0.424$ | $9+14=23$ | $23 / 33=0.697$ |
| 90 up to 100 | $10 / 33=0.303$ | $23+10=33$ | $33 / 33=1$ |
|  | Total $=1$ |  |  |

c. 9 cities had temperatures less than $80^{\circ}$.
d. $42.4 \%$ of the cities recorded temperatures of at least $80^{\circ}$ but less than $90^{\circ} ; 69.7 \%$ of the cities had temperatures less than $90^{\circ}$.
e.


The distribution is slightly negatively skewed.
23.
a.

| SAT Scores | Frequency |
| :---: | :---: |
| 450 up to 500 | 6 |
| 501 up to 550 | 24 |
| 551 up to 600 | 15 |
| 601 up to 650 | 5 |
|  | Total $=50$ |

Fifteen states had scores of at least 551 but less than 600 .
b.

| SAT Scores | Relative <br> Frequency | Cumulative Frequency | Cumulative Relative Frequency |
| :---: | :---: | :---: | :---: |
| 450 up to 500 | $6 / 50=0.12$ | 6 | $6 / 50=0.12$ |
| 501 up to 550 | $24 / 50=0.48$ | $6+24=30$ | $30 / 50=0.60$ |
| 551 up to 600 | $15 / 50=0.30$ | $30+15=45$ | $45 / 50=0.90$ |
| 601 up to 650 | $5 / 50=0.10$ | $45+5=50$ | $50 / 50=1$ |
|  | Total $=1$ |  |  |

c. 30 states had scores less than 551 .
d. $30 \%$ of the states had scores between 551 and $600 ; 60 \%$ of the states had scores less than 551.
e.


The histogram is positively skewed.
24.
a.

| Vacancy <br> Rate (\%) | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | ---: | ---: | ---: |
| 0 up to 3 | $5 / 5=0.10$ | 5 | 0.10 |
| 3 up to 6 | $10 / 50=0.20$ | $5+10=15$ | $0.10+0.20=0.30$ |
| 6 up to 9 | $20 / 50=0.40$ | $15+20=35$ | $0.30+0.40=0.70$ |
| 9 up to 12 | $10 / 50=0.20$ | $35+10=45$ | $0.70+0.20=0.90$ |
| 12 up to 15 | $5 / 50=0.10$ | $45+5=50$ | $0.90+0.10=1$ |
|  | Total $=1$ |  |  |

b. 45 cities had a vacancy rate of less than $12 \% ; 40 \%$ of the cities had a vacancy rate of at least $6 \%$ but less than $9 \% ; 70 \%$ of the cities had a vacancy rate of less than $9 \%$.
C.


The distribution is symmetric.
25.
a.

| Age | Frequency | Cumulative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | ---: | ---: | ---: |
| 15 up to 20 | $0.10(2000)=200$ | 200 | 0.10 |
| 20 up to 25 | $0.25(2000)=500$ | $200+500=700$ | $0.10+0.25=0.35$ |
| 25 up to 30 | $0.28(2000)=560$ | $700+560=1260$ | $0.35+0.28=0.63$ |
| 30 up to 35 | $0.24(2000)=480$ | $1260+480=1740$ | $0.63+0.24=0.87$ |
| 35 up to 40 | $0.11(2000)=220$ | $1740+220=1960$ | $0.87+0.11=0.98$ |
| 40 up to 45 | $0.02(2000)=40$ | $1960+40=2000$ | $0.98+0.02=1$ |
|  | Total $=2000$ |  |  |

b. $28 \%$ of the women were at least 25 but less than 30 years old; $87 \%$ were less than 35 years old.
c.


The distribution appears to be relatively symmetric with possibly a slight positive skew.
d.


If we draw a horizontal line that corresponds to the 0.5 value on the vertical axis ( $50 \%$ of the distribution), it will intersect the ogive at approximately 28 years old.
26.
a.

| Age | Frequency | Relative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | ---: | ---: | ---: |
| 18 up to 22 | 45 | $45 / 100=0.45$ | 0.45 |
| 22 up to 26 | $70-45=25$ | $25 / 100=0.25$ | $0.45+0.25=0.70$ |
| 26 up to 30 | $85-70=15$ | $15 / 100=0.15$ | $0.70+0.15=0.85$ |
| 30 up to 34 | $96-85=11$ | $11 / 100=0.11$ | $0.85+0.11=0.96$ |
| 34 up to 38 | $100-96=4$ | $4 / 100=0.04$ | $0.96+0.04=1$ |
|  | Total $=100$ | Total $=1$ |  |

b. Fifteen guests were at least 26 but less than 30 years old; $25 \%$ of the guests were at least 22 but less than 26 years old; $96 \%$ of the guests were younger than 34 years old; $4 \%$ were 34 years or older.
c.


The histogram shows a positively skewed data set reflecting the relatively young age of the nightclub's guests.
27.

| Stem | Leaf |
| ---: | :--- |
| 2. | 368 |
| 3. | 0223456 |
| 4. | 0222567 |
| 5. | 455 |

This distribution is symmetric. There are the same number of observations on each end of the data, and the same number of observations in the middle.
28.

| Stem | Leaf |
| :---: | :---: |
| -8 | 75532000 |
| -7 | 9753321 |
| -6 | 554 |
| -5 | 20 |

(Keep in mind that these values are negative - thus, the ordering of values in the leaf.)
The distribution is not symmetric; it is positively skewed. Most of the numbers are in the lower stems of -8 and - 7 .
29.

| Stem | Leaf |
| :---: | :--- |
| 99. | 678 |
| 100. | 45 |
| 101. | 022233556 |
| 102 | 0122345 |

The temperatures ranged from a low of 99.6 to a high of 102.5. The distribution is not symmetric - it has negative skew. The majority of patients recorded a temperature higher than 101.
30.

| Stem | Leaf |
| :---: | :--- |
| 7 | 346788 |
| 8 | 0123444478 |
| 9 | 0001122233444445666889 |
| 10 | 67 |

Temperatures ranged from a low of 73 to a high of 107. The distribution is not symmetric - it has negative skew. Temperatures in 90 s were the most frequent.
31.

| Stem | Leaf |
| ---: | :--- |
| 6 | 55677 |
| 7 | 00011223335589 |
| 8 | 000112 |

The officers concerns are warranted. The data shows that the majority of cars exceed the 65 miles-per-hour limit.
32.

| Spain <br> Stem | Leaf |
| ---: | :--- |
| 2 | 11123344555678999 |
| 3 | 002 |


| Netherlands |
| :--- |
| Stem |
| 2 |
| 233455566677779 |
| 3 | | Leaf |
| :--- |

Spain has a relatively younger team compared to Netherlands. Spain's ages range from 21 to 32, while Netherlands' ages range from 22 to 39 . The majority of players in both teams are in their 20s. However, Netherlands has a couple of more players in their 30s than Spain.
33.


There is a negative linear relationship between x and y . As x increases, y tends to decrease.
34.

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There is no relationship between x and y .
35.


There is a negative relationship between x and y . As x increases, y tends to decrease.
36.


There is a positive relationship between number of hours spent studying and grades. As the number of hours spent studying increases, grades tend to increase.
37.


The results support the finding. As a mother's weight gain increases, the newborn's birth weight tends to increase as well.
38.


There is a slightly negative relationship between the two assets. Therefore, it would be wise for the investor to include them in her portfolio.
39.


There is a positive relationship. The realtor can conclude that generally, with higher home prices, the number of days to sell the home will tend to be higher as well.
40.
a.


| Yes | $2 / 20=0.10$ | $9 / 20=0.45$ |
| :--- | ---: | ---: |
| No | $18 / 20=0.90$ | $11 / 20=0.55$ |
|  | Total =1 | Total = |

The sample responses show the difference regarding smoking behavior in the two states. Notice that $45 \%$ of the households in Kentucky allow smoking at home whereas only $10 \%$ do so in Utah.
b.


The bar chart shows that smoking at home is much more common in Kentucky than in Utah.
41.
a.

| Rating | Frequency | Relative <br> Frequency |
| :---: | :---: | ---: |
| Outstanding | 0 | $0 / 28=0$ |
| Good | 8 | $8 / 28=0.286$ |
| Ok | 7 | $7 / 28=0.250$ |
| Please Get Help | 13 | $13 / 28=0.464$ |
|  | Total $=28$ | Total $=1$ |

From the relative frequency distribution, we can conclude that the majority of the evaluations were either "OK" or "Please Get Help". Notice that none of the responses included "Outstanding". Therefore, it is necessary for the owner of the restaurant to improve the service and/or experience provided.
b.


The pie chart which depicts categorical data in percentage values demonstrates the poor evaluations received.


The bar chart is another way to depict categorical data effectively. We notice that the highest bar is the last category "Please Get Help" and that there are no responses given for "Outstanding."
42.
a.



The charts reveal parent preferences. Sixty-five percent of parents want their children to have a profession such as a doctor, lawyer, banker or president. Less preferable are other professions such humanitarian-aid worker or a movie star.
b. Since $9 \%$ of parents want their children to become an athlete, $550 \times 0.09 \approx 50$. Therefore, among 550 parents approximately 50 parents want their kids to become an athlete.
43.
a.

| Classes | Frequency |
| :--- | :--- |


| -20 up to -10 | 4 |
| :---: | :---: |
| -10 up to 0 | 7 |
| 0 up 10 | 9 |
| 10 up 20 | 3 |
| 20 up to 30 | 1 |
|  | Total $=24$ |

b.

| Classes (in \%) | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative Relative Frequency |
| :---: | :---: | :---: | :---: |
| -20 up to -10 | $4 / 24=0.167$ | 4 | $4 / 24=0.167$ |
| -10 up to 0 | $4 / 24=0.292$ | $4+7=11$ | $11 / 24=0.458$ |
| 0 up 10 | $9 / 24=0.375$ | $11+9=20$ | $20 / 24=0.833$ |
| 10 up 20 | $3 / 24=0.125$ | $20+3=23$ | $23 / 24=0.958$ |
| 20 up to 30 | $1 / 24=0.042$ | $23+1=24$ | $24 / 24=1$ |
|  | Total $\approx 1$ |  |  |

c. Nine funds had returns of at least $0 \%$ but less than $10 \%$; there were 4 funds with returns of $10 \%$ or more.
d. $12.5 \%$ of the funds had a return of at least $10 \%$ but not greater than $20 \% ; 95.8 \%$ of the funds had returns less than $20 \%$.
44.
a.

| Region | Relative Frequency |
| :---: | ---: |
| Northeast | $6,166 / 37,276=0.165$ |
| Midwest | $7,237 / 37,276=0.194$ |
| South | $15,501 / 37,276=0.416$ |
| West | $8,372 / 37,276=0.225$ |
|  | Total $=1$ |

19.4\% of people living below the poverty level live in the Midwest region.
b.



These charts show that the region with the highest percentage of people who live below the poverty level live in the South, and the lowest percentage is in the Northeast.
45.
a.

| Resolution | Relative Frequency |
| :---: | ---: |
| Saving more | $328 / 1026=0.320$ |
| Paying down debt | $257 / 1026=0.250$ |
| Making more income | $154 / 1026=0.150$ |
| Spending less | $133 / 1026=0.130$ |
| Investing more | $103 / 1026=0.100$ |
| Saving for large purchase | $41 / 1026=0.040$ |
| Don't know | $10 / 1026=0.010$ |
|  | Total $=1$ |

$25 \%$ of the sample said paying down debt was the top financial resolution.
b.


The bar chart shows that saving more in general is the top financial resolution, followed by paying down debt. Only a small portion of the sample didn't know their financial resolution.
46.
a.

| Response | Frequency |
| :---: | ---: |
| A few days | $0.21(3057)=642$ |
| A few long weekends | $0.18(3057)=550$ |
| One week | $0.36(3057)=1101$ |
| Two weeks | $0.25(3057)=764$ |
|  | Total $=3057$ |

Approximately 1101 people are going to take a one week vacation.
b.

47.
a.


Notice that the most frequent responses were regards to paying off debts or putting it in the bank.
b. Since $11 \%$ of 1026 respondents said they would spend the refund, $0.11(1026) \approx 113$. Therefore, approximately 113 of the respondents would spend the tax refund.
48.
a.
$\qquad$
Drug Relative Frequency

| Topomax | $1825.4 / 5718.4=0.319$ |
| :---: | ---: |
| Lamictal | $1684.3 / 5718.4=0.295$ |
| Depakote | $770.4 / 5718.4=0.135$ |
| Lyrica | $727.8 / 5718.4=0.127$ |
| Keppra | $710.5 / 5718.4=0.124$ |
|  | Total $=1$ |

b. Lamictal accounted for $29.5 \%$ of the sales.
c.

49.
a.

| Attendance | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | ---: | ---: | ---: |
| 1000 up to 1250 | $5 / 60=0.083$ | 5 | 0.083 |
| 1250 up to 1500 | $6 / 60=0.10$ | $5+6=11$ | $0.083+0.10=0.183$ |
| 1500 up to 1750 | $10 / 60=0.167$ | $11+10=21$ | $0.183+0.167=0.35$ |
| 1750 up to 2000 | $20 / 60=0.333$ | $21+20=41$ | $0.35+0.333=0.683$ |
| 2000 up to 2250 | $15 / 60=0.25$ | $41+15=56$ | $0.683+0.25=0.933$ |
| 2250 up to 2500 | $4 / 60=0.067$ | $56+4=60$ | $0.933+0.067=1$ |
|  | Total =1 |  |  |

b. The most likely attendance range is from 1,750 up to 2,000 with a $33 \%$ frequency; there were 41 times out of 60 that attendance was less than 2,000 .
c. Attendance was at least 1,750 but less than $2,00033.3 \%$ of the time; Attendance was less than 1,750 people $35 \%$ of the time; Therefore, attendance was 1,750 or more ( 1 $-0.35=0.65), 65 \%$ of the time.
d.


The histogram is not symmetric; it is negatively skewed.
50.
a.

| Average <br> MPG | Relative <br> frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | ---: | ---: | ---: |
| 15 up to 20 | $15 / 80=0.1875$ | 15 | 0.1875 |
| 20 up to 25 | $30 / 80=0.375$ | $15+30=45$ | $45 / 80=0.5625$ |
| 25 up to 30 | $15 / 80=0.1875$ | $45+15=60$ | $60 / 80=0.75$ |
| 30 up to 35 | $10 / 80=0.125$ | $60+10=70$ | $70 / 80=0.875$ |
| 35 up to 40 | $7 / 80=0.0875$ | $70+7=77$ | $77 / 80=0.9625$ |
| 40 up to 45 | $3 / 80=0.0375$ | $77+3=80$ | $80 / 80=1$ |
|  | Total $=1$ |  |  |

b.
than $30 \mathrm{mpg} ; 37.5 \%$ of the cars got at least 20 but less than $25 \mathrm{mpg} ; 87.5 \%$ of the cars got less than 35 mpg ; Since $87.5 \%$ got less than 35 mpg , ( $1-0.875=0.125$ ), $12.5 \%$ of the cars got 35 mpg or more.
c.

The histogram is not symmetric; it is positively skewed.
51.

52.
d. There were 4 people out of 25 with a net worth greater than $\$ 20$ billion. Therefore, $4 / 25=0.16$, so $16 \%$ of the wealthiest people had net worth greater than $\$ 20$ billion.
e. Two people had a net worth less than $\$ 10$ billion, which is $2 / 25=0.08$, or $8 \%$.

From the previous question, we know that $16 \%$ had a net worth greater than $\$ 20$ billion. Therefore, $16 \%+8 \%=24 \%$ did nothave a net worth between $\$ 10$ and $\$ 20$ billion. Therefore, $(1-0.24)=0.76$, so $76 \%$ had net worth between $\$ 10$ billion and \$20 billion.
f.

| Steam | Leaf |
| :---: | :--- |
| 3 | 66 |
| 4 | 47 |
| 5 | 3346 |
| 6 | 01556779 |
| 7 | 013337899 |

The distribution is not symmetric - it is negatively skewed. The majority of ages range from the 60 s to 70 s . Table 2.16 shows the majority of ages to be in the 50 s and 60s. Further, this diagram shows ages ranging from 36 to 79, whereas Table 2.16 has ages ranging from 36 to 90 .
51.

| Steam | Leaf |
| :---: | :--- |
| 0. | 8899 |
| 1. | 00112222334456688999 |
| 2. | 0099 |
| 3. | 07 |

The vast majority of the PEG ratios fall in the 1 range. The diagram is somewhat positively skewed; there are a few firms with relatively high PEG ratios.
52.
a.



These charts show that the majority (60\%) of houses were either Ranch or Colonial, but also $40 \%$ were either Contemporary or some other type.
b.

To figure out how
wide to make the classes, find the highest price and subtract the lowest price to get the range. That is $\$ 568,000-\$ 300,000=\$ 268,000$. Then since we want 7 classes, divide the range by $7: 268,000 / 7=\$ 38,386$. However, for ease of interpretation, round to the most sensible number: $\$ 50,000$. Therefore, our classes will have a width of $\$ 50,000$, starting at $\$ 300,000$.

| Classes | Frequency |
| :---: | :---: |
| 300,000 up to 350,000 | 4 |


| 350,000 up to 400,000 | 6 |
| :--- | :---: |
| 400,000 up to 450,000 | 4 |
| 450,000 up to 500,000 | 2 |
| 500,000 up to 550,000 | 3 |
| 550,000 up to 600,000 | 1 |
|  | Total $=20$ |

c.



The histogram shows that the most frequent house price is in the $\$ 350,000$ up to $\$ 400,000$ range. The ogive shows that the middle price (with a frequency of $10 / 20$ or $50 \%$ ) is about $\$ 400,000$.
53.


The scatter plot shows that the relation between Advertising and Sales is positive. The positive trend demonstrates that an increase in advertising will tend to increase sales.
54.


The scatterplot reveals no clear relationship between PPG and MPG.

## Case Study 2.1

Proportion of Nike's Net Sales by Region:

|  | 2000 | 2009 |
| :--- | :---: | :---: |
| US Region | $4732.1 / 8588.3=0.551$ | $6542.9 / 16661.8=0.392$ |


| EMEA Region | $2350.9 / 8588.3=0.274$ | $5512.2 / 16661.8=0.331$ |
| :--- | ---: | ---: |
| Asia Pacific Region | $955.1 / 8588.3=0.111$ | $3322 / 16661.8=0.199$ |
| Americas Region | $550.2 / 8588.3=0.064$ | $1284.7 / 16661.8=0.077$ |
|  | Total $=1$ | Total $\approx 1$ |

Proportion of Adidas' Net Sales by Region (From Table 2.6):

|  | 2000 | 2 |
| :--- | ---: | ---: |
| Europe | 0.492 | 0.423 |
| North America | 0.328 | 0.228 |
| Asia | 0.151 | 0.252 |
| Latin America | 0.029 | 0.097 |
|  | Total $=1$ | Total $=1$ |

## Case Study 2.2

- The net profit margin is a firm's net profit after taxes to revenue. It is measured in percentage, showing the percentage of net income per dollar in sales or other operating income.

| Net Profit Margin | Frequency | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | :---: | ---: | :---: | :---: |
| $-10 \%$ up to $-5 \%$ | 1 | $1 / 32=0.031$ | 1 | $1 / 32=0.031$ |
| -5 up to 0 | 6 | $6 / 32=0.188$ | 7 | $7 / 32=0.219$ |
| 0 up to 5 | 10 | $10 / 32=0.313$ | 17 | $17 / 32=0.531$ |
| 5 up to 10 | 11 | $11 / 32=0.344$ | 28 | $28 / 32=0.875$ |
| 10 up to 15 | 2 | $2 / 32=0.063$ | 30 | $30 / 32=0.938$ |
| 15 up to 20 | 2 | $2 / 32=0.063$ | 32 | $32 / 32=1$ |
|  | Total $=32$ | Total $\approx 1$ |  |  |




- The data tends to cluster between $0 \%$ and $10 \%$, as shown in the histogram. The net profit margins range from $-5.19 \%$ to $19.95 \%$. Approximately $53 \%$ of the Firms have a net profit margin below $5 \%$.


## Case Study 2.3

| Median Housing <br> Price (in $\$ 1000 \mathrm{~s}$ ) | Frequency | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :--- | ---: | ---: | ---: | ---: |
| $\$ 0$ up to $\$ 100$ | 6 | 0.12 | 6 | 0.12 |
| $\$ 100$ up to $\$ 200$ | 29 | 0.58 | 35 | 0.7 |
| $\$ 200$ up to $\$ 300$ | 11 | 0.22 | 46 | 0.92 |
| $\$ 300$ up to $\$ 400$ | 2 | 0.04 | 48 | 0.96 |
| $\$ 400$ up to $\$ 500$ | 2 | 0.04 | 50 | 1 |
|  | Total $=50$ | Total $=1$ |  |  |

Chapter 02 - Tabular and Graphical Methods



- The majority of median housing prices (70\%) are below $\$ 200,000$. The prices range from $\$ 82,700$ up to $\$ 477,700$. The distribution is positively skewed with only 4 states having a median housing price above $\$ 400,000$.

