# **Test Bank**

# Calculus

**TENTH EDITION** 

**Ron Larson** 

**Bruce Edwards** 





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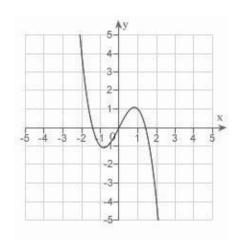
## P.1 Graphs and Models

## **Multiple Choice**

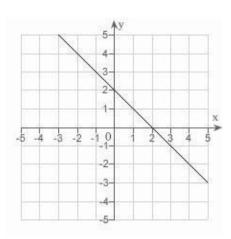
Identify the choice that best completes the statement or answers the question.

Which of the following is the correct graph of  $y = -\sqrt{2 - x^2}$ ? 1.

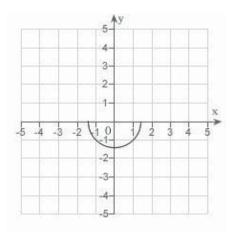
a.



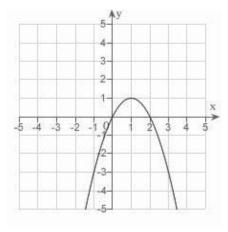
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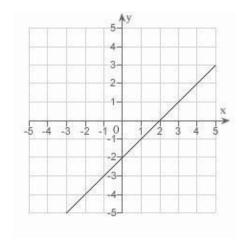


b.



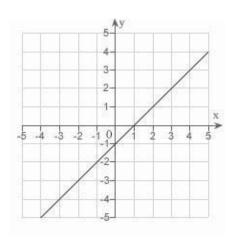
e.



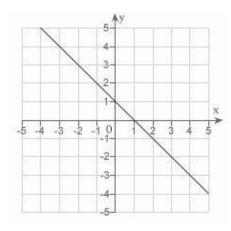


2. Which of the following is the correct graph of  $y = x - x^3$ ?

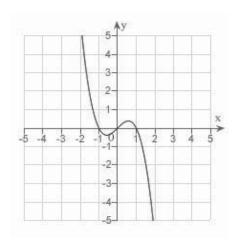
a.



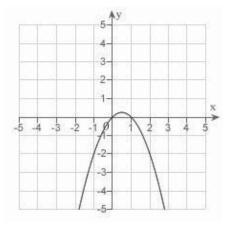
d.

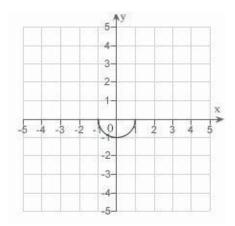


b.



e.





#### 3. Find all intercepts:

$$y = x^2 - x - 12$$

- a. x-intercepts: (4,0), (-3,0); y-intercepts: (0,4), (0,3)
- b. x-intercept: (12, 0); y-intercepts: (0, 4), (0, 3)
- c. x-intercepts: (4, 0), (-3,0); y-intercept: (0, -12)
- d. x-intercepts: (4, 0), (-3,0); y-intercepts: (0, -12), (0, 12)
- e. x-intercept: (-3, 0); y-intercept: (0, -12)

#### Find all intercepts:

$$y = (x+5)\sqrt{4-x^2}$$

- a. x-intercepts: (-5, 0), (-2, 0), (2, 0); y-intercepts: (0, 0), (0, 10)
- b. x-intercepts: (-5, 0), (2, 0); y-intercept: (0, 10)
- c. x-intercepts: (-5, 0), (2, 0); y-intercept: (0, -10)
- d. x-intercepts: (-5, 0), (-2, 0), (2, 0); y-intercept: (0, 10)
- e. x-intercepts: (-5, 0), (-2, 0), (2, 0); y-intercept: (0, -10)
  - 5. Test for symmetry with respect to each axis and to the origin.

$$x^2y^2 = 8$$

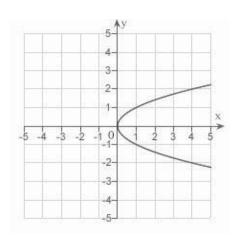
- a. symmetric with respect to the origin
- b. symmetric with respect to the x-axis
- c. symmetric with respect to the y-axis
- d. no symmetry
- e. A, B, and C
- Test for symmetry with respect to each axis and to the origin.

$$y = \frac{x^2 + 2}{x}$$

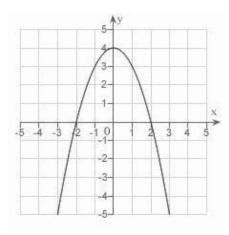
- a. symmetric with respect to the origin
- b. symmetric with respect to the *y*-axis
- c. symmetric with respect to the *x*-axis
- d. both B and C
- e. no symmetry

$$x = 4 - y^2$$

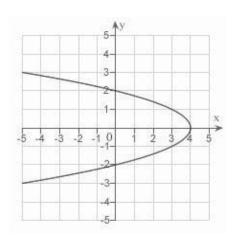
a



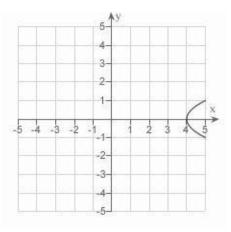
d.

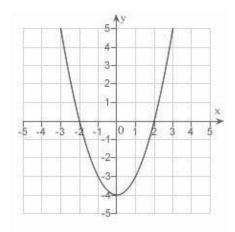


b.



e.

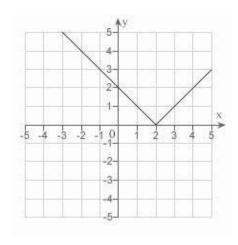




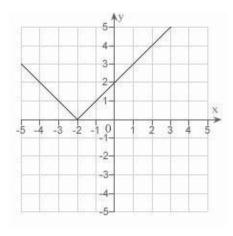
8. Sketch the graph of the equation:

$$y = |x + 2|$$

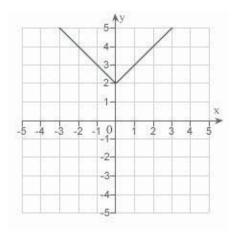
a.



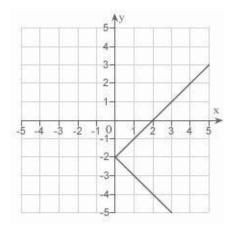
d.



b.



e. none of the above

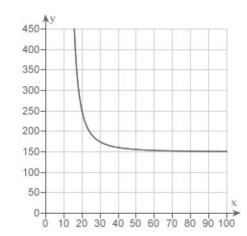


9. Find the points of intersection of the graphs of the equations:

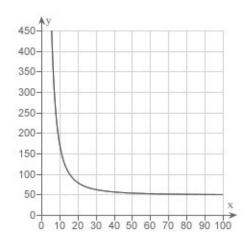
$$x = y^2 - 3$$

$$y = x + 1$$

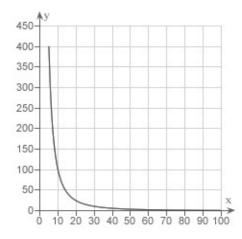
- a. (-2, 1), (-1, 2)b. (-2, 0), (1, 2)c. (-2, -1), (1, 2)d. (2, -1), (-1, 2)e. (-2, -3), (-1, 2)
- The resistance y in ohms of 1000 feet of solid metal wire at  $77^{\circ}F$  can be 10. approximated by the model  $y = \frac{10,000}{x^2} - 0.57$ ,  $5 \le x \le 100$ , where x is the diameter of the wire in mils (0.001 in). Use a graphing utility to graph the model  $y = \frac{10,000}{x^2} - 0.57$ ,  $5 \le x \le 100$ .



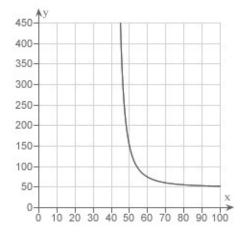
d.



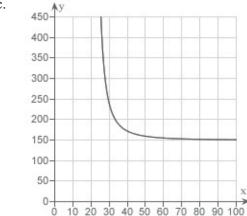
b.



e.



c.



The resistance y in ohms of 1000 feet of solid metal wire at  $77^{\circ}F$  can be 11.

approximated by the model  $y = \frac{12,000}{x^2} - 0.46$ ,  $5 \le x \le 100$ , where x is the diameter of the wire in

mils (0.001 in). If the diameter of the wire is doubled, the resistance is changed by approximately what factor? In determining your answer, you can ignore the constant -0.46.

- $\frac{1}{2}$
- b. 5
- d. 5
- 1 e.  $\overline{4}$

12. Test for symmetry with respect to each axis and to the origin.

$$y = x^2 - 8$$

- a. symmetric with respect to the origin
- b. symmetric with respect to the *y*-axis
- c. symmetric with respect to the *x*-axis
- d. both B and C
- e. no symmetry

\_\_\_\_ 13. Test for symmetry with respect to each axis and to the origin.

$$|y| - x = 6$$

- a. symmetric with respect to the origin
- b. symmetric with respect to the *x*-axis
- c. symmetric with respect to the *y*-axis
- d. no symmetry
- e. A, B, and C

14. Find all intercepts:

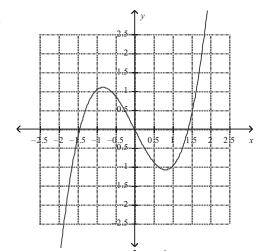
$$y^2 = x^3 - 25x$$

- a. *x*-intercepts: (0,0), (5,0), (-5,0); *y*-intercept: (0, -25)
- b. x-intercepts: (0,0), (5,0); y-intercept: (0,0)
- c. x-intercepts: (0,0), (5,0), (-5,0); y-intercept: (0,0)
- d. x-intercepts: (0,0), (5,0); y-intercept: (0,5)
- e. x-intercepts: (0,0), (5,0), (25,0); y-intercept: (0,0)

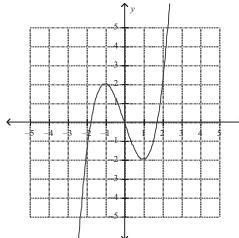
15. Sketch the graph of the equation:

$$y = x^3 - 3x$$

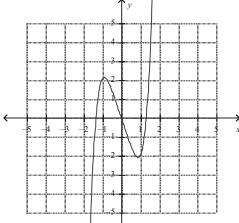
a.

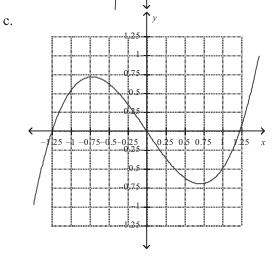


d.



b.





e. none of the above

## P.1 Graphs and Models Answer Section

#### **MULTIPLE CHOICE**

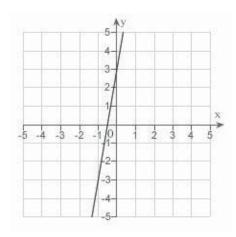
1.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Identify the gr	MSC:	Skill						
2.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Identify the gr	MSC:	Skill						
3.	ANS:	C	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Calculate the	MSC:	Skill						
4.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Calculate the	intercep	ots of an equation	on			MSC:	Skill	
5.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Identify the ty	pe of s	ymmetry of the	graph	of an equation		MSC:	Skill	
6.	ANS:	A	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Identify the ty	pe of s	ymmetry of the	graph	of an equation		MSC:	Skill	
7.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Graph a quad	ratic eq	uation in y				MSC:	Skill	
8.	ANS:	D	PTS:	1	DIF:	Med	REF:	Section 0.1	
OBJ:	Graph an abso	MSC:	Skill						
9.	ANS:	C	PTS:	1	DIF:	Med	REF:	Section 0.1	
OBJ:	Calculate the	points o	of intersection o	f the g	raphs of equation	ons	MSC:	Skill	
10.	ANS:	В	PTS:	1	DIF:	Med	REF:	Section 0.1	
OBJ:	Plot a rational	l model	using the capal	oilities	of a graphing u	tility	MSC:	Application	
11.	ANS:	E	PTS:	1	DIF:	Med	REF:	Section 0.1	
OBJ:	Interpret a rat	ional m	odel				MSC:	Application	
12.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Identify the ty	pe of s	ymmetry of the	graph	of an equation		MSC:	Skill	
13.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Identify the ty	pe of s	ymmetry of the	graph	of an equation		MSC:	Skill	
14.	ANS:	C	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	: Calculate the intercepts of an equation MSC:								
15.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.1	
OBJ:	Graph an equa	ation in	y				MSC:	Skill	

## P.2 Linear Models and Rates of Change

## **Multiple Choice**

Identify the choice that best completes the statement or answers the question.

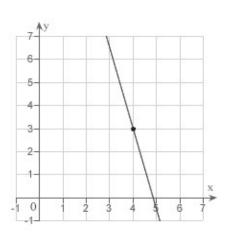
Estimate the slope of the line from the graph. 1.



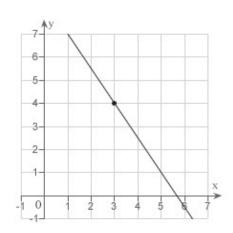
- e.

Sketch the line passing through the point (3, 4) with the slope  $-\frac{3}{2}$ . 2.

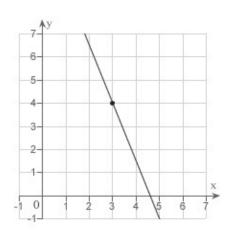
a.



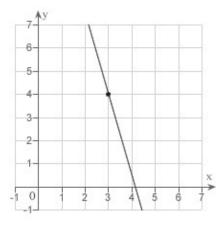
d.



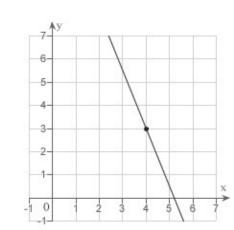
b.



e.



c.



3. Find the slope of the line passing through the pair of points.

- a.  $\frac{3}{5}$
- b.  $-\frac{5}{3}$
- c.  $\frac{5}{3}$
- d.
- e.  $-\frac{3}{5}$

- Find the slope of the line passing through the points  $\left(-\frac{1}{8}, \frac{8}{3}\right)$  and  $\left(-\frac{3}{16}, \frac{1}{24}\right)$ . 4.
- a. 63
- -21
- c. 42
- d. 21
- e. -42
- If a line has slope m = -4 and passes through the point (4, 8), through which of the following points does the line also pass?
- a. (1, 20)
- b. (1, 12)
- c. (1, 0)
- d. (8, -16)
- e. (8, -24)
- A moving conveyor is built to rise 5 meters for every 7 meters of horizontal change. 6. Find the slope of the conveyor.
- a. 0
- $\frac{5}{7}$

- A moving conveyor is built to rise 1 meter for every 5 meters of horizontal change. Suppose the conveyor runs between two floors in a factory. Find the length of the conveyor if the vertical distance between floors is 10 meters. Round your answer to the nearest meter.
- 61 meters
- 39 meters
- c. 51 meters
- d. 50 meters
- e. 41 meters

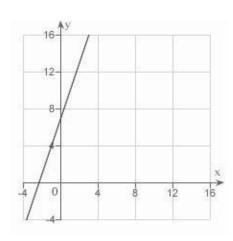
- Find the slope of the line x + 3y = 15. 8.

- Find the *y*-intercept of the line x + 4y = 8. 9.
- a. (0, 2)
- b. (0, 4)
- c. (0, 8)
- d. (4, 0)
- e. (2, 0)
- Find an equation of the line that passes through the point (7, 2) and has the slope m10. that is undefined.
- a. y = 7
- b. x = 7
- c. y = 2
- d. x = 2
- e. y = 7x
- Find an equation of the line that passes through the point (-11, -9) and has the slope
- a.  $y = \frac{9}{2}x \frac{81}{2}$
- b.  $y = \frac{9}{2}x + \frac{81}{2}$
- c.  $y = \frac{9}{2}x + 162$ d.  $y = \frac{9}{2}x$

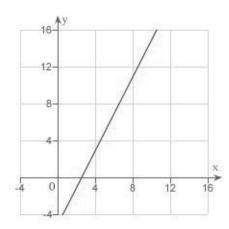
- Find an equation of the line that passes through the points (18, -7) and (-18, 23). 12.
- $y = -\frac{5}{6}x 8$
- b.  $y = \frac{5}{6}x 8$
- c.  $y = \frac{5}{6}x + 8$
- $y = -\frac{5}{6}x + 8$
- e.  $y = -\frac{5}{6}x$
- Find an equation of the line that passes through the points  $\left(-\frac{8}{11}, -\frac{70}{11}\right)$  and 13.
- $\left(\frac{3}{2}, -\frac{21}{4}\right)$ .
- a.  $y = \frac{1}{2}x$
- b.  $y = \frac{1}{2}x + 6$
- $c. \qquad y = \frac{1}{2}x + 12$
- d.  $y = \frac{1}{2}x 12$
- e.  $y = \frac{1}{2}x 6$
- Use the result, "the line with intercepts (a, 0) and (0, b) has the equation  $\frac{x}{a} + \frac{y}{b} = 1$ ,  $a \neq 0, b \neq 0$ ", to write an equation of the line with x-intercept: (8,0) and y-intercept: (0,7).
- 8x 7y 8 = 0
- b. 7x 8y + 7 = 0
- c. 8x + 7y + 8 = 0
- d. 7x + 8y + 56 = 0
- e. 7x + 8y 56 = 0

15. Sketch a graph of the equation y - 8 = 2(x + 4).

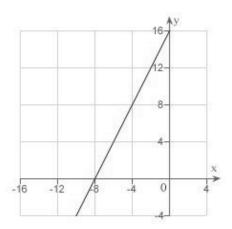
a.



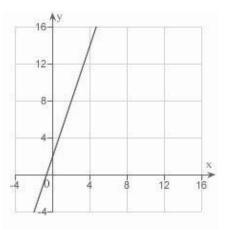
d.

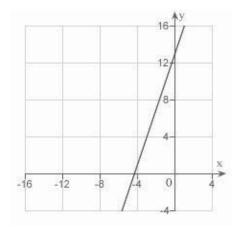


b.



e.





17

\_\_\_\_ 16. Write an equation of the line that passes through the given point and is perpendicular to the given line.

Point Line

$$(-1, -7)$$
  $x = 6$ 

- a. y = 7
- b. y = -7
- c. y = -1
- d. x = -1
- e. x = 1

\_\_\_\_ 17. Write an equation of the line that passes through the given point and is parallel to the given line.

Point

$$(3,-4) \quad -2x-5y=9$$

- a. -2x 5y = 14
- b. -2x 5y = 23
- c. 2x 5y = 14
- d. -2x + 5y = -26
- e. 2x 5y = 23

\_\_\_\_ 18. Write an equation of the line that passes through the point (-6, 4) and is perpendicular to the line x + y = 5.

- a. x-y+10=0
- b. x y + 2 = 0
- c. x + y 2 = 0
- d. x + y + 10 = 0
- e. x + y 5 = 0

\_\_\_\_\_ 19. Write an equation of the line that passes through the point  $\left(\frac{5}{4}, \frac{5}{8}\right)$  and is parallel to the line 7x - 3y = 0.

- a. 56x 24y 55 = 0
- b. 56x + 12y 55 = 0
- c. 56x 8y + 55 = 0
- d. 56x + 6y + 55 = 0
- e. 56x + 4y 55 = 0

- $\frac{20}{\$800}$  A real estate office handles an apartment complex with 50 units. When the rent is  $\frac{\$800}{\$800}$  per month, all 50 units are occupied. However, when the rent is \$845, the average number of occupied units drops to 47. Assume that the relationship between the monthly rent p and the demand x is linear. Write a linear equation giving the demand x in terms of the rent p.
- a.  $x = \frac{1}{15} (1595 p)$
- b.  $x = \frac{1}{15} \left( 1505 + p \right)$
- c.  $x = \frac{1}{45} \left( 1550 + p \right)$
- d.  $x = \frac{1}{15} (1550 p)$
- e.  $x = \frac{1}{45} (1595 p)$
- $\frac{21}{$600}$  A real estate office handles an apartment complex with 50 units. When the rent is  $\frac{600}{$600}$  per month, all 50 units are occupied. However, when the rent is  $\frac{645}{$600}$ , the average number of occupied units drops to 47. Assume that the relationship between the monthly rent p and the demand x is linear. Predict the number of units occupied if the rent is raised to  $\frac{660}{$600}$ .
- a. 43 units
- b. 54 units
- c. 57 units
- d. 49 units
- e. 46 units
- \_\_\_\_ 22. Find the distance between the point (-4,7) and line x-y-2=0 using the formula,

Distance =  $\frac{\left|Ax_1 + By_1 + C\right|}{\sqrt{A^2 + B^2}}$  for the distance between the point  $(x_1, y_1)$  and the line

$$Ax + By + C = 0.$$

- a.  $\frac{11\sqrt{2}}{2}$
- b.  $\frac{4\sqrt{3}}{3}$
- c.  $\frac{13\sqrt{2}}{2}$
- d.  $\frac{9\sqrt{2}}{2}$
- e.  $\frac{6\sqrt{3}}{3}$

- Suppose that the dollar value of a product in 2008 is \$174 and the rate at which the 23. value of the product is expected to increase per year during the next 5 years is \$7.50. Write a linear equation that gives the dollar value V of the product in terms of the year t. (Let t = 0 represent 2000.) Round the numerical values in your answer to one decimal place, where applicable.
- a. V = 7.5t 159
- b. V = -7.5t 114
- c. V = -7.5t + 174
- d. V = 7.5t + 114
- e. V = 7.5t 144
- A company reimburses its sales representatives \$ 175 per day for lodging and meals plus  $45\phi$  per mile driven. Write a linear equation giving the daily cost C to the company in terms of x, the number of miles driven. Round the numerical values in your answer to two decimal places, where applicable.
- a. C = -1.75x + 45
- b. C = 0.45x + 175
- c. C = -0.45x 175
- d. C = 0.45x 175
- e. C = 1.75x 45
- A company reimburses its sales representatives \$160 per day for lodging and meals plus 42¢ per mile driven. How much does it cost the company if a sales representative drives 135 miles on a given day? Round your answer to the nearest cent.
- a. 227.20
- b. 216.70
- c. 136.35
- d. 161.35
- e. 191.70

## P.2 Linear Models and Rates of Change **Answer Section**

#### **MULTIPLE CHOICE**

1.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Estimate the	slope of	f a line from its	s graph			MSC:	Skill
2.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Sketch the lin	e passi	ng through a p	oint witl	n specified slop	e	MSC:	Skill
3.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Calculate the	slope o	of a line passing	g throug	h two points		MSC:	Skill
4.	ANS:	C	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	Calculate the	slope o	of a line passing	g throug	h two points		MSC:	Skill
5.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	Identify a poi	nt on a	line with spec	ified pro	perties		MSC:	Skill
6.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.2
MSC:	Application							
7.	ANS:	C	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	Calculate slop	pes in a	pplications				MSC:	Application
8.	ANS:	E	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	Manipulate a	linear e	equation to det	ermine i	ts slope		MSC:	Skill
9.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	Manipulate a	linear e	equation to det	ermine i	ts y-intercept		MSC:	Skill
10.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Write an equa	ation of		point on	the line and its	s slope	MSC:	Skill
11.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Write an equa	ation of	-	_	the line and its	s slope	MSC:	Skill
12.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Write an equa	ation of	a line given to	vo point	s on the line		MSC:	Skill
13.	ANS:	E	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	_	ation of	a line given to	vo point			MSC:	Skill
14.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	-		a line given it		-		MSC:	Skill
15.	ANS:	В	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	_	_	a linear equation	on			MSC:	Skill
16.	ANS:	С	PTS:	1	DIF:	Med	REF:	Section 0.2
			a line given a	point on	the line and a	line to v		
•	el/perpendicula	ar					MSC:	
17.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.2
			a line given a	point on	the line and a	line to v		
	el/perpendicula						MSC:	
18.	ANS:	A	PTS:	1	DIF:	Med	REF:	
		ation of	a line given a	point on	the line and a	line to v	which it	is perpendicular
MSC:			DTC	1	DIE	Г	DEE	G .: 0.2
19.	ANS:	A	PTS:	1	DIF:	-		Section 0.2
OBJ: MSC:		uion of	a line given a	point on	the line and a	iine to v	wnich it	is parallel
MISC:	SKIII							

20.	ANS:	D	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	Write linear e	Write linear equations in applications						
21.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Evaluate line	ar equat	tions in applica	tions			MSC:	Application
22.	ANS:	C	PTS:	1	DIF:	Med	REF:	Section 0.2
OBJ:	Calculate the	distanc	e between a po	int and	a line		MSC:	Skill
23.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Write linear equations in applications							Application
24.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Write linear equations in applications							Application
25.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.2
OBJ:	Evaluate line	ar equat	tions in applica	tions			MSC:	Application

## P.3 Functions and Their Graphs

#### **Multiple Choice**

Identify the choice that best completes the statement or answers the question.

- 1. Evaluate (if possible) the function f(x) = -6x 5 at x = -2. Simplify the result.
- a. -7
- b. 17
- c. 3
- d.
- e. undefined
- 2. Evaluate (if possible) the function  $f(x) = \sqrt{x-5}$  at x = 9. Simplify the result.
- a. 3
- b. 2
- c. -2
- d. 4
- e. undefined
- 2. Evaluate (if possible) the function  $g(x) = x^2(x+2)$  at x = t 6. Simplify the result.
- a.  $t^3 4t^2 + 12t 144$
- b.  $t^3 4t^2 + 84t 144$
- c.  $t^3 16t^2 + 84t 144$
- d.  $t^3 16t^2 + 12t 144$
- e. none of the above
- \_\_\_\_ 4. Let f(x) = 14x + 8. Then simplify the expression  $\frac{f(x) f(9)}{x 9}$ .
- a. 15
- b. 14
- c. 19
- d. 11
- e. undefined

Let 
$$g(x) = \frac{1}{\sqrt{x+15}}$$
. Evaluate the expression  $\frac{g(x)-g(-11)}{x+11}$  and then simplify the

result.

a. 
$$\frac{2\sqrt{x+15} - x - 15}{2(x+11)(x+15)}$$

b. 
$$\frac{2\sqrt{x+15} + x-15}{2(x-11)(x+15)}$$

c. 
$$\frac{2\sqrt{x+15} + x - 15}{2(x+11)(x+15)}$$

d. 
$$\frac{2\sqrt{x+15} - x - 15}{2(x-11)(x+15)}$$

- e. undefined
- Find the domain and range of the function  $f(x) = x^2 6$ . 6.
- a. domain: [-6, ∞)
  - range: [-6, ∞)
- b. domain: [−6, ∞)
  - range: (−6, ∞)
- c. domain: (-∞, ∞)
  - range: (−6, ∞)
- d. domain: (-∞, ∞)
  - range: [6, ∞)
- e. domain: (-∞, ∞)
  - range: [−6, ∞)
- Find the domain and range of the function  $g(t) = \sqrt{t-10}$ . 7.
- a. domain: [10, ∞)
  - range: (0, ∞)
- b. domain: (10, ∞) range: [0, ∞)
- c. domain: [10, ∞)
- range: (−∞, ∞) d. domain: [0, ∞)
  - range: [10, ∞)
- e. none of the above

- 8. Find the domain and range of the function  $h(x) = \frac{11}{x+6}$ .
- a. domain:  $(-\infty, -6) \cup (-6, \infty)$ 
  - range: (-∞, ∞)
- b. domain:  $(-\infty, -6) \cup (-6, \infty)$ 
  - range:  $(-\infty, 0) \cup (0, \infty)$
- c. domain:  $(-\infty, -6] \cup [-6, \infty)$ 
  - range:  $(-\infty, 0) \cup (0, \infty)$
- d. domain: (-∞, 6)
  - range: (0, ∞)
- e. domain: (-6, ∞)
  - range: (0, ∞)
- \_\_\_\_ 9. Evaluate the function  $f(x) = \begin{cases} 2x + 1, & x < 0 \\ 2x + 2, & x \ge 0 \end{cases}$  at f(5).
- a. f(5) = 6
- b. f(5) = 5
- c. f(5) = 13
- d. f(5) = 11
- e. f(5) = 12
- \_\_\_\_\_ 10. Determine the domain and range of the function  $f(x) = \begin{cases} 3x + 2, & x < 0 \\ 3x + 6, & x \ge 0 \end{cases}$ .
- a. domain: (-∞, 2)
  - range:  $(-\infty, 2) \cap [6, \infty]$
- b. domain: (-∞, ∞)
  - range:  $(-\infty, 2) \cup [6, \infty)$
- c. domain: (-∞, ∞)
  - range:  $(-\infty, 2) \cup (\infty, 6]$
- d. domain: (-∞, ∞)
  - range:  $(\infty, 2) \cup (6, -\infty)$
- e. domain: (-∞, 3)
- range:  $(-\infty, 2) \cap [6, \infty)$
- \_\_\_\_ 11. Determine whether y is a function of x.

$$y - 5x^2 = 6$$

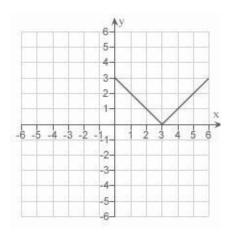
- a. no
- b. yes

12. Determine whether y is a function of x.

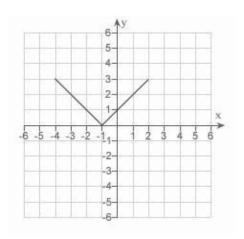
$$xy - x^2 = 3y + x$$

- a. no
- b. yes

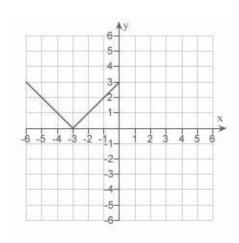
Use the graph of y = f(x) given below to find the graph of the function y = f(x + 5). 13.



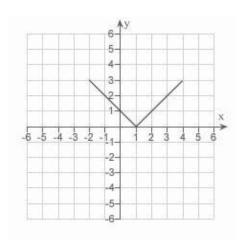
a.



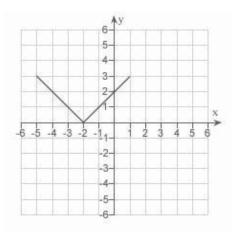
d.



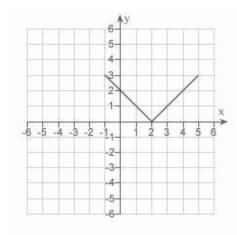
b.



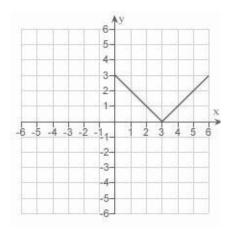
e.



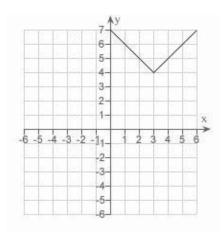
c.



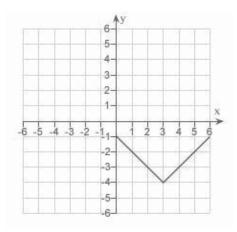
14. Use the graph of y = f(x) given below to find the graph of the function y = f(x) + 4.



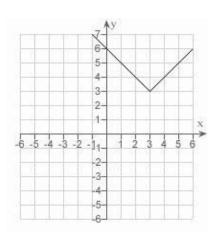
a.



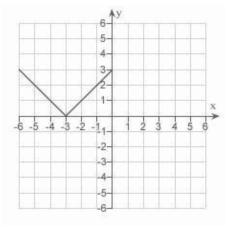
d.

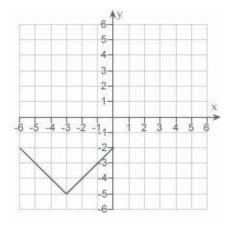


b.



e.





- d. -1e.  $\frac{\pi}{2}\cos(2)$

16. Determine whether the function is even, odd, or neither.

$$f(x) = x^2(3-x)^2$$

- a. odd
- even
- c. neither

17. Determine whether the function is even, odd, or neither.

$$f(x) = x \sin 2x$$

- a. even
- odd
- c. neither

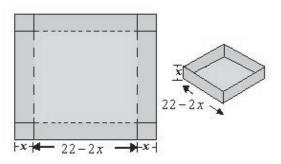
Find the coordinates of a second point on the graph of a function f if the given point  $\left(-\frac{6}{5}, 8\right)$  is on the graph and the function is even.

- $\left(\frac{6}{5}, -8\right)$

- Find the coordinates of a second point on the graph of a function f if the given point  $\left(-\frac{9}{8}, 5\right)$  is on the graph and the function is odd.
- b.  $\left(\frac{9}{8}, -5\right)$ c.  $\left(-5, \frac{9}{8}\right)$
- d.  $\left(-\frac{9}{8}, -5\right)$
- The horsepower H required to overcome wind drag on a certain automobile is approximated by  $H(x) = 0.002x^2 + 0.005x - 0.027$ ,  $10 \le x \le 100$  where x is the speed of the car in miles per hour. Find  $H\left(\frac{x}{1.1}\right)$ . Round the numerical values in your answer to five decimal places.
- $H\left(\frac{x}{1.1}\right) = 0.00150x^2 + 0.00455x 0.02700$   $H\left(\frac{x}{1.1}\right) = 0.00150x^2 + 0.00165x 0.00455$

- c.  $H\left(\frac{x}{1.1}\right) = 0.00165x^2 + 0.00150x 0.02700$ d.  $H\left(\frac{x}{1.1}\right) = 0.00165x^2 + 0.00455x 0.02700$
- e.  $H\left(\frac{x}{1.1}\right) = 0.00455x^2 + 0.00165x 0.02700$

\_\_\_\_ 21. An open box of maximum volume is to be made from a square piece of material 22 centimeters on a side by cutting equal squares from the corners and turning up the sides (see figure). Write the volume V as a function of x, the length of the corner squares.



a. 
$$V = x(22 - 2x)^2$$

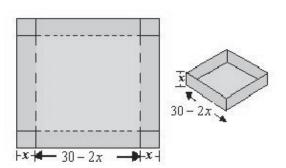
b. 
$$V = x + (22 - x)^2$$

c. 
$$V = x^2 + (22 - 2x)$$

d. 
$$V = x^2(22 - 2x)$$

e. 
$$V = x(22 - 2x)$$

22. An open box of maximum volume is to be made from a square piece of material 30 centimeters on a side by cutting equal squares from the corners and turning up the sides(see figure). What is the domain of the function  $V = x(30 - 2x)^2$ .



- a. domain:  $0 < x < \infty$
- b. domain: 30
- c. domain: 0 < x < 15
- d. domain: 0 < x < 30
- e. domain: 15

## P.3 Functions and Their Graphs **Answer Section**

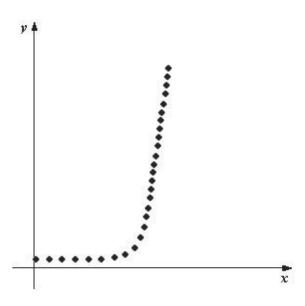
1.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:				1	DIE.	Г	MSC:	Skill		
2.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Evaluate a fur				DIE	P.	MSC:	Skill		
3.	ANS:	C	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Evaluate a fur						MSC:	Skill		
4.	ANS:	В	PTS:	1	DIF:	Med	REF:	Section 0.3		
OBJ:	Simplify a dif		-				MSC:	Skill		
5.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.3		
OBJ:	Simplify a difference quotient MSC: Skill									
6.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify the do	omain	and range of a	functio	n		MSC:	Skill		
7.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify the do	omain	and range of a	function	n		MSC:	Skill		
8.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify the do	omain	and range of a	function	n	•	MSC:	Skill		
9.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Evaluate a pie	cewise	function			,	MSC:	Skill		
10.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify the do	omain	and range of a	function	n	,	MSC:	Skill		
11.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify equat				211.	2007	MSC:	Skill		
12.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify equat			_	DII.	Lusy	MSC:	Skill		
13.	ANS:	Е	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Graph transfor			_	DII.	Lusy	MSC:	Skill		
14.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.3		
OBJ:			ns of functions	-	DII.	Wica	MSC:	Skill		
15.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Evaluate com			1	DIF.	Lasy	MSC:	Skill		
16.	ANS:	C C	PTS:	1	DIF:	Form	REF:	Section 0.3		
OBJ:						Easy	MSC:	Skill		
	Identify the ty	_	•			Г				
17.	ANS:	A	PTS:	1	DIF:	Easy	REF:	Section 0.3		
	Identify the ty					P.	MSC:	Skill		
18.	ANS:	Е	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify points					_	MSC:	Skill		
19.	ANS:	В	PTS:	1	DIF:	Easy	REF:	Section 0.3		
OBJ:	Identify points						MSC:	Skill		
20.	ANS:	D	PTS:	1	DIF:	Med	REF:	Section 0.3		
OBJ:	Apply compos						MSC:	Application		
21.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.3		
OBJ:	Create function						MSC:	Application		
22.	ANS:	C	PTS:	1	DIF:	Med	REF:	Section 0.3		
OBJ:	Identify doma	ins in	applications				MSC:	Application		

## P.4 Fitting Models to Data

## **Multiple Choice**

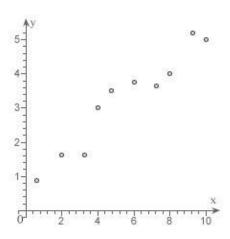
Identify the choice that best completes the statement or answers the question.

Determine which type of function would be most appropriate to fit the given data. 1.



- exponential
- linear b.
- quadratic c.
- no relationship
- trigonometric

2. Which function below would be most appropriate model for the given data?



- no apparent relationship between x and y
- trigonometric
- quadratic c.
- linear d.
- 3. Hooke's Law states that the force F required to compress or stretch a spring (within its elastic limits) is proportional to the distance d that the spring is compressed or stretched from its original length. That is, F = kd where k is a measure of the stiffness of the spring and is called the spring constant. The table shows the elongation d in centimeters of a spring when a force of Fnewtons is applied. Use the regression capabilities of a graphing utility to find a linear model for the data. Round the numerical values in your answer to three decimal places.

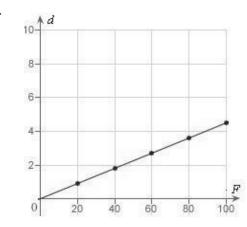
F	20	40	60	80	100
d	1.9	3.8	5.7	7.6	9.5

- a. d = 0.675F
- b. d = 0.118F
- d = 0.112F
- d = 0.095F
- e. d = 0.905F

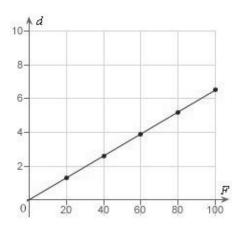
4. Hooke's Law states that the force F required to compress or stretch a spring (within its elastic limits) is proportional to the distance d that the spring is compressed or stretched from its original length. That is, F = kd where k is a measure of the stiffness of the spring and is called the spring constant. The table shows the elongation d in centimeters of a spring when a force of F newtons is applied. Use a graphing utility to plot the data and graph the linear model.

F	20	40	60	80	100
d	1.3	2.6	3.9	5.2	6.5

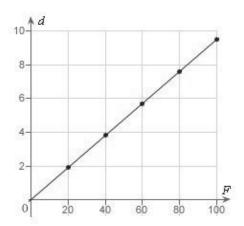
a.



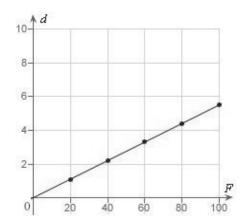
d.



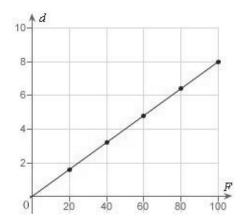
b.



e.







5. Hooke's Law states that the force F required to compress or stretch a spring (within its elastic limits) is proportional to the distance d that the spring is compressed or stretched from its original length. That is, F = kd where k is a measure of the stiffness of the spring and is called the spring constant. The table shows the elongation d in centimeters of a spring when a force of Fnewtons is applied. Use the model d = 0.085 F to estimate the elongation of the spring when a force of 55 newtons is applied. Round your answer to two decimal places.

F	20	40	60	80	100
d	1.7	3.4	5.1	6.8	8.5

- a. 8.08 cm
- b. 6.38 cm
- c. 4.68 cm
- d. 2.98 cm
- e. 9.78 cm

In an experiment, students measured the speed s (in meters per second) of a falling object t seconds after it was released. The results are shown in the table below. Use the regression capabilities of a graphing utility to find a linear model for the data. Round all numerical values in your answer to one decimal place.

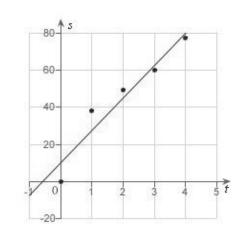
t	0	1	2	3	4
S	0	13.0	21.4	31.2	41.4

- a. s = 10.1t + 1.2
- b. s = 3.0t 1.2
- c. s = 1.2t + 10.1
- d. s = 10.1t + 3.0
- e. s = 1.2t 3.0

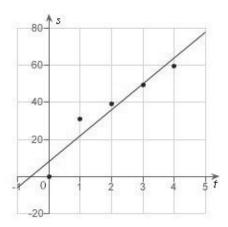
 $\overline{\phantom{a}}$  7. In an experiment, students measured the speed s (in meters per second) of a falling object t seconds after it was released. The results are shown in the table below. Use the regression capabilities of a graphing utility to find a linear model for the data. Round all numerical values in your answer to one decimal place.

t	0	1	2	3	4
S	0	40	48.4	58.2	68.4

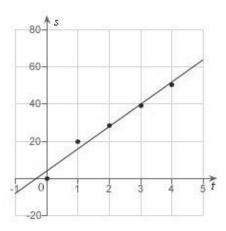
a.



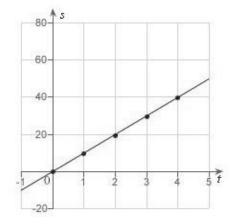
d.



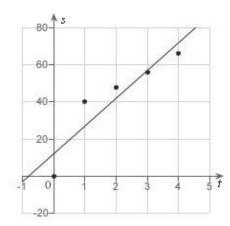
b.



e.



c.



8. In an experiment, students measured the speed s (in meters per second) of a falling object t seconds after it was released. The results are shown in the table below. Use the model s = 11.9t + 4.8 to estimate the speed of the object after 1.5 seconds. Round your answer to two decimal places.

t	0	1	2	3	4
S	0	22.0	30.4	40.2	50.4

- a. 21.05 meters/second
- b. 20.95 meters/second
- c. 24.25 meters/second
- d. 23.55 meters/second
- e. 22.65 meters/second

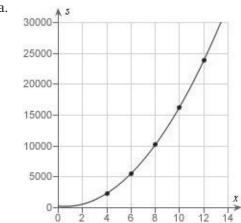
Students in a lab measured the breaking strength S (in pounds) of wood 2 inches thick, x inches high, and 12 inches long. The results are shown in the table below. Use the regression capabilities of a graphing utility to fit a quadratic model to the data. Round the numerical values in your answer to two decimal places, where applicable.

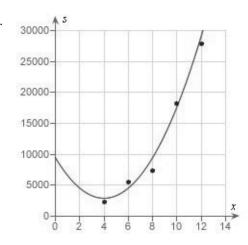
х	4	б	8	10	12
ន	2422	5512	10, 362	16, 302	23, 912

- a.  $S = 170.89x^2 209.79x + 324$
- b.  $S = 180.89x^2 205.79x + 324$
- c.  $S = 190.89x^2 + 201.79x + 331$
- d.  $S = 170.89x^2 209.79x + 327$
- e.  $S = 180.89x^2 + 203.79x 331$

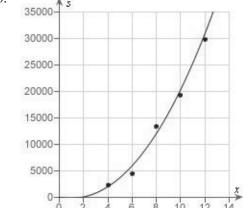
х	4	б	8	10	12
ន	2370	4460	13,310	19, 250	29,860

a.

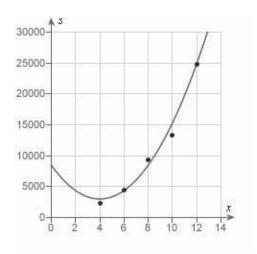


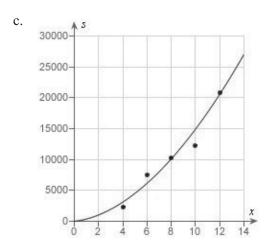


b.



e.





11. Students in a lab measured the breaking strength S (in pounds) of wood 2 inches thick, x inches high, and 12 inches long. The results are shown in the table below. Use the model  $S = 180.89x^2 - 205.79x + 284$  to approximate the breaking strength when x = 2. Round your answer to two decimal places.

х	4	б	8	10	12
ಭ	2382	5472	10,322	16, 262	23, 872

- a. 595.98 pounds
- b. 390.19 pounds
- c. 957.76 pounds
- d. 801.77 pounds
- e. 751.97 pounds

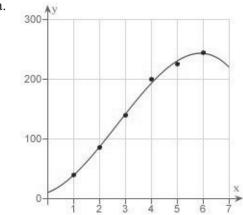
12. A V8 car engine is coupled to a dynamometer and the horsepower *y* is measured at different engine speeds *x* (in thousands of revolutions per minute). The results are shown in the table below. Use the regression capabilities of a graphing utility to find a cubic model for the data. Round the numerical values in your answer to three decimal places, where applicable.

х	1	2	3	4	5	б
У	64	109	164	224	249	269

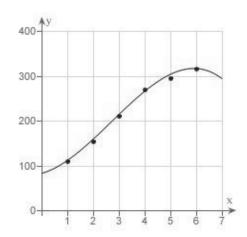
- a.  $y = -1.608x^3 14.583x^2 + 13.389x 37$
- b.  $y = -1.706x^3 14.583x^2 16.389x + 34$
- c.  $y = 1.806x^3 + 11.583x^2 + 16.389x 41$
- d.  $y = -1.806x^3 + 14.583x^2 + 16.389x + 34$
- e.  $y = 1.608x^3 + 11.583x^2 19.389x + 41$

х	1	2	3	4	5	6
у	110	155	210	270	295	315

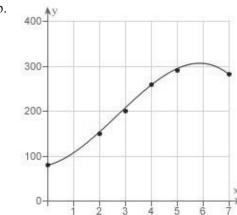
a



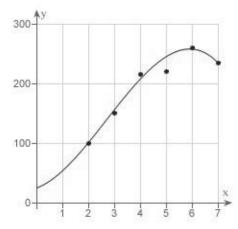
d.



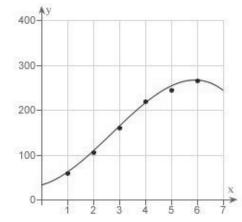
b.



e.



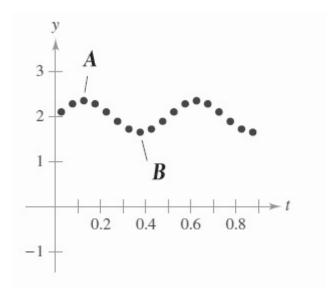
c.



A V8 car engine is coupled to a dynamometer and the horsepower y is measured at different engine speeds x (in thousands of revolutions per minute). The results are shown in the table below. Use the model  $y = -1.806x^3 + 14.58x^2 + 16.4x + 30$  to approximate the horsepower when the engine is running at 5500 revolutions per minute. Round your answer to two decimal places.

х	1	2	3	4	5	б
у	60	105	160	220	245	265

- 260.77 hp
- b. 262.73 hp
- c. 262.36 hp
- d. 261.38 hp
- 261.91 hp
- 15. The motion of an oscillating weight suspended by a spring was measured by a motion detector. The data collected and the approximate maximum (positive and negative) displacements from equilibrium are shown in the figure. The displacement is measured in centimeters, and the time is measured in seconds. Take A(0.133,2.49) and B(0.343,1.78). Approximate the amplitude and period of the oscillations.



- Amplitude = 0.335. Period = 4.3.
- b. Amplitude = 0.71. Period = 2.1.
- Amplitude = 0.355. Period = 4.2.
- Amplitude = 4.2. Period = 0.355.
- Amplitude = 2.1. Period = 0.71.

## P.4 Fitting Models to Data **Answer Section**

## **MULTIPLE CHOICE**

1.	ANS:	A	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	Identify the most appropriate function for a scatter plot MSC: Skill							
2.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	-		propriate function	on for a	_		MSC:	Skill
3.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	Write a linear model for data using the regression capabilities of a graphing utility							
MSC:	Application							
4.	ANS:	D	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	Plot data points and the graph of a linear model MSC: Application							
5.	ANS:	C	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	Evaluate linea	ar mode	els in application	ns			MSC:	Application
6.	ANS:	A	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	Write a linear model for data using the regression capabilities of a graphing utility							
	Application							
7.	ANS:	C	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	Plot data points and the graph of a linear model MSC: Application							
8.	ANS:	E	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:		ır mode	els in application	ns			MSC:	Application
9.	ANS:	В	PTS:	1	DIF:	Med	REF:	Section 0.4
OBJ:	Write a quadratic model for data using the regression capabilities of a graphing utility							
	Application							
10.	ANS:	В	PTS:	1	DIF:	Med	REF:	Section 0.4
OBJ:	Plot data points and the graph of a quadratic model MSC: Application							
11.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.4
OBJ:	Evaluate quadratic models in applications MSC: Application							
12.	ANS:	D	PTS:	1	DIF:	Med	REF:	Section 0.4
OBJ:	Evaluate cubic models in applications MSC: Application							
13.	ANS:	D	PTS:	1	DIF:	Med	REF:	Section 0.4
OBJ:	Plot data points and the graph of a cubic model MSC: Application							
14.	ANS:	A	PTS:	1	DIF:	Med	REF:	Section 0.4
OBJ:	Write a cubic model for data using the regression capabilities of a graphing utility							
MSC:	SC: Application							
15.	ANS:	C	PTS:	1	DIF:	Easy	REF:	Section 0.4
OBJ:	Fit a trigonom	netric m	odel to a real-li	ife data	set.		MSC:	Application

## 1.1 A Preview of Calculus

## **Multiple Choice**

Identify the choice that best completes the statement or answers the question.

Decide whether the following problem can be solved using precalculus, or whether calculus is required. If the problem can be solved using precalculus, solve it. If the problem seems to require calculus, use a graphical or numerical approach to estimate the solution.

Find the distance traveled in 16 seconds by an object traveling at a constant velocity of 20 feet per second.

- calculus, 320 ft
- b. calculus, 340 ft
- c. precalculus, 320 ft
- d. calculus, 640 ft
- e. precalculus, 640 ft

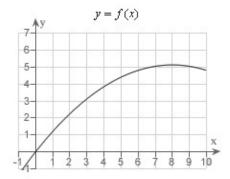
Decide whether the following problem can be solved using precalculus, or whether calculus is required. If the problem can be solved using precalculus, solve it. If the problem seems to require calculus, use a graphical or numerical approach to estimate the solution.

Find the distance traveled in 20 seconds by an object moving with a velocity of  $v(t) = 8 + 6 \cos t$  feet per second.

- calculus, 162.4485 ft
- b. precalculus, 163.7985 ft
- c. calculus, 165.4777 ft
- d. precalculus, 165.4777 ft
- e. precalculus, 162.4485 ft

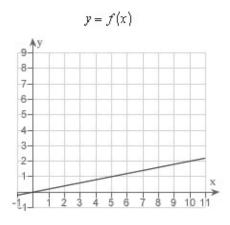
3. Decide whether the following problem can be solved using precalculus, or whether calculus is required. If the problem can be solved using precalculus, solve it. If the problem seems to require calculus, use a graphical or numerical approach to estimate the solution.

A cyclist is riding on a path whose elevation is modeled by the function  $f(x) = 0.08 \left( 16x - x^2 \right)$  where x and f(x) are measured in miles. Find the rate of change of elevation when x = 4.



- a. precalculus, 0.08
- b. calculus, 0.2
- c. calculus, 0.64
- d. calculus, 0.08
- e. precalculus, 0.2
- 4. Decide whether the following problem can be solved using precalculus, or whether calculus is required. If the problem can be solved using precalculus, solve it. If the problem seems to require calculus, use a graphical or numerical approach to estimate the solution.

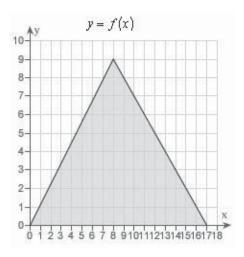
A cyclist is riding on a path whose elevation is modeled by the function f(x) = 0.2x where x and f(x) are measured in miles. Find the rate of change of elevation when x = 5.



- a. calculus, 2
- b. precalculus, 0.2
- c. calculus, 0.2
- d. precalculus, 2
- e. precalculus, 0.45

5. Decide whether the following problem can be solved using precalculus, or whether calculus is required. If the problem can be solved using precalculus, solve it. If the problem seems to require calculus, use a graphical or numerical approach to estimate the solution.

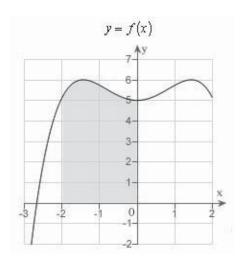
Find the area of the shaded region bounded by the triangle with vertices (0,0), (8,9), (17,0).



- precalculus, 153
- calculus, 229.5
- precalculus, 76.5
- precalculus, 229.5
- calculus, 153

Decide whether the following problem can be solved using precalculus, or whether calculus is required. If the problem can be solved using precalculus, solve it. If the problem seems to require calculus, use a graphical or numerical approach to estimate the solution.

Find the area of the shaded region.



- calculus, 11
- precalculus, 11
- precalculus, 13

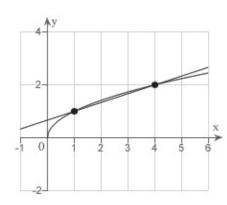
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d. calculus, 16

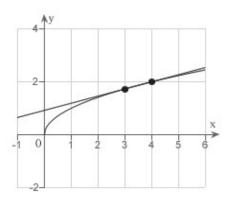
e. precalculus, 16

7. Consider the function  $f(x) = \sqrt{x}$  and the point P(4,2) on the graph of f. Graph f and the secant line passing through P(4,2) and Q(x,f(x)) for x=3.

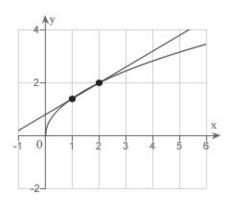
a.



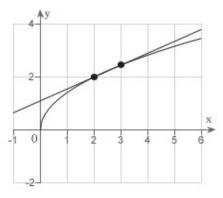
d.



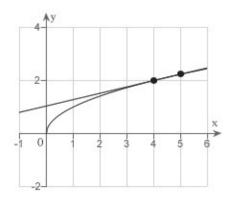
b.



e.



c.



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