## Chapter 2

## Organizing and Summarizing Data

## Section 2.1

1. Raw data are the data as originally collected, before they have been organized or coded.
2. Number (or count); proportion (or percent)
3. The relative frequencies should add to 1 , although rounding may cause the answers to vary slightly.
4. A bar graph is used to illustrate qualitative data. It is a chart in which rectangles are used to illustrate the frequency or relative frequency with which a category appears. A Pareto chart is a bar chart with bars drawn in order of decreasing frequency or relative frequency.
5. (a) The largest segment in the pie chart is for "Washing your hands" so the most commonly used approach to beat the flu bug is washing your hands. $61 \%$ of respondents selected this as their primary method for beating the flu.
(b) The smallest segment in the pie chart is for "Drinking Orange Juice" so the least used method is drinking orange juice. $2 \%$ of respondents selected this as their primary method for beating the flu.
(c) $25 \%$ of respondents felt that flu shots were the best way to beat the flu.
6. (a) $\frac{128,000}{1,350,000}=\frac{64}{675} \approx 0.0948$;
approximately $9.48 \%$ of cosmetic surgeries in 2009 were for tummy tucks.
(b) $\frac{138,000}{1,350,000}=\frac{23}{225} \approx 0.102$; approximately $10.2 \%$ of cosmetic surgeries in 2009 were for nose reshaping.
(c) The graph accounts for $312,000+284,000$ $+150,000+138,000+128,000=$ $1,012,000$ surgeries. Thus, $1,350,000-$ $1,012,000=338,000$ surgeries are not accounted for in the graph.
7. (a) The largest bar corresponds to China, so China had the most internet users in 2010.
(b) The bar for the United Kingdom appears to reach the line for 50 . Thus, we estimate that there were 50 million internet users in the United Kingdom in 2007.
(c) The bar for China appears to reach 420 on the vertical axis. The bar for Germany appears to reach 70 . Since, $420-70=350$, we estimate that there were about 350 million more internet users in China than in Germany during 2007.
(d) This graph should use relative frequencies, rather than frequencies.
8. (a) $29,830,000$ whites were living in poverty.
(b) $12350 /(29830+9944+12350+1746)=$ $0.229=22.9 \%$
In 2009, about $22.9 \%$ of the impoverished in the United States were Hispanic.
(c) This graph should use relative frequencies, rather than frequencies. The graph does not account for the different population size of each ethnic group. Without knowing the population sizes, we cannot determine whether a group is disproportionally impoverished.
9. (a) $69 \%$ of the respondents believe divorce is morally acceptable.
(b) $23 \%$ believe divorce is morally wrong. So, 240 million * $0.23=55.2$ million adult Americans believe divorce is morally wrong.
(c) This statement is inferential, since it is a generalization based on the observed data.
10. (a) $5 \%$ of identity theft was loan fraud.
(b) $26 \%$ of the identity fraud cases in 2008 involved credit card fraud. So, 10 million $* 0.26=2.6$ million cases of credit card fraud occurred in 2008.
11. (a) The proportion of 18-34 year old respondents who are more likely to buy when made in America is 0.42 . For 34-44 year olds, the proportion is 0.61 .
(b) The 55+ age group has the greatest proportion of respondents who are more likely to buy when made in America.
(c) The 18-34 age group has a majority of respondents who are less likely to buy when made in America.
(d) As age increases, so does the likelihood that a respondent will be more likely to buy a product that is made in America.
12. (a) The proportion of males who would like to be richer is 0.46 . The proportion of females who would like to be richer is 0.41 .
(b) The attribute that females desire more than males is to be thinner.
(c) The attribute that males prefer over females two-to-one is to be younger.
(d) Equal proportions of males and females desire to be smarter.
13. (a) Total students surveyed $=125+324+$ $552+1257+2518=4776$
Relative frequency of "Never" $=125 / 4776 \approx 0.0262$ and so on.

| Response | Relative <br> Frequency |
| :--- | :--- |
| Never | 0.0262 |
| Rarely | 0.0678 |
| Sometimes | 0.1156 |
| Most of the time | 0.2632 |
| Always | 0.5272 |

(b) $52.72 \%$
(c) $0.0262+0.0678=0.0940$ or $9.40 \%$
(d)

(e)

(f)

(g) The statement is inferential since it is inferring something about the entire population based on the results of a sample survey.
14. (a) Total students surveyed $=249+118+$ $249+345+716+3093=4770$
Relative frequency of "I do not drive" $=\frac{249}{4770} \approx 0.0522$ and so on.

| Response | Relative <br> Frequency |
| :--- | :--- |
| I do not drive | 0.0522 |
| Never | 0.0247 |
| Rarely | 0.0522 |
| Sometimes | 0.0723 |
| Most of the time | 0.1501 |
| Always | 0.6484 |

(b) $64.84 \%$
(c) $0.0247+0.0522=0.0769$ or $7.7 \%$
(d)

(e)

(f)
"How Often Do You Wear a Seat Belt When Driving a Car?"

(g) Total students $=118+249+345+716+$ $3093=4521$
Relative frequency of "Never"
$=\frac{118}{4521} \approx 0.0261$ and so on.

| Response | Relative Frequency |
| :---: | :---: |
| Never | 0.0261 |
| Rarely | 0.0551 |
| Sometimes | 0.0763 |
| Most of the time | 0.1584 |
| Always | 0.6841 |

The relative frequencies of all categories are very similar except that students are more likely to wear their seatbelt 'Always' when driving than when riding in a car driven by another.
(h) The statement is descriptive because it is describing the particular sample.
15. (a) Total adults surveyed $=377+192+132$ $+81+243=1025$
Relative frequency of "More than 1 hour a day" $=377 / 1025 \approx 0.3678$ and so on.

| Response | Relative <br> Frequency |
| :--- | :--- |
| More than 1 hr a day | 0.3678 |
| Up to 1 hr a day | 0.1873 |
| A few times a week | 0.1288 |
| A few times a month or less | 0.0790 |
| Never | 0.2371 |

(b) 0.2371 (about $24 \%$ )
(c)

(d)

(e)

(f) The statement provides an estimate, but no level of confidence is given.
16. (a) Total adults surveyed $=103+204+130$
$+79+5=521$
Relative frequency of "Several times a week" $=\frac{103}{521} \approx 0.197$ and so on.

Relative
Response Frequency

| Several times a week | 0.197 |
| :--- | :--- |
| Once or twice a week | 0.392 |
| A few times a month | 0.250 |
| Vary rarely | 0.152 |
| Never | 0.010 |

(b) The proportion surveyed who dine out once or twice a week is $204 /(103+204+130+79+5)=0.396$
(c)

(d)

17. (a) Total adults $=1936$

Relative frequency for "none" is: $173 / 1936=0.09$, and so on.

| Number of Texts | Rel. Freq. (Adults) |
| :--- | :---: |
| None | 0.09 |
| 1 to 10 | 0.51 |
| 11 to 20 | 0.13 |
| 21 to 50 | 0.13 |
| 51 to 100 | 0.07 |
| $101+$ | 0.08 |

(b) Total teens $=627$

Relative frequency for "none" is:
$13 / 627=0.02$, and so on.

| Number of Texts | Rel. Freq. (Teens) |
| :--- | :---: |
| None | 0.02 |
| 1 to 10 | 0.22 |
| 11 to 20 | 0.11 |
| 21 to 50 | 0.18 |
| 51 to 100 | 0.18 |
| $101+$ | 0.29 |

(c)

(d) Answers will vary. Adults are much more likely to do fewer texts per day, while teens are much more likely to do more texting.
18. (a), (b)

Total males $=94.5$ million
Relative frequency for "Not HS graduate" is $13.3 / 94.5=0.141$ and so on.

Total females $=102.0$ million
Relative frequency for "Not HS graduate" is $13 / 100.5=0.130$ and so on.

| Educational Attainment | Males | Females |
| :--- | :---: | :---: |
| Not a HS graduate | 0.141 | 0.127 |
| High school graduate | 0.312 | 0.311 |
| Some college, no degree | 0.167 | 0.176 |
| Associate's degree | 0.079 | 0.096 |
| Bachelor's degree | 0.190 | 0.192 |
| Advanced degree | 0.110 | 0.097 |

(c)

(d) Answers will vary. It appears that females are slightly more likely to start, but not finish college. Males appear to be slightly more likely to attain an advanced degree.
19. (a) Total males $=99$; Relative frequency for "Professional Athlete" is $40 / 99=0.404$, and so on.

Total number of females $=100$; Relative frequency for "Professional Athlete" is $18 / 100=0.18$, and so on.

| Dream Job | Men | Women |
| :--- | :---: | :---: |
| Professional Athlete | 0.404 | 0.180 |
| Actor/Actress | 0.263 | 0.370 |
| President of the U.S. | 0.131 | 0.130 |
| Rock Star | 0.131 | 0.130 |
| Not Sure | 0.071 | 0.190 |

(b)

Dream Job

(c) Answers will vary. Males are much more likely to want to be a professional athlete. Women are more likely to aspire to a career in acting than men. Men's desire to become athletes may be influenced by the prominence of male sporting figures in popular culture. Women may aspire to careers in acting due to the perceived glamour of famous female actresses.
20. (a) Relative frequency for "White" luxury cars $=\frac{25}{100}=0.25$ and so on.
Relative frequency for "Silver" sport cars $=\frac{10}{100}=0.10$ and so on.

Relative Frequencies

| Color | Luxury Cars | Sport Cars |
| :--- | :--- | :--- |
| White | 0.25 | 0.10 |
| Black | 0.22 | 0.15 |
| Silver | 0.16 | 0.18 |
| Bray | 0.12 | 0.15 |
| Blue | 0.07 | 0.13 |
| Red | 0.07 | 0.15 |
| Gold | 0.06 | 0.05 |
| Green | 0.03 | 0.02 |
| Brown | 0.02 | 0.07 |

(b)

(c) Answers will vary. White is the most popular color for luxury cars, while silver is the most popular for sports cars. People who drive luxury cars may enjoy the clean look of a white vehicle. People who drive sports cars may prefer the flashier look of silver.
21. (a), (b)

Total number of Winter Olympics $=22$; relative frequency for Canada is $8 / 22=0.364$.

| Winner | Freq. | Rel. Freq. |
| :--- | :---: | :---: |
| Canada | 8 | 0.364 |
| Czech Republic | 1 | 0.045 |
| Great Britain | 1 | 0.045 |
| Soviet Union | 7 | 0.318 |
| Sweden | 2 | 0.091 |
| U.S.A. | 2 | 0.091 |
| Unified Team | 1 | 0.045 |

(c)

Olympic Hockey Gold Medals

(d)

Olympic Hockey Gold Medals

(e)

Olympic Hockey Gold Medals

22. (a), (b)

Total number of responses $=25$; relative frequency for "edit details" is $7 / 25=0.28$.

| Response | Freq. | Rel. Freq |
| :--- | :---: | :---: |
| Edit details | 7 | 0.28 |
| Say nothing | 4 | 0.16 |
| Tell all | 14 | 0.56 |

(c)

Bachelor Party Details to Fiancé

(d)

(e)

Bachelor Party Details to Financé

23. (a), (b)

Total number of responses $=40$; relative frequency for "Sunday" is $3 / 40=0.075$.

| Response | Freq. | Rel. Freq. |
| :--- | :---: | :---: |
| Sunday | 3 | 0.075 |
| Monday | 2 | 0.05 |
| Tuesday | 5 | 0.125 |
| Wednesday | 6 | 0.15 |
| Thursday | 2 | 0.05 |
| Friday | 14 | 0.35 |
| Saturday | 8 | 0.2 |

(c) Answers will vary. If you own a restaurant, you will probably want to advertize on the days when people will be most likely to order takeout: Friday. You might consider avoiding placing an ad on Monday and Thursday, since the readers are least likely to choose to order takeout on these days.
(d)

Favorite Day to Eat Out

(e)

Favorite Day to Eat Out

(f)

Favorite Day to Eat Out

24. (a), (b)

Total number of patients $=50$
Relative frequency for "Type A"
$=\frac{18}{50}=0.36$ and so on.

| Blood Type | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| A | 18 | 0.36 |
| AB | 4 | 0.08 |
| B | 6 | 0.12 |
| O | 22 | 0.44 |

(c) Type O is the most common.
(d) Type AB is the least common.
(e) We estimate that $44 \%$ of the population has type O blood. This is considered inferential statistics because a conclusion about the population is being drawn based on sample data.
(f) Answers will vary; in 2008 the Red Cross reported that $45 \%$ of the population had type O blood (either + or - ). Results will differ because of sampling variability.
(g)

(h)

(i)

25. (a), (b)

Total number of students $=30$
Relative frequency for "Chinese"
$=\frac{3}{30}=0.100$ and so on.

| Language | Freq. | Rel. Frequency |
| :---: | :---: | :---: |
| Chinese | 3 | 0.100 |
| French | 3 | 0.100 |
| German | 3 | 0.100 |
| Italian | 2 | 0.067 |
| Japanese | 2 | 0.067 |
| Latin | 2 | 0.067 |
| Russian | 1 | 0.033 |
| Spanish | 14 | 0.467 |

(c)

Foreign Languages Studied by College Students

(d)

(e) Foreign Languages
Studied by College Students

26. (a)

| State | AR | CA | CT | GA | HI | IL |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Freq. | 1 | 1 | 1 | 1 | 1 | 1 |
| State | IA | KY | MA | MO | NE |  |
| Freq. | 1 | 1 | 4 | 1 | 1 |  |
| State | NH | NJ | NY | NC | OH |  |
| Freq. | 1 | 2 | 4 | 2 | 7 |  |
| State | PA | SC | TX | VT | VA |  |
| Freq. | 1 | 1 | 2 | 2 | 8 |  |

The U.S. Presidents' Birthplaces

(b) More presidents were born in Virginia than in any other state.
(c) Answers will vary. The data do not take the year of statehood into account. For example, Virginia has been a state for roughly 62 years more than California. The population of the U.S. was more concentrated in the east in the early years so it was more likely that the president would be from that part of the country.
27. (a) It would make sense to draw a pie chart for land area since the 7 continents contain all the land area on Earth. Total land area is $11,608,000+5,100,000$ $+\ldots+9,449,000+6,879,000=$ $57,217,000$ square miles The relative frequency (percentage) for Africa is $\frac{11,608,000}{57,217,000}=0.2029$.

| Continent | Land Area <br> $\left(\mathrm{mi}^{2}\right)$ | Rel. Freq. |
| :---: | :---: | :---: |
| Africa | $11,608,000$ | 0.2029 |
| Antarctica | $5,100,000$ | 0.0891 |
| Asia | $17,212,000$ | 0.3008 |
| Australia | $3,132,000$ | 0.0547 |
| Europe | $3,837,000$ | 0.0671 |
| North America | $9,449,000$ | 0.1651 |
| South America | $6,879,000$ | 0.1202 |


(b) It would not make sense to draw a pie chart for the highest elevation because there is no whole to which to compare the parts.
28. Answers will vary.
29. Answers will vary.
30. (a) The researcher wants to determine if online homework improves student learning over traditional pencil-and-paper homework.
(b) This study is an experiment because the researcher is actively imposing treatments (the homework style) on subjects.
(c) Answers will vary. Some examples are same teacher, same semester, and same course.
(d) Assigning different homework methods to entire classes could confound the results because there may be differences between the classes. The instructor may give more instruction to one class than the other. The instructor is not blinded, so he or she may treat one group differently from the other.
(e) Number of students: quantitative, discrete Average age: quantitative, continuous Average exam score: quantitative, continuous
Type of homework: qualitative College experience: qualitative
(f) Letter grade is a qualitative variable at the ordinal level of measurement. Answers will vary. It is possible that ordering the data from A to F is better because it might give more "weight" to the higher grade and the researcher wants to show that a higher percent of students passed using the online homework.
(g) The graph being displayed is a side-byside relative frequency bar graph.
(h) Yes; the 'whole' is the set of students who received a grade for the course for each homework method.
(i) The table shows that the two groups with no prior college experience had roughly the same average exam grade. From the bar graph, we see that the students using online homework had a lower percent for As, but had a higher percent who passed with a C or better.
31. Relative frequencies should be used when the size of two samples or populations differ.
32. Answers will vary. If the goal is to illustrate the levels of importance, then arranging the bars in a bar chart in decreasing order makes sense. Sometimes it is useful to arrange the categorical data in a bar chart in alphabetical order. A pie chart does not readily allow for arranging the data in order.
33. A bar chart is preferred when trying to compare two specific values. Pie charts are helpful for comparing parts of a whole. A pie chart cannot be drawn if the data do not include all possible values of the qualitative variable.
34. No, the percentages do not sum to $100 \%$.

## Consumer Reports ${ }^{\circledR}$ : Consumer Reports Rates Treadmills

(a) A bar chart is used to display the overall scores. Because the bars are in decreasing order, this is an example of a Pareto chart.
(b) The Precor M9.33 has the highest construction score since it was the only model receiving an excellent rating. Two models, the Tunturi J6F and the ProForm 525E received a Fair rating, making them the models with the lowest ease of use score.
(c) 1 model was rated Excellent, 7 models were rated Very Good, 1 model was rated Good, and 2 models were rated Fair. No models were rated Poor for ease of use.
(d) The following bar charts were created in Microsoft® Excel:




(e) The following scatterplot was obtained by eyeballing the value of the scores from the Overall Score Pareto chart. Although there is a great deal of scatter in the data, even within a similar price range, there appears to be a relationship between score and price. The more expensive models tested by Consumer Reports in March 2002 tended to score higher in overall performance. (One should be cautious about generalizing the conclusions to the universe of treadmills since only a small sample of treadmills have been tested here.)


## Section 2.2

1. Classes
2. Lower; upper
3. Class width
4. Skewed left means that the left tail is longer than the right tail.
5. True
6. False
7. False
8. False
9. (a) 8
(b) 2
(c) 15
(d) $11-7=4$
(e) $\frac{15}{100}=0.15$ or $15 \%$
(f) The distribution is bell shaped.
10. (a) 4 cars
(b) There were 9 weeks in which 2 cars sold.
(c) Total frequency $=4+2+9+8+12+8+$ $5+2+1+1=52$ (as required)
Percentage of time two cars are sold
$=\frac{9}{52} \cdot 100=17.3 \%$
(d) Slightly skewed to the right.
11. (a) Total frequency $=2+3+13+42+58+$ $40+31+8+2+1=200$
(b) 10 (e.g. $70-60=10$ )
(c)

| IQ Score (class) | Frequency |
| :---: | :---: |
| $60-69$ | 2 |
| $70-79$ | 3 |
| $80-89$ | 13 |
| $90-99$ | 42 |
| $100-109$ | 58 |
| $110-119$ | 40 |
| $120-129$ | 31 |
| $130-139$ | 8 |
| $140-149$ | 2 |
| $150-159$ | 1 |

(d) The class ' $100-109$ ' has the highest frequency.
(e) The class ' $150-159$ ' has the lowest frequency.
(f) $\frac{8+2+1}{200}=0.055=5.5 \%$
(g) No, there were no IQs above 159.
12. (a) 200 (e.g. $200-0=200$ )
(b) 0-199, 200-399, 400-599, 600-799, 800999, 1000-1199, 1200-1399, 1400-1599
(c) The highest frequency is in class $0-199$.
(d) The distribution is skewed right.
(e) Answers will vary. The statement is incorrect because they are comparing counts from populations of different size. To make a fair comparison, the reporter should use rates of fatalities such as the number of fatalities per 1000 residents.
13. (a) Likely skewed right. Most household incomes will be to the left (perhaps in the $\$ 50,000$ to $\$ 150,000$ range), with fewer higher incomes to the right (in the millions).
(b) Likely bell-shaped. Most scores will occur near the middle range, with scores tapering off equally in both directions.
(c) Likely skewed right. Most households will have, say, 1 to 4 occupants, with fewer households having a higher number of occupants.
(d) Likely skewed left. Most Alzheimer's patients will fall in older-aged categories, with fewer patients being younger.
14. (a) Likely skewed right. More individuals would consume fewer alcoholic drinks per week, while less individuals would consume more alcoholic drinks per week.
(b) Likely uniform. There will be approximately an equal number of students in each age category.
(c) Likely skewed left. Most hearing-aid patients will fall in older-aged categories, with fewer patients being younger.
(d) Likely bell-shaped. Most heights will occur, say, in the 66- to 70-inch range, with heights tapering off equally in both directions.
15. (a) The HOI in the first quarter of 1999 is about 70\%.
(b) The lowest value of the HOI was about $40 \%$. This occurred in 2006.
(c) The highest value of the HOI was about $75 \%$. This occurred in 2011.
(d) $\frac{40-70}{70}=\frac{-30}{70} \approx-0.43$

The HOI decreased by about $43 \%$ from the first quarter of 1999 to the third quarter of 2006.
(e) There is an increase of about $87.5 \%$.
16. (a) About 8.8 million motor vehicles were produced in the United States in 1991.
(b) About 13.0 million motor vehicles were produced in the United States in 1999.
(c) $\frac{13000-8800}{8800}=\frac{4200}{8800} \approx 0.477$ The number of vehicles produced increased by about $47.7 \%$ between 1991 and 1999.
(d) $\frac{5700-13000}{13000}=\frac{-7300}{13000} \approx-0.562$ The number of vehicles produced decreased by about $56 \%$ between 1999 and 2009.
17. (a) For 1992, the unemployment rate was about $7.5 \%$ and the inflation rate was about $3.0 \%$.
(b) For 2009, the unemployment rate was about $9.2 \%$ and the inflation rate was about $-0.4 \%$.
(c) $7.5 \%+3.0 \%=10.5 \%$

The misery index for 1992 was $10.5 \%$. $4.6 \%+3.4 \%=8.0 \%$
The misery index for 2009 was $8.8 \%$.
(d) Answers may vary. One possibility: An increase in the inflation rate seems to be followed by an increase in the unemployment rate. Likewise, a decrease in the inflation rate seems to be followed by a decrease in the unemployment rate.
18. (a) In 1996, the men's prize money was $£ 400,000$ and the ladies’ prize money was £350,000.
(b) In 2006, the men's prize money was $£ 655,000$ and the ladies’ prize money was £625,000.
(c) Answers may vary. One possibility: Until 2007, the prize money for men's singles is higher than the prize money for ladies' singles. Both prizes increase over time at similar rates.
(d) In 2007, the prize money for men's and ladies' singles was the same for the first time. The prize money for each was £700,000.
(e) From 2010 to 2011, the prize money increased from $£ 1,000,000$ to $£ 1,100,000$ for both the men and the women. This is a relative increase of $\frac{1,100,000-1,000,000}{1,000,000} \approx 0.10$
or $10 \%$.
19. (a) Total number of households $=$
$16+18+12+3+1=50$
Relative frequency of 0 children $=16 / 50$ $=0.32$, and so on.

| Number of Children Under Five | Relative <br> Frequency |
| :---: | :---: |
| 0 | 0.32 |
| 1 | 0.36 |
| 2 | 0.24 |
| 3 | 0.06 |
| 4 | 0.02 |

(b) $\frac{12}{50}=0.24$ or $24 \%$ of households have two children under the age of 5 .
(c) $\frac{18+12}{50}=\frac{30}{50}=0.6$ or $60 \%$ of households have one or two children under the age of 5.
20. (a) Total number of free throws $=$ $16+11+9+7+2+3+0+1+0+1=50$. Relative frequency of 1 throw until a miss $=16 / 50=0.32$, and so on.

| Number of Free <br> Throws Until a Miss | Relative <br> Frequency |
| :---: | :---: |
| 1 | 0.32 |
| 2 | 0.22 |
| 3 | 0.18 |
| 4 | 0.14 |
| 5 | 0.04 |
| 6 | 0.06 |
| 7 | 0.00 |
| 8 | 0.02 |
| 9 | 0.00 |
| 10 | 0.02 |

(b) $\frac{7}{50}=0.14 ; 14 \%$ of the time she first missed on the fourth try.
(c) $\frac{1}{50}=0.02 ; 2 \%$ of the time she first missed on the tenth try.
(d) 'at least 5' means that the basketball player misses on the $6^{\text {th }}$ shot or $7^{\text {th }}$ shot or $8^{\text {th }}$, etc. $\frac{3+0+1+0+1}{50}=\frac{5}{50}=0.10$ or $10 \%$ of the time.
21. From the legend, $1 \mid 0$ represents 10 , so the original data set is:
$10,11,14,21,24,24,27,29,33,35,35,35$, $37,37,38,40,40,41,42,46,46,48,49,49$, 53, 53, 55, 58, 61, 62
22. From the legend, $24 \mid 0$ represents 240 , so the original data set is:
$240,244,247,252,252,253,259,259,263$, 264, 265, 268, 268, 269, 270, 271, 271, 273, 276, 276, 282, 283, 288
23. From the legend, $1 \mid 2$ represents 1.2 , so the original data set is:
$1.2,1.4,1.6,2.1,2.4,2.7,2.7,2.9,3.3,3.3$, $3.3,3.5,3.7,3.7,3.8,4.0,4.1,4.1,4.3,4.6$, $4.6,4.8,4.8,4.9,5.3,5.4,5.5,5.8,6.2,6.4$
24. From the legend, $12 \mid 3$ represents 12.3 , so the original data set is:
$12.3,12.7,12.9,12.9,13.0,13.4,13.5,13.7$, $13.8,13.9,13.9,14.2,14.4,14.4,14.7,14.7$, $14.8,14.9,15.1,15.2,15.2,15.5,15.6,16.0$, 16.3
25. (a) 8 classes
(b) Lower class limits: 775, 800, 825, 850, 875, 900, 925, 950
Upper class limits: 799, $824,849,874$, 899, 924, 949, 974
(c) The class width is found by subtracting consecutive lower class limits. For example, $800-775=25$. Therefore, the class width is 25 (dollars).
26. (a) 8 classes
(b) Lower class limits: $0,1.0,2.0,3.0,4.0$, 5.0, 6.0, 7.0, 8.0

Upper class limits: $0.9,1.9,2.9,3.9,4.9$, 5.9, 6.9, 7.9, 8.9
(c) The class width is found by subtracting consecutive lower class limits. For example, $2.0-1.0=1.0$. Therefore, the class width is 1.0 .
27. (a) 7 classes
(b) Lower class limits: $15,20,25,30,35,40$, 45; Upper class limits: $19,24,29,34,39$, 44, 49
(c) The class width is found by subtracting consecutive lower class limits. For example, $20-15=5$. Therefore, the class width is 5 (years).
28. (a) 6 classes
(b) Lower class limits: $0,5000,10,000$, $15,000,20,000,25,000$
Upper class limits: 4999, 9999, 19,999, 24,999, 29,999
(c) The class width is found by subtracting consecutive lower class limits. For example, $10,000-5000=5000$. Therefore, the class width is 5000 (students).
29. (a) Total frequency is:
$22+68+15+5+0+0+0+1=111$
Relative frequency for 775-779 is $22 / 111=0.1982$ and so on.

| Tuition (\$) | Relative <br> Frequency |
| :---: | :---: |
| $775-799$ | 0.1982 |
| $800-825$ | 0.6126 |
| $825-849$ | 0.1351 |
| $850-874$ | 0.0450 |
| $875-899$ | 0.0000 |
| $900-924$ | 0.0000 |
| $925-949$ | 0.0000 |
| $950-974$ | 0.0090 |

(b)

(c)


Total number of California community colleges with tuition less than $\$ 800$ is 22 .
$\frac{22}{111} \cdot 100 \% \approx 19.82 \%$ of California community colleges had tuition of less than $\$ 800$.
Total number of colleges with tuition of $\$ 850$ or more $=5+1=6$
$\frac{6}{111} \cdot 100 \% \approx 5.41 \%$ of California community colleges had tuition of $\$ 850$ or more.
30. (a) Total number of earthquakes is:
$22+22+3201+3332+7276+1430+$ $130+18+1=15,342$
Relative frequency for 0-0.9 is $22 / 15,342=0.0014$ and so on.

| Magnitude | Relative Frequency |
| :---: | :---: |
| $0-0.9$ | 0.0014 |
| $1.0-1.9$ | 0.0014 |
| $2.0-2.9$ | 0.2086 |
| $3.0-3.9$ | 0.2172 |
| $4.0-4.9$ | 0.4743 |
| $5.0-5.9$ | 0.0932 |
| $6.0-6.9$ | 0.0085 |
| $7.0-7.9$ | 0.0012 |
| $8.0-8.9$ | 0.0001 |

(b)

Worldwide Earthquakes, 2010


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$\frac{7,276}{15,432} \cdot 100 \%=47.15 \%$ of earthquakes
registered 4.0-4.9 in magnitude, and $\frac{22+22+3201+3332+7276}{15,432} \cdot 100 \%$
$=\frac{13,853}{15,432} \cdot 100 \%=89.77 \%$
of earthquakes in 2007 registered 4.9 or less in magnitude.
31. (a) Total births $=445,045+1,082,837+$
$1,208,405+962,179+499,816+105,071+$ $7,349=4,310,802$
Relative frequency for 15-19 = $445,045 / 4,310,802=0.1032$ and so on.

| Age | Relative Frequency |
| :---: | :---: |
| $15-19$ | 0.1032 |
| $20-24$ | 0.2512 |
| $25-29$ | 0.2803 |
| $30-34$ | 0.2232 |
| $35-39$ | 0.1160 |
| $40-44$ | 0.0244 |
| $45-49$ | 0.0017 |

(c)


The relative frequency is 0.0244 , so $2.44 \%$ of live births were to women 40-44 years of age.
$0.1032+0.2512=0.3544$ so $35.44 \%$ of live births were to women 24 years of age or younger.
32. (a) Total frequency:
$17+18+7+5+0+1=48$
Relative frequency for 0-4999 is $17 / 45=0.3542$ and so on.

| Enrollment | Relative Frequency |
| :---: | :---: |
| $0-4999$ | 0.3542 |
| $5000-9999$ | 0.3750 |
| $10,000-14,999$ | 0.1458 |
| $15,000-19,999$ | 0.1042 |
| $20,000-24,999$ | 0.0000 |
| $25,000-29,999$ | 0.0208 |

(b)

(c)


The relative frequency is 0.3750 , so $37.50 \%$ of public Illinois community colleges enrolled between 5000 and 9999 students.
$0.1042+0+0.0208=0.1250$, so $12.50 \%$ of public Illinois community colleges enrolled 15,000 or more students.
33. (a) The data are discrete. The possible values for the number of color televisions in a household are countable.
(b), (c)

The relative frequency for 0 color televisions is $1 / 40=0.025$, and so on.

| Number of <br> Color TVs | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| 0 | 1 | 0.025 |
| 1 | 14 | 0.350 |
| 2 | 14 | 0.350 |
| 3 | 8 | 0.200 |
| 4 | 2 | 0.050 |
| 5 | 1 | 0.025 |

(d) The relative frequency is 0.2 so $20 \%$ of the households surveyed had 3 color televisions.
(e) $0.05+0.025=0.075$
$7.5 \%$ of the households in the survey had 4 or more color televisions.
(f)

(g)

34. (a) The data are discrete. The possible values for the number of customers waiting for a table are countable.
(b) and (c)

Relative frequency of 3 customers waiting $=2 / 40=0.05$, and so on.

| Number of <br> Customers | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| 3 | 2 | 0.050 |
| 4 | 3 | 0.075 |
| 5 | 3 | 0.075 |
| 6 | 5 | 0.125 |
| 7 | 4 | 0.100 |
| 8 | 8 | 0.200 |
| 9 | 4 | 0.100 |
| 10 | 4 | 0.100 |
| 11 | 4 | 0.100 |
| 12 | 0 | 0.000 |
| 13 | 2 | 0.050 |
| 14 | 1 | 0.025 |

(d) $10.0+10.0+0.0+5.0+2.5=27.5 \%$ of the Saturdays had 10 or more customers waiting for a table at 6 p.m.
(e) $5.0+7.5+7.5=20.0 \%$ of the Saturdays had 5 or fewer customers waiting for a table at 6 p.m.
(f)

(g)

(h) The distribution is more or less symmetric.
(h) The distribution is skewed right.
35. (a) and (b)

Relative frequency for $24,000-26,999=8 / 51=$ 0.1569 and so on.

| Disposable Income (\$) | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $30,000-35,999$ | 21 | 0.4118 |
| $36,000-41,999$ | 18 | 0.3529 |
| $42,000-47,999$ | 7 | 0.1373 |
| $48,000-53,999$ | 3 | 0.0588 |
| $54,000-59,999$ | 1 | 0.0196 |
| $60,000-65,999$ | 0 | 0.0000 |
| $66,000-71,999$ | 1 | 0.0196 |

(c)

Per Capita Disposable Income by State, 2009

(d)

Per Capita Disposable Income by State, 2009

(e) The distribution appears to be skewed right.
(f) Relative frequency for 30,000-32,999 = $10 / 51=0.1961$ and so on.

| Disposable Income (\$) | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $30,000-32,999$ | 9 | 0.1765 |
| $33,000-35,999$ | 12 | 0.2353 |
| $36,000-38,999$ | 10 | 0.1961 |
| $39,000-41,999$ | 8 | 0.1569 |
| $42,000-44,999$ | 5 | 0.0980 |
| $45,000-47,999$ | 2 | 0.0392 |
| $48,000-50,999$ | 3 | 0.0588 |
| $51,000-53,999$ | 0 | 0.0000 |
| $54,000-56,999$ | 1 | 0.0196 |
| $57,000-59,999$ | 0 | 0.0000 |
| $60,000-62,999$ | 0 | 0.0000 |
| $63,000-65,999$ | 0 | 0.0000 |
| $66,000-68,999$ | 1 | 0.0196 |

Per Capita Disposable Income by State, 2009


Per Capita Disposable Income by State, 2009


The distribution appears to be skewed right.
(g) Answers will vary. While both distributions indicate the data are skewed right, the first distribution provides a more detailed look at the data. The second distribution has a larger width of the bars, which can potential obscure details in the data.
36. (a) and (b)

Relative frequency for 4.0-5.9 $=1 / 51$
$=0.0196$ and so on.

| $\%$ Uninsured | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $4.0-5.9$ | 1 | 0.0196 |
| $6.0-7.9$ | 0 | 0.0000 |
| $8.0-9.9$ | 5 | 0.0980 |
| $10.0-11.9$ | 9 | 0.1765 |
| $12.0-13.9$ | 6 | 0.1176 |
| $14.0-15.9$ | 7 | 0.1373 |
| $16.0-17.9$ | 5 | 0.0980 |
| $18.0-19.9$ | 11 | 0.2157 |
| $20.0-21.9$ | 5 | 0.0980 |
| $22.0-23.9$ | 1 | 0.0196 |
| $24.0-25.9$ | 1 | 0.0196 |

(c)

Uninsured Rates by State, 2009

(d)

Uninsured Rates by State, 2009

(e) The distribution is symmetric.
(f) Relative frequency for 4.0-7.9 $=1 / 51$ $=0.0196$ and so on.

| $\%$ Uninsured | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $4.0-7.9$ | 1 | 0.0196 |
| $8.0-11.9$ | 14 | 0.2745 |
| $12.0-15.9$ | 13 | 0.2549 |
| $16.0-19.9$ | 16 | 0.3137 |
| $20.0-23.9$ | 6 | 0.1176 |
| $24.0-25.9$ | 1 | 0.0196 |

Uninsured Rates by State, 2009


Uninsured Rates by State, 2009


The distribution is symmetric.
(g) Answers will vary. Both frequency distributions show the data are skewed right. The number of classes in the first distribution gives more detail, but this makes the graph a bit more jagged. The second distribution gives a cleaner view of the data.
37. (a) and (b)

Total number of data points $=51$
Relative frequency of 0-0.49 is:
$7 / 51=0.1373$, and so on.

| Cigarette Tax | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| $0.00-0.49$ | 7 | 0.1373 |
| $0.50-0.99$ | 14 | 0.2745 |
| $1.00-1.49$ | 7 | 0.1373 |
| $1.50-1.99$ | 8 | 0.1569 |
| $2.00-2.49$ | 6 | 0.1176 |
| $2.50-2.99$ | 4 | 0.0784 |
| $3.00-3.49$ | 4 | 0.0784 |
| $3.50-3.99$ | 0 | 0.0000 |
| $4.00-4.49$ | 1 | 0.0196 |

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Cigarette Tax Rates by State, 2010

(d)

Cigarette Tax Rates by State, 2010

(e) The distribution appears to be right skewed.
(f) Relative frequency of $0-0.99$ is:
$21 / 51=0.4118$, and so on.

| Cigarette Tax | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| $0.00-0.99$ | 21 | 0.4118 |
| $1.00-1.99$ | 15 | 0.2941 |
| $2.00-2.99$ | 10 | 0.1961 |
| $3.00-3.99$ | 4 | 0.0784 |
| $4.00-4.99$ | 1 | 0.0196 |

Cigarette Tax Rates by State, 2010


Cigarette Tax Rates by State, 2010


The distribution is right skewed.
(g) Answers will vary. The first distribution gives a more detailed pattern.
38. (a) and (b)

Relative frequency for 0.00-0.39 $=7 / 28$ $=0.2500$, and so on.

| Dividend | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $0.00-0.39$ | 7 | 0.2500 |
| $0.40-0.79$ | 4 | 0.1429 |
| $0.80-1.19$ | 5 | 0.1786 |
| $1.20-1.59$ | 2 | 0.0714 |
| $1.60-1.99$ | 3 | 0.1071 |
| $2.00-2.39$ | 4 | 0.1429 |
| $2.40-2.79$ | 2 | 0.0714 |
| $2.80-3.19$ | 1 | 0.0357 |

(c)

(d)

Dividend Yield

(e) The distribution is skewed right.
(f) Relative frequency for 0.00-0.79 $=11 / 28$
$=0.3929$ and so on.

| Dividend | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $0.00-0.79$ | 11 | 0.3929 |
| $0.80-1.59$ | 7 | 0.2500 |
| $1.60-2.39$ | 7 | 0.2500 |
| $2.40-3.19$ | 3 | 0.1071 |

Dividend Yield


Dividend Yield


The distribution is skewed right.
(g) Answers will vary. Both distributions indicate the data are skewed right. The first graph is preferred because it gives more detailed information. The second graph is a little too compressed to get a complete view of what is happening with the data.
39. Answers will vary. One possibility follows.
(a) Lower class limit of first class: 100; We can determine a class width by subtracting the smallest value from the largest, dividing by the desired number of classes, then rounding up. For example,
Class width $\approx \frac{1345.9-119.8}{13}=94.3 \rightarrow 100$
So, a class width 100 should suffice.
(b), (c)

Relative frequency for 100-199 is:
$4 / 51=0.0784$, and so on.

| Violent Crimes <br> per 100,000 | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $100-199$ | 4 | 0.0784 |
| $200-299$ | 17 | 0.3333 |
| $300-399$ | 7 | 0.1373 |
| $400-499$ | 11 | 0.2157 |
| $500-599$ | 3 | 0.0588 |
| $600-699$ | 7 | 0.1373 |
| $700-799$ | 1 | 0.0196 |
| $800-899$ | 0 | 0.0000 |
| $900-999$ | 0 | 0.0000 |
| $1000-1099$ | 0 | 0.0000 |
| $1100-1199$ | 0 | 0.0000 |
| $1200-1299$ | 0 | 0.0000 |
| $1300-1399$ | 1 | 0.0196 |

(d)

Violent Crimes per $\mathbf{1 0 0 , 0 0 0}$
Population by State, 2009

(e)

(f) The distribution is skewed right.
40. Answers will vary. One possibility follows.
(a) We can determine a class width by subtracting the smallest value from the largest, dividing by the desired number of classes, then rounding up. For example, $\frac{23.59-6.37}{6}=2.87 \rightarrow 3$

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Our first lower class limit should be a nice number below the smallest data value. In this case, 6 is a good first lower limit since it is the nearest whole number below the smallest data value. Thus, we will have a class width of 3 and the first class will have a lower limit of 6 .
(b), (c)

Relative frequency for 6-8.99 $=15 / 35$
$=0.4286$ and so on.

| Volume | Freq. | Rel. Freq. |
| :---: | :---: | :---: |
| $6-8.99$ | 15 | 0.4286 |
| $9-11.99$ | 9 | 0.2571 |
| $12-14.99$ | 4 | 0.1143 |
| $15-17.99$ | 4 | 0.1143 |
| $18-20.99$ | 2 | 0.0571 |
| $21-23.99$ | 1 | 0.0286 |

(d)

Daily Volume of Altria Stock

(e)

(f) The distribution is skewed right.

41. (a) President Ages at Inauguration | 4 | 23 |
| :--- | :--- |
| 4 | 6677899 |
| 5 | 0011112244444 |
| 5 | 555566677778 |
| 6 | 0111244 |
| 6 | 589 |
| Legend: $4 \mid 2$ represents 42 years. |  |

(b) The distribution appears to be roughly symmetric and bell shaped.
42. (a)

Divorce Rates by State, 2006

```
2 \123 [ \ 5678999
3000233
3 555666889999
4
4 57789
5 1134
5
```

Legend: 211 represents 2.1 divorces per 1000 population.
(b) The distribution appears to be roughly symmetric and bell shaped. One could argue that the distribution is slightly skewed right.
43. (a) Fat in McDonald's Breakfast

| 0 | 39 |
| :--- | :--- |
| 1 | 1266 |
| 2 | 1224577 |
| 3 | 0012267 |
| 4 | 6 |
| 5 | 159 |

Legend: 511 represents 51 grams of fat.
(b) The distribution appears to be roughly symmetric and bell shaped.
44. (a) Gasoline Mileages

| 2 | 2233 |
| :--- | :--- |
| 2 | 55567889999 |
| 3 | 00000111111111222223333333333334444444444444 |
| 3 | 55555555566666666666778 |
| 4 | 0223 |
| Legend: 212 represents 22 miles per gallon. |  |

(b) The distribution appears to be symmetric and bell shaped.
45. (a) Rounded data:

| 17.3 | 10.5 | 8.7 | 9.4 | 8.8 | 6.7 | 6.5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12.3 | 9.6 | 8.9 | 13.1 | 8.8 | 7.5 | 15.4 |
| 14.5 | 7.5 | 8.1 | 8.6 | 7.8 | 10.2 | 25.3 |
| 14.6 | 10.4 | 7.7 | 8.6 | 7.6 | 9.0 |  |
| 14.6 | 9.4 | 8.1 | 8.8 | 8.1 | 7.6 |  |
| 13.2 | 10.0 | 12.3 | 7.1 | 9.8 | 6.1 |  |
| 15.7 | 7.8 | 13.9 | 9.2 | 10.5 | 14.4 |  |
| 17.2 | 8.6 | 10.7 | 6.9 | 10.0 | 7.7 |  |

## Electric Rates by State, 2010

| 6 | 1579 |
| ---: | :--- |
| 7 | 155667788 |
| 8 | 11166678889 |
| 9 | 024468 |
| 10 | 0024557 |
| 11 |  |
| 12 | 33 |
| 13 | 129 |
| 14 | 4566 |
| 15 | 47 |
| 16 |  |
| 17 | 23 |
| 18 |  |
| 19 |  |
| 20 |  |
| 21 |  |
| 22 |  |
| 23 |  |
| 24 |  |
| 25 | 3 |
| Legend: 611 represents 6.1 cents per kWh. |  |

(b) The distribution is skewed right.
(c) Hawaii's average retail price is 25.33 cents/kWh. Hawaii's rate may be so much higher because it is an island far away from the mainland. Resources on the island are limited and importing resources increases the overall cost. (Answers will vary.)
46. (a) Rounded data:

| 68 | 100 | 94 | 222 | 121 | 121 | 97 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 118 | 86 | 96 | 131 | 94 | 112 | 170 |
| 91 | 89 | 87 | 123 | 193 | 80 | 93 |
| 59 | 92 | 124 | 126 | 59 | 202 | 87 |
| 118 | 119 | 75 | 71 | 90 | 89 | 113 |
| 180 | 80 | 108 | 138 | 86 | 162 | 85 |
| 119 | 98 | 49 | 106 | 85 | 33 | 91 |
| 89 | 111 |  |  |  |  |  |

## Home Appreciation from 1991 to 2010

| 3 | 3 |
| ---: | :--- |
| 4 | 9 |
| 5 | 99 |
| 6 | 8 |
| 7 | 15 |
| 8 | 00556677999 |
| 9 | 0112344678 |
| 10 | 068 |
| 11 | 1238899 |
| 12 | 11346 |
| 13 | 18 |
| 14 |  |
| 15 |  |
| 16 | 2 |
| 17 | 0 |
| 18 | 0 |
| 19 | 3 |
| 20 | 2 |
| 21 |  |
| 22 | 2 |
| Legend: 813 represents 33 percent price increase. |  |

(b) The distribution is skewed right.
(c) Answers will vary.
47. (a) Violent crime rates rounded to the nearest tens:

| 450 | 1350 | 400 | 280 | 380 | 670 | 300 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 630 | 610 | 260 | 490 | 400 | 190 | 260 |
| 410 | 430 | 620 | 250 | 200 | 670 | 230 |
| 520 | 270 | 120 | 280 | 330 | 490 |  |
| 470 | 230 | 590 | 700 | 500 | 210 |  |
| 340 | 500 | 460 | 160 | 250 | 130 |  |
| 300 | 330 | 500 | 310 | 380 | 230 |  |
| 640 | 280 | 240 | 620 | 250 | 330 |  |

(b) Violent Crime Rates by State, 2009

1||2369

```
2 013334555667888
3 001333488
4 001356799
5 00029
6 1223477
7 0
9
10
Legend: 112 represents 120 violent crimes per 100,000 population
```

(c)

Violent Crime Rates by State, 2009

| 1 | 23 |
| ---: | :--- |
| 1 | 69 |
| 2 | 013334 |
| 2 | 555667888 |
| 3 | 0013334 |
| 3 | 88 |
| 4 | 0013 |
| 4 | 56799 |
| 5 | 0002 |
| 5 | 9 |
| 6 | 12234 |
| 6 | 77 |
| 7 | 0 |
| 7 |  |
| 8 |  |
| 8 |  |
| 9 |  |
| 9 |  |
| 10 |  |
| 10 |  |
| 11 |  |
| 11 |  |
| 12 |  |
| 12 |  |
| 13 |  |
| 13 | 5 |

(d) Answers will vary. The first display is decent. It clearly shows that the distribution is skewed right and has an outlier. The second display is not as good as the first. Splitting the stems did not reveal any additional information and has made the display more cluttered and cumbersome.
48. (a) Ages of Academy Award Winners


Legend: 6|7|4 represents 76 years old for Best Actor and 74 years old for Best Actress.
(b) Answers will vary. It appears that Academy Award winners for best actor tend to be older on the whole than winners for best actress.
49. (a)

| Home Run Distances |  |  |
| :---: | :---: | :---: |
| McGwire |  | Bonds |
|  | 32 <br> 33 | 00 |
| 10 | 34 | 7 |
| 00 | 35 | 0 |
| 9000 | 36 | 00015 |
| 70000 | 37 | 005555 |
| 85500000 | 38 | 000005 |
| 80000 | 39 | 00146 |
| 900 | 40 | 000045 |
| 00000 | 41 | 0000000000155677 |
| 5300000 | 42 | 000000009 |
| 0000000 | 43 | 00000556 |
| 000 | 44 | 00002 |
| 820000 | 45 | 04 |
| 100 | 46 |  |
| 8000 | 47 |  |
| 0 | 48 49 | 8 |
| 0 | 50 |  |
| 00 | 51 |  |
| 7 | 52 53 |  |
|  | 53 54 |  |
|  |  |  |

Legend: $0|34| 7$ represents 340 feet for McGwire and 347 feet for Bonds.
(b) Answers will vary. For both players, the distances of homeruns mainly fall from 360 to 450 feet. McGwire has quite a few extremely long distances.
50. Answers will vary.
51. Answers will vary.
52.



There are several similarities in the distribution of the ideal number of children, as reported by males and females. However, females seem more likely to esteem larger families as ideal.
A histogram would better serve us in comparing the preferences between males and females.
53.

Televisions in Household

54.

Customers Waiting for a Table

55. The price of Disney stock over the year seemed to fluctuate somewhat, with a general upward trend.

Walt Disney Company, 2010


The percent change in the stock price of Disney from January 2010 to December 1010 is $30.7 \%$.
56. Since going public, the price of Google stock has increased rapidly at the onset with a sharp decrease in 2008, and then a recovery in 2009 and a slight decrease in 2010.

Google Inc. Stock


The percent change in the stock price of Google from 2009 to 2010 is $-4.2 \%$.
57. During the late 1990s debt as a percent of GDP was decreasing. It was increasing slightly during the early to mid 2000s. It has increased substantially from 2007 to 2010.

58. The percent of recent high school graduates enrolling in college seems to have increased slightly over the given time period amid a variety of fluctuations. The early 1990s showed no increase, but this was followed by an unusual jump and decline in the mid-to-late

1990s. There has been a steady increase since 2000 (with the exception of 2005 to 2006.)

59. Because the data are quantitative, either a stem-and-leaf plot or a histogram would be appropriate. There were 20 people who spent less than 30 seconds, 7 people spent at least 30 seconds but less than 60 seconds, etc. One possible histogram is:


The data appear to be skewed right with a gap and one potential outlier. It seems as if the majority of surfers spent less than one minute viewing the page, while a few surfers spent several minutes viewing the page.
60. Age: histogram, stem-and-leaf plot, or dot plot; Income: histogram or stem-and-leaf plot; Marital status: bar graph or pie chart; Number of vehicles: histogram, stem-and-leaf plot, or dot plot
61. Answers will vary. Reports should address the fact that the number of people going to the beach and participating in underwater activities (e.g. scuba diving, snorkeling) has also increased, so an increase in shark attacks is not unexpected. A better comparison would be the rate of attacks per 100,000 beach visitors. The number of fatalities could decrease due to better safety equipment (e.g. bite resistant suits) and better medical care.
62. Classes should not overlap to avoid any confusion as to which class an observation belongs.
63. Histograms are useful for large data sets or data sets with a large amount of spread. Stemand -leaf plots are nice because the raw data can easily be retrieved. A disadvantage of stem-and-leaf plots is that sometimes the data must be rounded, truncated, or adjusted in some way that requires extra work. Furthermore, if these steps are taken, the original data is lost and a primary advantage of stem-and-leaf plots is lost.
64. There is no such thing as the correct choice for a class width; however, some choices are better than others. For example, if the class width is too small, the histogram will show many gaps between the bars.
65. Relative frequencies should be used when comparing two data sets with different sample sizes.
66. Answers will vary.
67. Answers will vary. Sample histograms are given below.

Skewed Right


Skewed Left



A histogram is skewed left if it has a long tail on the left side. A histogram is skewed right if it has a long tail on the right side. A histogram is symmetric if the left and right sides of the graph are roughly mirror images of each other. A histogram is uniform if all the bars are about the same height.
68. Answers will vary. Time series plots are drawn with quantitative variables. They are drawn to see trends in the data.

## Section 2.3

1. The lengths of the bars are not proportional. For example, the bar representing the cost of Clinton's inauguration should be slightly more than 9 times as long as the one for Carter's cost, and twice as long as the bar representing Reagan's cost.
2. (a) The lengths of the bars are not proportional. For example, the bar for soda is $1 / 3$ the size of the bar for cheeseburger, but the number of steps for a cheeseburger is just over twice that for the soda. In addition, it is unclear where the graph begins: at the base of each figure or the bottom of the platform.
(b) Answers will vary. The pictures could be replaced by simple bars (of the same width) that are proportional in area.
3. (a) The vertical axis starts at 34,500 instead of 0 . This tends to indicate that the median earnings for females changed at a faster rate than actually occurred.
(b) This graph indicates that the median earnings for females has decreased slightly over the given time period.

Median Earnings for Females

4. (a) The vertical axis starts at 4 instead of 0 . This might cause the reader to conclude, for example, the percentage of employed people aged 55-64 who are members of a union is more than double the percentage of those aged 25-34 years.
(b)

5. The bar for $12 p-6 p$ covers twice as many hours as the other bars. By combining two 3-hour periods, this bar looks larger compared to the others, making afternoon hours look more dangerous. If this bar were split into two periods, the graph may give a different impression. For example, the graph may show that daylight hours are safer.
6. The article is basing its conclusion on a comparison of categories that do not cover the same number of years. A better comparison is the incidence rate (number of accidents per 100,000 licensed drivers). [Note: only about $14 \%$ of licensed drivers in 2005 were aged 24 years or younger.]
7. (a) The vertical axis starts at 0.1 instead of 0 . This might cause the reader to conclude, for example, that the proportion of people aged 25-34 years old who are not covered by any type of health insurance is more
than 3 times the proportion for those aged 55-64 years old.
(b)

8. (a) The vertical axis starts at 50 without indicating a gap.
(b) The graph may be trying to convey that new home construction in the Midwest increased significantly between 2000 and 2004, then declined at roughly twice the rate between 2004 and 2009 .
(c) The graph does support this view. The sharp drop after 2005 indicates a market cooling and less demand for new construction. The National Association of Realtors was not correct in their assessment of the new home market.
9. This graph is misleading because it does not take into account the size of the population of each state. Certainly, Vermont is going to pay less in total taxes than California simply because its population is so much lower. The moral of the story here is that many variables should be considered on a per capita (per person) bias. For example, this graph should be drawn with taxes paid per capita (per person).
10. (a) $\frac{726.6}{7.5}=96.88 \rightarrow 97$

Since the oil reserve in 2009 was about 97 times the oil reserve in 1977, the graphic for 2009 should be 97 times the size (i.e. area) of the graphic for 1977.
(b) $\frac{726.6 \text { million }}{10 \text { million }}=\frac{726.6}{10} \approx 72.7$

Assuming no change in production, the 2009 oil reserves would last about 73 days.
11. (a) The graphic is misleading because the bars are not proportional. The bar for housing should be a little more than twice the length of the bar for transportation, but it is not.
(b) The graphic could be improved by adjusting the bars so that their lengths are proportional.
12. (a)


The graphic is misleading because it starts at 7 instead of 0 without indicating a gap. This might cause the reader to conclude that cost of electricity has risen more sharply than actually occurred.
(b)

13. (a)
U.S. Adults Who Believe Moral Values are Poor


This graphic is misleading because the vertical scale starts at 34 instead of 0 without indicating a gap. This might cause the reader to think that the proportion of U.S. adults who believe moral values are poor is increasing more
quickly than they really are.
(b)
U.S. Adults Who Believe Moral Values are Poor

14. The graphic does not support the safety manager's claim. The vertical scale starts at 0.17 instead of 0 , so the difference between the bars is distorted. While there has been a decrease in the proportion of workers injured, it appears that the decrease is only about $10 \%$ of the 1992 rate.
15. (a) The politician's view:

Health Care as a Percent of GDP

(b) The health care industry's view:

Health Care as a Percent of GDP

(c) A view that is not misleading:

Health Care as a Percent of GDP

16. (a) A graph that is not misleading will use a vertical scale starting at $\$ 0$ and bars of equal width. Here is one example:

(b) A graph that is misleading might use bars of unequal width or will use a vertical scale that does not start at $\$ 0$. One example, as follows, indicates that the average price for regular unleaded gasoline has increased tremendously from 2001 to 2011.

Unleaded Gasoline Cost

17. (a) A graph that is not misleading will use a vertical scale starting at $0 \%$ and bars of equal width. One example:

Overweight Adults in U.S.

(b) A graph that is misleading might use bars of unequal width or will use a vertical scale that does not start at $0 \%$. One example, as follows, implies that the percent of overweight adults in the U.S. has more than quadrupled between 1980 and 2010.

Overweight Adults in U.S.

18. (a) A bar graph
(b) A reader cannot tell whether the graph ends at the top of the nipple on the baby bottle, or at the end of the milk.
(c)

19. This is a histogram and the bars do not touch. In addition, there are no labels on the axes and there is not title on the graph.
20. (a) The two variables being graphed are Cornell's tuition and Cornell's ranking.

Tuition: quantitative, discrete, interval level of measurement

Ranking: qualitative, ordinal level of measurement
(b) The graph was likely generated from existing data sources such as the U.S. Department of Education.
(c) The graph is a time series plot because the data are plotted in time order.
(d) Answers may vary. The graph appears to show that the cost to attend Cornell is increasing while its ranking is decreasing. The graph is misleading because the ranking graph may imply that ranking is getting worse (the graph goes down) when in fact a lower value means a better ranking.
(e) Answers may vary. No horizontal or vertical scale is provided; the horizontal scale is inconsistent; the vertical scale is inconsistent between graphs; the reader's attention is drawn more to the picture than the data.

## Chapter 2 Review Exercises

1. (a) There are $614+154+1448=2216$ participants.
(b) The relative frequency of the respondents indicating that it makes no difference is
$\frac{1448}{2216} \approx 0.653$
(c) A Pareto chart is a bar chart where the bars are in descending order.

Convincing Voice in Purchasing a Car

(d) Answers will vary.
2. (a) Total homicides $=9,146+1,825+611+$ $801+121+99+895=13,498$
Relative frequency for Firearms $=$ $\frac{9,146}{13,498} \approx 0.6776$ and so on.

| Type of Weapon | Relative <br> Frequency |
| :--- | :---: |
| Firearms | 0.6776 |
| Knives or <br> cutting intstruments | 0.1352 |
| Blunt objects <br> (clubs, hammers, etc.) | 0.0453 |
| Personal weapons <br> (hands, fists, etc.) | 0.0593 |
| Strangulation | 0.0090 |
| Fire | 0.0073 |
| Other weapon <br> or not stated | 0.0663 |

(b) The relative frequency is 0.0453 , so $4.5 \%$ of the homicides were due to blunt objects.
(c)

(d)

(e)

3. (a) Total births (in thousands) $=6+435+$ $1053+1197+958+489+106=4244$ Relative frequency for 10-14 year old mothers $=6 / 4244 \approx 0.0014$ and so on.

| Age of <br> Mother | Rel. <br> Freq. |
| :---: | :---: |
| $10-14$ | 0.0014 |
| $15-19$ | 0.1025 |
| $20-24$ | 0.2481 |
| $25-29$ | 0.2820 |
| $30-34$ | 0.2257 |
| $35-39$ | 0.1152 |
| $40-44$ | 0.0250 |

(b) The distribution is roughly symmetric and bell shaped.

Live Births in the U.S. by Age of Mother

(c)

Live Births in the U.S. by Age of Mother

(d) From the relative frequency table, the relative frequency of $20-24$ is 0.2481 and so the percentage is $24.81 \%$.
(e) $\frac{958+489+106}{4244}=\frac{1553}{4244} \approx 0.3659$
$36.59 \%$ of live births were to mothers aged 30 years or older.
4. (a) and (b)

| Affiliation | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| Democrat | 46 | 0.46 |
| Independent | 16 | 0.16 |
| Republican | 38 | 0.38 |



Political Affiliation
(d)

(e) Democrat appears to be the most common affiliation in Naperville.
5. (a), (b)

| Family <br> Size | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| 0 | 7 | 0.1167 |
| 1 | 7 | 0.1167 |
| 2 | 18 | 0.3000 |
| 3 | 20 | 0.3333 |
| 4 | 7 | 0.1167 |
| 5 | 1 | 0.0167 |

(c) The distribution is more or less symmetric.

Number of Children for Couples Married 7 Years

(d)

(e) From the relative frequency table, the relative frequency of two children is 0.3000 so $30 \%$ of the couples have two children.

## Chapter 2: Organizing and Summarizing Data

(f) From the frequency table, the relative frequency of at least two children (i.e. two or more) is

$$
0.3000+0.3333+0.1167+0.0167=0.7667
$$ or $76.67 \%$. So, $76.67 \%$ of the couples have at least two children.

(g)

6. (a), (b)

| Ownership <br> Rate | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| $40-44.9$ | 1 | 0.0196 |
| $45-49.9$ | 0 | 0.0000 |
| $50-54.9$ | 1 | 0.0196 |
| $55-59.9$ | 2 | 0.0392 |
| $60-64.9$ | 2 | 0.0392 |
| $65-69.9$ | 19 | 0.3725 |
| $70-74.9$ | 21 | 0.4118 |
| $75-79.9$ | 5 | 0.0980 |

(c)

Home Ownership Rates by State, 2009

(d)

(e) The distribution is skewed left.
(f)

| Ownership <br> Rate | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| $40-49.9$ | 1 | 0.0196 |
| $50-59.9$ | 3 | 0.0588 |
| $60-69.9$ | 21 | 0.4118 |
| $70-79.9$ | 26 | 0.5098 |

Home Ownership Rates by State, 2009
 Home Ownership Rates by State, 2009


The distribution is skewed left.
Answers will vary. Both class widths give a good overall picture of the distribution. The first class width provides a little more detail to the graph, but not necessarily enough to be worth the trouble. An intermediate value, say a width of 500, might be a reasonable compromise.
7. (a), (b)

Answers will vary. Using 2.2000 as the lower class limit of the first class and 0.0200 as the class width, we obtain the following.

| Class | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| $2.2000-2.2199$ | 2 | 0.0588 |
| $2.2200-2.2399$ | 3 | 0.0882 |
| $2.2400-2.2599$ | 5 | 0.1471 |
| $2.2600-2.2799$ | 6 | 0.1765 |
| $2.2800-2.2999$ | 4 | 0.1176 |
| $2.3000-2.3199$ | 7 | 0.2059 |
| $2.3200-2.3399$ | 5 | 0.1471 |
| $2.3400-2.3599$ | 1 | 0.0294 |
| $2.3600-2.3799$ | 1 | 0.0294 |

(c)


The distribution is roughly symmetric.
(d)

8.

```
l_}\begin{array}{l}{\mathrm{ Hours Spent Online }}\\{12}
```

The distribution is slightly skewed right.
9. (a) Grade inflation seems to be happening in colleges. GPAs have increased every time period for all schools.
(b) GPAs increased $5.6 \%$ for public schools. GPAs increased $6.8 \%$ for private schools. Private schools have higher grade inflation because the GPAs are higher and they are increasing faster.
(c) The graph is misleading because it starts at 2.6 on the vertical axis.
10. (a) Answers will vary. The adjusted gross income share of the top $1 \%$ of earners shows steady increases overall, with a few minor exceptions. The adjusted gross income share of the bottom $50 \%$ of earners shows steady decreases overall, with a few minor exceptions.
(b) Answers will vary. The income tax share of the top $1 \%$ of earners shows steady increases overall, with few exceptions, including a notable decrease from 2007 to 2008. The income tax share of the bottom $50 \%$ of earners shows steady decreases over time.

2005 Average Earnings

11. (a) Graphs will vary. One way to mislead would be to start the vertical scale at a value other than 0 . For example, starting the vertical scale at $\$ 30,000$ might make the reader believe that college graduates earn more than three times what a high school graduate earns (on average).
(b) A graph that does not mislead would use equal widths for the bars and would start the vertical scale at $\$ 0$. Here is an example of a graph that is not misleading:

2005 Average Earnings

12. (a) Flats are preferred the most ( $40 \%$ ) and extra-high heels are preferred the least (1\%).
(b) The graph is misleading because the bar heights and areas for each category are not proportional.

## Chapter 2 Test

1. (a) The United States won the most men's singles championships between 1968 and 2010 with 15 wins.
(b) $6-4=2$

Representatives from Australia have won 2 more championships than representatives from Germany.
(c) $15+8+6+5+4+2+1+1+1=43$ championships between 1968 and 2010.
$\frac{8}{43}=0.186$
Representatives of Sweden won $18.6 \%$ of the championships.
(d) No, it is not appropriate to describe the shape of the distribution as skewed right. The data represented by the graph are qualitative so the bars in the graph could be placed in any order.
2. (a) There were 1005 responses. The relative frequency who indicated they preferred new tolls was $\frac{412}{1005}=0.4100$ and so on.

| Response | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| New Tolls | 412 | 0.4100 |
| Inc. Gas Tax | 181 | 0.1801 |
| No New Roads | 412 | 0.4100 |

(b) The relative frequency is 0.1801 , so the percentage of respondents who would like to see an increase in gas taxes is $18.01 \%$.
(c)

(d)

(e)

3. (a), (b)

| Education | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| No high school <br> diploma | 9 | 0.18 |
| High school <br> graduate | 16 | 0.32 |
| Some college | 9 | 0.18 |
| Associate's degree | 4 | 0.08 |
| Bachelor's degree | 8 | 0.16 |
| Advanced degree | 4 | 0.08 |

(c)

Educational Attainment of Commuters

(d) Educational Attainment of Commuters

(e) The largest bar (and largest pie segment) corresponds to 'High School Graduate', so high school graduate is the most common educational level of a commuter.
4. (a), (b)

| No. of <br> Cars | Freq. | Rel. <br> Freq. |
| :---: | :---: | :---: |
| 1 | 5 | 0.10 |
| 2 | 7 | 0.14 |
| 3 | 12 | 0.24 |
| 4 | 6 | 0.12 |
| 5 | 8 | 0.16 |
| 6 | 5 | 0.10 |
| 7 | 2 | 0.04 |
| 8 | 4 | 0.08 |
| 9 | 1 | 0.02 |

(c)

Number of Cars Arriving at McDonald's


The distribution is skewed right.
(d)

Number of Cars Arriving at McDonald's

(e) The relative frequency of exactly 3 cars is 0.24 . So, for $24 \%$ of the weeks, exactly three cars arrived between 11:50 am and 12:00 noon.
(f) The relative frequency of 3 or more cars $=0.24+0.12+0.16+0.10$

$$
+0.04+0.08+0.02
$$

$$
=0.76
$$

So, for $76 \%$ of the weeks, three or more cars arrived between 11:50 am and 12:00 noon.
(g)

5. Answers may vary. One possibility follows:
(a), (b) Using a lower class limit of the first class of 20 and a class width of 10 :
Total number of data points $=40$
Relative frequency of $20-29=1 / 40$
$=0.025$, and so on.

| HDL <br> Cholesterol | Frequency | Relative <br> Frequency |
| :---: | :---: | :---: |
| $20-29$ | 1 | 0.025 |
| $30-39$ | 6 | 0.150 |
| $40-49$ | 10 | 0.250 |
| $50-59$ | 14 | 0.350 |
| $60-69$ | 6 | 0.150 |
| $70-79$ | 3 | 0.075 |

(c)

Serum HDL of 20-29 Year Olds

(d)

Serum HDL of 20-29 Year Olds

(e) The distribution appears to be roughly bell-shaped.
6. The stem-and-leaf diagram below shows a symmetric (uniform) distribution. Time Spent on Homework

| 4 | 0567 |
| :--- | :--- | :--- |
| 5 | 26 |
| 6 | 13 |
| 7 | 01338 |
| 8 | 59 |
| 9 | 1369 |
| 10 | 3899 |
| 11 | 0098 |
| 12 | 556 |
| Legend: 410 represents 40 minutes. |  |

7. The curves in the figure below appear to follow the same trend. Birth rate increases as per capita income increases.

Fertility Rates (births per 1000 women aged 15-44)
and per Capita Income (thousands of 2008 dollars)

8. Answers may vary. It is difficult to interpret this graph because it is not clear whether the
scale is represented by the height of the steps, the width of the steps, or by the graphics above the steps. The graphics are misleading because they must be increased in size both vertically and horizontally to avoid distorting the image. Thus, the resulting areas are not proportionally correct. The graph could be redrawn using bars whose widths are the same and whose heights are proportional based on the given percentages. The use of graphics should be avoided, or a standard size graphic representing a fixed value could be used and repeated as necessary to illustrate the given percentages.

## Case Study: The Day the Sky Roared

1. 




During the April 3-4, 1974 outbreak, $20 \%$ of the tornadoes exceeded F-3 on the Fujita Wind Damage Scale. This was much greater than the $1 \%$ that typically occurs.
2. The histogram will vary depending on the class width.

3. Histograms may vary depending on class widths. For comparison purposes, the same class width was used for each histogram.


The distributions all appear to be skewed right, though the distribution for F-5 tornadoes is difficult to see due to the low sample size. There is an obvious shift in the distributions. As the strength of the tornado increases, the duration of the tornado increases.
4. There were 305 deaths during the outbreak. Of these, 259 were due to the more severe tornadoes.
$\frac{259}{305} \approx 0.8492$
Roughly $85 \%$ of the deaths during the outbreak were due to the more severe tornadoes. This may be a little high, but it is consistent since it is greater than $70 \%$.


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5. The provided data is not sufficient to determine whether or not tornadoes are more likely to strike rural areas. Some research at Texas A\&M University indicates that tornadoes are more likely to occur in urban or suburban areas, possibly due to greater temperature differences. The data does indicate that the number of deaths decreases as the population of the community increases. The higher the population density, the greater the chance that a tornado is detected and reported early, thereby providing more time for residents to take shelter.

6. Answers will vary. The outbreak of April $3-4,1974$ seemed to be more severe in intensity than usual with $20 \%$ of the tornadoes being classified as F-4 or F-5. While the shape of the duration distribution was roughly the same for each intensity level, the duration of a tornado increased with its intensity. The number of deaths decreased as the community size increased.

