Introduction to Management Science, 12e (Taylor)

Chapter 2 Linear Programming: Model Formulation and Graphical Solution

1) Linear programming is a model consisting of linear relationships representing a firm's decisions given an objective and resource constraints.

Answer: TRUE Diff: 2 Page Ref: 32

Section Heading: Model Formulation Keywords: model formulation AACSB: Analytical thinking

2) The objective function always consists of either maximizing or minimizing some value.

Answer: TRUE Diff: 2 Page Ref: 32

Section Heading: Model Formulation

Keywords: objective function AACSB: Analytical thinking

3) The objective function is a linear relationship reflecting the objective of an operation.

Answer: TRUE Diff: 1 Page Ref: 32

Section Heading: Model Formulation Keywords: model formulation AACSB: Analytical thinking

4) A constraint is a linear relationship representing a restriction on decision making.

Answer: TRUE Diff: 1 Page Ref: 32

Section Heading: Model Formulation Keywords: model formulation AACSB: Analytical thinking

5) Proportionality means the slope of a constraint is proportional to the slope of the objective function.

Answer: FALSE Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems Keywords: properties of linear programming models, proportionality

AACSB: Analytical thinking

6) The terms in the objective function or constraints are additive.

Answer: TRUE Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems Keywords: properties of linear programming models, additive

7) The terms in the objective function or constraints are multiplicative.

Answer: FALSE Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems Keywords: properties of linear programming models, additive

AACSB: Analytical thinking

8) All linear programming models exhibit a set of constraints.

Answer: TRUE Diff: 1 Page Ref: 32

Section Heading: Model Formulation

Keywords: properties of linear programming models, constraints

AACSB: Analytical thinking

9) When using the graphical method, only one of the four quadrants of an xy-axis needs to be drawn.

Answer: TRUE Diff: 1 Page Ref: 37

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical linear programming

AACSB: Analytical thinking

10) Linear programming models exhibit linearity among all constraint relationships and the objective function.

Answer: TRUE Diff: 1 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems Keywords: properties of linear prog models, linearity, proportionality

AACSB: Analytical thinking

11) The equation 8xy = 32 satisfies the proportionality property of linear programming.

Answer: FALSE Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: graphical solution, proportionality

AACSB: Analytical thinking

12) Typically, finding a corner point for the feasible region involves solving a set of three simultaneous equations.

Answer: FALSE Diff: 2 Page Ref: 43

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, extreme points, feasible region

AACSB: Analytical thinking

13) Objective functions in linear programs always minimize costs.

Answer: FALSE Diff: 2 Page Ref: 32

Section Heading: Model Formulation

Keywords: properties of linear programming models, objective function

14) The feasible solution area contains infinite solutions to the linear program.

Answer: TRUE Diff: 1 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models Keywords: properties of linear programming models, feasible solution area

AACSB: Analytical thinking

15) There is exactly one optimal solution point to a linear program.

Answer: FALSE Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems Keywords: properties of linear programming models, optimal solution pt

AACSB: Analytical thinking

16) The following equation represents a resource constraint for a maximization problem: $X + Y \ge 20$.

Answer: FALSE Diff: 2 Page Ref: 34

Section Heading: A Maximization Model Example

Keywords: properties of linear programming models, constraints

AACSB: Analytical thinking

17) The optimal solution for a graphical linear programming problem is the corner point that is the farthest from the origin.

Answer: FALSE Diff: 2 Page Ref: 40

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: feasibility, constraints AACSB: Analytical thinking

18) A minimization model of a linear program contains only surplus variables.

Answer: FALSE
Diff: 1 Page Ref: 53

Section Heading: A Minimization Model Example

Keywords: properties of linear programming models, surplus variables

AACSB: Analytical thinking

19) In the graphical approach, simultaneous equations may be used to solve for the optimal solution

point.

Answer: TRUE Diff: 2 Page Ref: 43

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution AACSB: Analytical thinking

20) Slack variables are only associated with maximization problems.

Answer: FALSE Diff: 2 Page Ref: 45

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, slack variables

21) Surplus variables are only associated with minimization problems.

Answer: FALSE Diff: 2 Page Ref: 53

Section Heading: A Minimization Model Example Keywords: graphical solution, surplus variable

AACSB: Analytical thinking

22) If the objective function is parallel to a constraint, the constraint is infeasible.

Answer: FALSE Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: graphical solution AACSB: Analytical thinking

23) Multiple optimal solutions occur when constraints are parallel to each other.

Answer: FALSE Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: graphical solution AACSB: Analytical thinking

24) Graphical solutions to linear programming problems have an infinite number of possible objective

function lines. Answer: TRUE Diff: 2 Page Ref: 40

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, objective function line

AACSB: Analytical thinking

25) The first step in formulating a linear programming model is to define the objective function.

Answer: FALSE Diff: 2 Page Ref: 32

Section Heading: Introduction

Keywords: linear programming problems, formulation

AACSB: Analytical thinking

26) A linear programming problem requires a choice between alternative courses of action.

Answer: TRUE Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: linear programming problems, formulation

AACSB: Application of knowledge

27) The term *continuous* is synonymous with *divisible* in the context of linear programming.

Answer: TRUE Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: linear programming problems, formulation

AACSB: Application of knowledge

28) Linear programming problems can model decreasing marginal returns.
Answer: FALSE
Diff: 2 Page Ref: 57
Section Heading: Characteristics of Linear Programming Problems Keywords: linear programming problems, formulation
AACSB: Application of knowledge
AACSB. Application of knowledge
29) are mathematical symbols representing levels of activity.
Answer: Decision variables
Diff: 1 Page Ref: 32
Section Heading: Model Formulation
Keywords: decision variables, model formulation
AACSB: Analytical thinking
30) A is a linear relationship representing a restriction on decision making.
Answer: constraint
Diff: 1 Page Ref: 32
Section Heading: Model Formulation
Keywords: constraint, model formulation
AACSB: Analytical thinking
31) If at least one constraint in a linear programming model is violated, the solution is said to be
Answer: infeasible
Diff: 1 Page Ref: 55
Section Heading: Irregular Types of Linear Programming Problems
Keywords: constraint, infeasible solution
AACSB: Analytical thinking
32) A graphical solution is limited to solving linear programming problems with decision
variables.
Answer: two
Diff: 1 Page Ref: 36
Section Heading: Graphical Solutions of Linear Programming Models
Keywords: graphical solution
AACSB: Analytical thinking
33) The solution area is an area bounded by the constraint equations.
Answer: feasible
Diff: 1 Page Ref: 39
Section Heading: Graphical Solutions of Linear Programming Models
Keywords: graphical solution
AACSB: Analytical thinking
34) Multiple optimal solutions can occur when the objective function line is to a constraint line.
Answer: parallel
Diff: 2 Page Ref: 45
Section Heading: Graphical Solutions of Linear Programming Models
Keywords: graphical solution, multiple optimal solutions
AACSB: Analytical thinking

35) When a maximization problem is	, the objective function can increase indefinitely without
reaching a maximum value.	
Answer: unbounded	
Diff: 2 Page Ref: 56	
Section Heading: Irregular Types of Linear Progra	amming Problems
Keywords: graphical solution, unbounded proble	
AACSB: Analytical thinking	
36) The best feasible solution is	
Answer: optimal	
Diff: 1 Page Ref: 41	
Section Heading: Graphical Solutions of Linear Pr	rogramming Models
Keywords: optimal solutions	
AACSB: Analytical thinking	
37) In a constraint, the variable repr	resents unused resources.
Answer: slack	
Diff: 1 Page Ref: 45	
Section Heading: Graphical Solutions of Linear Pr	rogramming Models
Keywords: graphical solution, surplus variable	
AACSB: Analytical thinking	
38) is the difference between the lef	t- and right-hand sides of a greater than or equal to
constraint.	
Answer: Surplus	
Diff: 1 Page Ref: 53	
Section Heading: A Minimization Model Example	e
Keywords: surplus	
AACSB: Analytical thinking	
39) If the objective function is parallel to a con	nstraint, the linear program could have
Answer: multiple optimal solutions	
Diff: 2 Page Ref: 45	
Section Heading: Graphical Solutions of Linear Pr	
Keywords: graphical solutions, multiple optimal	solutions
AACSB: Analytical thinking	
40) Corner points on the boundary of the feas	sible solution area are called points.
Answer: extreme	
Diff: 1 Page Ref: 42	
Section Heading: Graphical Solutions of Linear Pr	rogramming Models
Keywords: feasibility, constraints	
AACSB: Analytical thinking	
41) are at the endpoints of the const	raint line segment that the objective function parallels.
Answer: Alternate optimal solutions	
Diff: 3 Page Ref: 55	
Section Heading: Irregular Types of Linear Progra	
Keywords: alternative optimal solutions, multiple	e optimal solutions
AACSB: Analytical thinking	

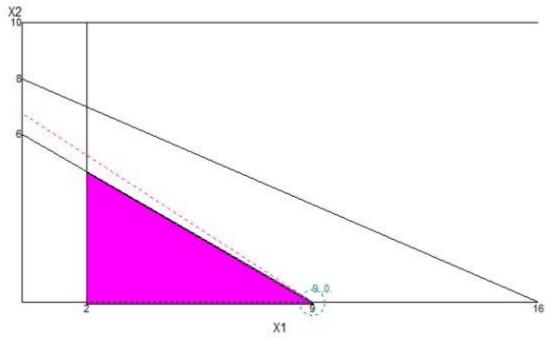
42) The	_ step in formulating a linear programming model is to define the decision variables.
Answer: first	
Diff: 1 Page Re	
	A Maximization Model Example
AACSB: Analytic	programming, formulation ral thinking
43) The manager	ment scientist constructed a linear program to help the alchemist maximize his gold
production prod	cess. The computer model chugged away for a few minutes and returned an answer of
infinite profit., v	which is what might be expected from a(n) problem.
Answer: unbou	nded
Diff: 1 Page Re	
_	Irregular Types of Linear Programming Problems
Keywords: unbou AACSB: Analytic	
THICOD. THURY HE	ui uiiiwiig
44) The	_ property of linear programming models indicates that the rate of change, or slope, of
the objective fur	nction or a constraint is constant.
	rtionality or linearity
Diff: 2 Page Re	
_	Characteristics of Linear Programming Problems erties of linear programming models, certainty
AACSB: Analytic	
45) The objective	e function 3x + 2y + 4xy violates the assumption of
Answer: propor	
Diff: 2 Page Re	
	Characteristics of Linear Programming Problems programming properties
AACSB: Applicat	
• •	Ç
this Sunday. The She sleeps well of she will need the Answer: certain	
Diff: 2 Page Re	
_	Characteristics of Linear Programming Problems programming properties
AACSB: Applicat	
11	
	procurement division works with their linear programming algorithm to secure
_	soline for the coming year. After twenty minutes of thinking, the computer suggests that
•	8125 contracts with their suppliers. This value illustrates the assumption of in
linear programn	
Answer: divisib	bility or continuous
_	Characteristics of Linear Programming Problems
_	programming properties
AACSB: Applicat	

48) Solve the following graphically:

Max
$$z =$$
 $3x_1 + 4x_2$
s.t. $x_1 + 2x_2 \le 16$
 $2x_1 + 3x_2 \le 18$
 $x_1 \ge 2$
 $x_2 \le 10$
 $x_1, x_2 \ge 0$

What are the optimal values of x_1 , x_2 , and z?

Answer: $x_1 = 9$, $x_2 = 0$, z = 27



Diff: 3 Page Ref: 37-41

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, simultaneous solution

49) A novice business analyst develops the following model to determine the optimal combination of socks and underwear to take on his next business trip. The model is as follows:

Maximize 5S+7U

subject to:

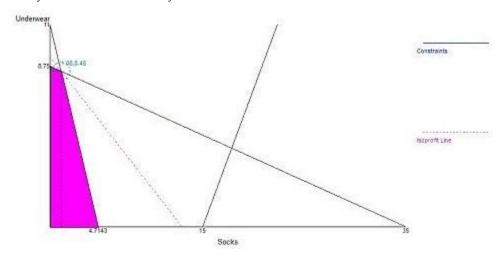
3S - 2U≤ 45

 $7S + 3U \le 33$

 $2S + 8U \le 70$

Solve this problem graphically and determine how many of each item the analyst should pack.

Answer: The optimal solution lies at the point representing 1.08 socks and 8.48 underwear. I suppose this is why I referred to the analyst as a novice.



Corner points and the objective function value in (Socks, Underwear) order are:

Z(0,0)=0

Z(4.714,0)=23.57

Z(0,8.75)=61.25

Z(1.08. 8.48)=64.76 optimal

Diff: 3 Page Ref: 37-41

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution AACSB: Analytical thinking

50) Nathan enters the final exam period needing to pull off a miracle to pass his three toughest classes, Healthy Life Choices, Success Central, and Walking Fitness. Naturally he would also prefer to expend as little effort as possible doing so and as luck would have it, he knows a guy that can help optimize his time and GPA using the magic of management science. The model they develop is built around the notion of time spent studying and doing all the assignments he has neglected throughout the semester. The model is as follows, where S represents time spent studying (in minutes) and A represents time spent making up assignments (also in minutes).

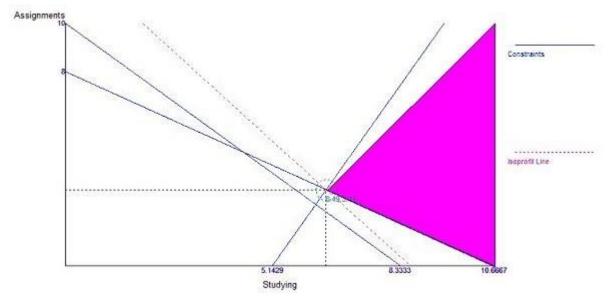
Maximize Z = 6S + 4A subject to:

HLC $12S+10A \ge 100$ SC $6S+8A \ge 64$ W $7S-3A \ge 36$

Graphing was never one of Nathan's strengths, so it is up to you to develop a graphical solution to his problem and advise him on how much time should be invested in studying and how much time should be spent catching up on assignments.

Answer: The two corner points meriting investigation are (in (Studying, Assignments) order) Z(10.67,0)=64

Z(6.48,3.13)=51.46 the optimal solution



So, 6 minutes of studying and 3 minutes of working on assignments was all that was required for my first born to successfully complete his first semester with something other than a 0.0 GPA. Sad, but true.

Diff: 2 Page Ref: 51-52

Section Heading: A Minimization Model Example

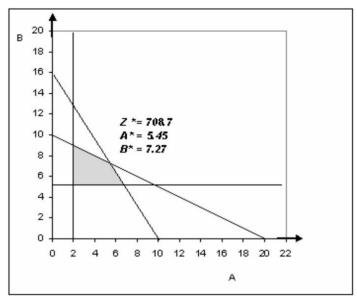
Keywords: graphical solution AACSB: Analytical thinking

51) Consider the following linear program:

MAX
$$Z = 60A + 50B$$

s.t. $10A + 20B \le 200$
 $8A + 5B \le 80$
 $A \ge 2$
 $B \ge 5$

Solve this linear program graphically and determine the optimal quantities of A, B, and the value of Z. Answer: Solution shown below.



Diff: 2 Page Ref: 37-41

Section Heading: Graphical Solutions of Linear Programming Models

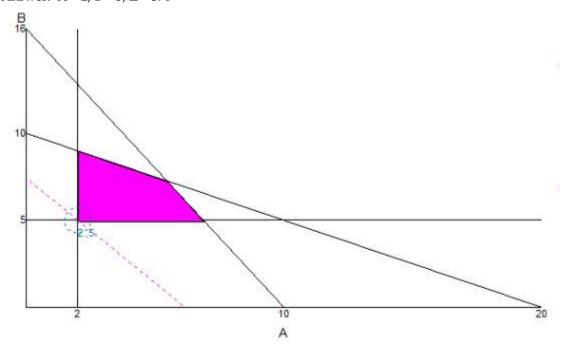
Keywords: graphical linear programming

52) Consider the following linear program:

MIN
$$Z = 60A + 50B$$

s.t. $10A + 20B \le 200$
 $8A + 5B \le 80$
 $A \ge 2$
 $B \ge 5$

Solve this linear program graphically and determine the optimal quantities of A, B, and the value of Z. Answer: A = 2, B = 5, Z = 370

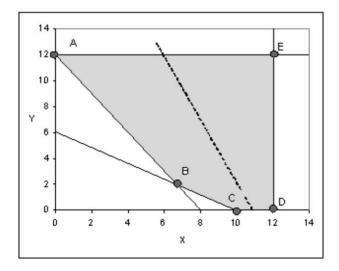


Diff: 2 Page Ref: 37-41

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical linear programming

53) A graphical representation of a linear program is shown below. The shaded area represents the feasible region, and the dashed line in the middle is the slope of the objective function.



If this is a maximization, which extreme point is the optimal solution?

Answer: E

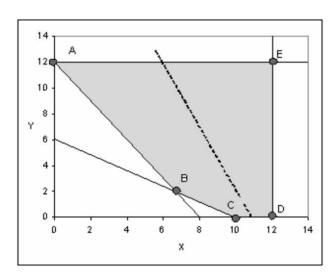
Diff: 1 Page Ref: 42

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, extreme points, feasible region

AACSB: Analytical thinking

54) A graphical representation of a linear program is shown below. The shaded area represents the feasible region, and the dashed line in the middle is the slope of the objective function.



If this is a minimization, which extreme point is the optimal solution?

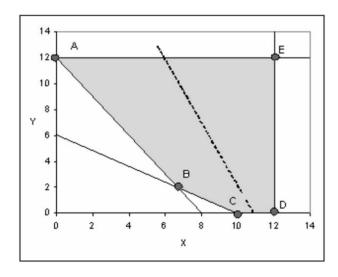
Answer: A

Diff: 2 Page Ref: 42

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, extreme points, feasible region

55) A graphical representation of a linear program is shown below. The shaded area represents the feasible region, and the dashed line in the middle is the slope of the objective function.



What would the be the new slope of the objective function if multiple optimal solutions occurred along line segment AB?

Answer: -3/2 Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: graphical solution, multiple optimal solutions

AACSB: Analytical thinking

56) Consider the following linear programming problem:

Max Z = \$15x + \$20ySubject to: $8x + 5y \le 40$

 $0.4x + y \ge 4$

 $x, y \ge 0$

Determine the values for x and y that will maximize revenue. Given this optimal revenue, what is the amount of slack associated with the first constraint?

Answer: x = 0, y = 8, revenue = \$160, $s_1 = 0$

Diff: 2 Page Ref: 46

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, slack variables

57) Given this model

Maximize Z = 6S + 4A

subject to:

 $12S + 10A \ge 100$

 $6S + 8A \ge 64$

7S - 3A ≥ 36

What is the optimal solution and the surplus associated with the first constraint?

Answer: The optimal solution lies at S = 6.48 and A = 3.13.

The s1 variable is 9.1892 Diff: 2 Page Ref: 52

Section Heading: A Minimization Model Example

Keywords: surplus

AACSB: Analytical thinking

58) The poultry farmer decided to make his own chicken scratch by combining alfalfa and corn in rail car quantities. A rail car of corn costs \$400 and a rail car of alfalfa costs \$200. The farmer's chickens have a minimum daily requirement of vitamin K (500 milligrams) and iron (400 milligrams), but it doesn't matter whether those elements come from corn, alfalfa, or some other grain. A unit of corn contains 150 milligrams of vitamin K and 75 milligrams of iron. A unit of alfalfa contains 250 milligrams of vitamin K and 50 milligrams of iron. Formulate the linear programming model for this situation.

Answer:

Min Z = \$4005C + \$200A

Subject to: $150C + 250A \ge 500$

 $75C + 50A \ge 400$

 $C, A \ge 0$

Diff: 3 Page Ref: 34-35

Section Heading: A Maximization Model Example

Keywords: constraint, model formulation

AACSB: Analytical thinking

59) Consider the following linear programming problem:

MIN $Z = 3x_1 + 2x_2$

Subject to: $2x_1 + 3x_2 \ge 12$

 $5x_1 + 8x_2 \ge 37$

 $x_1, x_2 \ge 0$

What is minimum cost and the value of x_1 and x_2 at the optimal solution?

Answer: 9.25 at $x_1 = 0$ and $x_2 = 4.625$

Diff: 3 Page Ref: 42

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: minimization problem AACSB: Analytical thinking

60) Consider the following linear programming problem:

MIN Z = $3x_1 + 2x_2$ Subject to: $2x_1 + 3x_2 \ge 12$ $5x_1 + 8x_2 \ge 37$ $x_1, x_2 \ge 0$

What is minimum cost and the value of x_1 and x_2 at the optimal solution?

Answer: 9.25 at $x_1 = 0$ and $x_2 = 4.625$

Diff: 3 Page Ref: 42

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: minimization problem AACSB: Analytical thinking

61) Ponder the following linear programming problem:

MIN Z = $3x_1 + 8x_2$ Subject to: $3x_1 + 4x_2 \ge 52$ $3x_1 + 4x_2 \ge 38$ $x_1, x_2 \ge 0$

What is minimum cost and the value of x_1 and x_2 at the optimal solution?

Answer: 52 at $x_1 = 17.33$ and $x_2 = 0.0$

Diff: 3 Page Ref: 42

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: minimization problem AACSB: Analytical thinking

62) The international man of mystery knew the finest haberdashers the world over and constantly sought to expand his dazzling array of fine suits, ties, and cufflinks. Closet space was at a premium however, so purchases were carefully weighed. Each suit provides 23 units of dazzlement, each tie 14, and a set of cufflinks is worth an easy 8. A suit takes up 0.5 cubic feet of closet space and \$900 of budget. A tie costs \$135 and cufflinks cost \$100 per set. Cufflinks are tiny — even in the original box, they take up only .01 cubic feet while ties occupy a lusty .25 cubic feet. He has budgeted \$12,000 for clothes on this trip and has 20 cubic feet of closet space left to fill.

Formulate an objective function and constraints to model this situation.

Answer: Max Dazzlement = 23S + 14T + 8C

subject to:

 $900S + 135T + 100C \le 12,000$ $0.5S + 0.25T + 0.01C \le 20$

Diff: 3 Page Ref: 34

Section Heading: A Maximization Model Example

Keywords: linear programming formulation

63) Ponder the following linear programming problem:

Max Z = $5x_1 + 6x_2$ Subject to: $3x_1 + 4x_2 \le 76$ $8x_1 + 9x_2 \le 123$ $3x_1 + 3x_2 \le 56$ $x_1, x_2 \ge 0$

What is the optimal solution point?

Answer: 12.31 at x_1 and 2.72 at x_2 for an objective function value of 77.897

Diff: 3 Page Ref: 40

Section Heading: A Maximization Model Example

Keywords: optimal solutions AACSB: Analytical thinking

64) List the four properties of linear programming models and provide an example of a violation of each. Answer: Properties and brief discussions are contained in the table. Counter examples will vary.

Proportionality	The slope of a constraint or objective function is	
	constant. There are no increasing or decreasing	
	marginal returns on either.	
Additivity	Strictly linear functions - there are no interaction	
	effects among decision variables.	
Divisibility	Non-integer values of decision variables are OK.	
Certainty	All model parameters are known exactly.	

Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: linear programming properties AACSB: Application of knowledge

65) Formulate all elements of linear program to model your university effort. Include a narrative that explains each of the components.

Answer: Answers will vary, perhaps dramatically. A noble objective function would seek to maximize a GPA or minimize total cost. Constraints would likely include budget, hours in a day, financial capital, conflicts with social endeavors, and others.

Diff: 2 Page Ref: 32

Section Heading: Model Formulation Keywords: linear programming properties

AACSB: Application of knowledge

66) Consider the following linear programming problem:

MIN Z =
$$10x_1 + 20x_2$$

Subject to: $x_1 + x_2 \ge 12$
 $2x_1 + 5x_2 \ge 40$
 $x_2 \le 13$
 $x_1, x_2 \ge 0$

At the optimal solution, what is the value of surplus associated with constraint 1 and constraint 3, respectively?

Answer: constraint 1: (0 surplus), constraint 2: (7.667 surplus)

Diff: 2 Page Ref: 50-54

Section Heading: A Minimization Model Example

Keywords: graphical solution AACSB: Analytical thinking

67) Given this set of constraints, for what objective function is the point x=5, y=3 in the feasible region?

s.t
$$3x + 6y \le 30$$

 $10x + 10y \le 60$
 $10x + 15y \le 90$

Answer: No objective function can move that point into the feasible region.

Diff: 2 Page Ref: 40

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: feasibility, constraints AACSB: Analytical thinking

68) Consider the following linear programming problem:

MIN
$$Z = 2x_1 + 3x_2$$

Subject to: $x_1 + 2x_2 \le 20$
 $5x_1 + x_2 \le 40$
 $4x_1 + 6x_2 \le 60$
 $x_1, x_2 \ge 0$

What is the optimal solution?

Answer: Multiple optimal solutions exist between the extreme point (0,10) and (6.92,5.38) along the line with a slope of -2/3.

Diff: 2 Page Ref: 50-51

Section Heading: A Minimization Model Example

Keywords: graphical solution, multiple optimal solutions

69) A company producing a standard line and a deluxe line of dishwashers has the following time requirements (in minutes) in departments where either model can be processed.

	Standard	Deluxe
Stamping	3	6
Motor installation	10	10
Wiring	10	15

The standard models contribute \$20 each and the deluxe \$30 each to profits. Because the company produces other items that share resources used to make the dishwashers, the stamping machine is available only 30 minutes per hour, on average. The motor installation production line has 60 minutes available each hour. There are two lines for wiring, so the time availability is 90 minutes per hour.

Let x = number of standard dishwashers produced per hour y = number of deluxe dishwashers produced per hour

Write the formulation for this linear program.

Answer: Max 20x + 30y

s.t $3x + 6y \le 30$

 $10x + 10y \le 60$

 $10x + 15y \le 90$

Diff: 2 Page Ref: 34-35

Section Heading: A Maximization Model Example Keywords: formulation, objective function, constraints

AACSB: Analytical thinking

70) In a linear programming problem, the binding constraints for the optimal solution are:

$$5x_1 + 3x_2 \le 30$$

$$2x_1 + 5x_2 \le 20$$

As long as the slope of the objective function stays between _____ and _____, the current optimal solution point will remain optimal.

Answer: -5/3, -2/5 Diff: 3 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: optimal solution, solution interpretation, slope

71) In a linear programming problem, the binding constraints for the optimal solution are:

$$5x_1 + 3x_2 \le 30$$
$$2x_1 + 5x_2 \le 20$$

Which of these objective functions will lead to the same optimal solution?

- A) $2x_1 + 1x_2$
- B) $7x_1 + 8x_2$
- C) $80x_1 + 60x_2$
- D) $25x_1 + 15x_2$

Answer: D

Diff: 3 Page Ref: 40

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: optimal solution, solution interpretation, slope

AACSB: Analytical thinking

- 72) Decision variables:
- A) measure the objective function.
- B) measure how much or how many items to produce, purchase, hire, etc.
- C) always exist for each constraint.
- D) measure the values of each constraint.

Answer: B

Diff: 2 Page Ref: 32

Section Heading: Model Formulation

Keywords: decision variables AACSB: Analytical thinking

- 73) In a linear programming problem, a valid objective function can be represented as:
- A) Max Z = 5xy
- B) Max $Z 5x^2 + 2y^2$
- C) Max 3x + 3y + 1/3z
- D) Min $(x_1 + x_2) / x_3$

Answer: C

Diff: 3 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: objective function AACSB: Analytical thinking

- 74) Which of the following could not be a linear programming problem constraint?
- A) $1A + 2B \neq 3$
- B) 1A + 2B = 3
- C) $1A + 2B \le 3$
- D) $1A + 2B \ge 3$

Answer: A

Diff: 2 Page Ref: 34-35

Section Heading: A Maximization Model Example

Keywords: formulation, constraints

75) Which of the following could be a linear programming objective function?

A)
$$Z = 1A + 2BC + 3D$$

B)
$$Z = 1A + 2B + 3C + 4D$$

C)
$$Z = 1A + 2B / C + 3D$$

D)
$$Z = 1A + 2B^2 + 3D$$

Answer: B

Diff: 2 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: objective function AACSB: Analytical thinking

76) The production manager for the Coory soft drink company is considering the production of two kinds of soft drinks: regular (R) and diet (D). Two of her limited resources are production time (8 hours = 480 minutes per day) and syrup (1 of the ingredients), limited to 675 gallons per day. To produce a regular case requires 2 minutes and 5 gallons of syrup, while a diet case needs 4 minutes and 3 gallons of syrup. Profits for regular soft drink are \$3.00 per case and profits for diet soft drink are \$2.00 per case. What is the objective function?

A) MAX \$2R + \$4D

B) MAX \$3R + \$2D

C) MAX \$3D + \$2R

D) MAX \$4D + \$2R

Answer: B

Diff: 2 Page Ref: 34

Section Heading: A Maximization Model Example

Keywords: formulation, objective function

AACSB: Analytical thinking

77) The production manager for the Coory soft drink company is considering the production of two kinds of soft drinks: regular (R) and diet(D). Two of the limited resources are production time (8 hours = 480 minutes per day) and syrup (1 of the ingredients), limited to 675 gallons per day. To produce a regular case requires 2 minutes and 5 gallons of syrup, while a diet case needs 4 minutes and 3 gallons of syrup. Profits for regular soft drink are \$3.00 per case and profits for diet soft drink are \$2.00 per case. What is the time constraint?

A) $2D + 4R \le 480$

B) $2R + 3D \le 480$

C) $3R + 2D \le 480$

D) $2R + 4D \le 480$

Answer: D

Diff: 2 Page Ref: 34-35

Section Heading: A Maximization Model Example

Keywords: formulation, constraints

78) The property of linear programming models indicates that the rate of change or slope of the
objective function or a constraint is constant.
A) additive
B) divisibility
C) certainty
D) proportionality
Answer: D
Diff: 2 Page Ref: 57
Section Heading: Characteristics of Linear Programming Problems
Keywords: properties of linear programming models
AACSB: Analytical thinking
79) The property of linear programming models indicates that the values of all the model
parameters are known and are assumed to be constant.
A) additive
B) divisibility
C) certainty
D) proportionality
Answer: C
Diff: 2 Page Ref: 57
Section Heading: Characteristics of Linear Programming Problems
Keywords: properties of linear programming models
AACSB: Analytical thinking
80) The region that satisfies all of the constraints in a graphical linear programming problem is called the:
A) region of optimality.
B) feasible solution space.
C) region of non-negativity.
D) optimal solution space.
Answer: B
Diff: 1 Page Ref: 39
Section Heading: Graphical Solutions of Linear Programming Models
Keywords: graphical solution, feasibility
AACSB: Analytical thinking
81) In the formulation of a \geq constraint:
A) a surplus variable is subtracted.
B) a surplus variable is added.
C) a slack variable is subtracted.
D) a slack variable is added.
Answer: A
Diff: 1 Page Ref: 53
Section Heading: A Minimization Model Example
Keywords: surplus
AACSB: Analytical thinking

- 82) Which of the following statements is not true?
- A) An infeasible solution violates all constraints.
- B) A feasible solution point does not have to lie on the boundary of the feasible solution.
- C) A feasible solution satisfies all constraints.
- D) An optimal solution satisfies all constraints.

Answer: A

Diff: 2 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, feasibility

AACSB: Analytical thinking

- 83) A hot dog manufacturer wishes to minimize the cost in dollars of producing a low-cost niched product while meeting the dietary guidelines for protein and sodium. Once the model has been run, the surplus variable in the sodium constraint has a value of 1300 milligrams. The best interpretation of this outcome is:
- A) The value of the sodium in a hot dog is 1300.
- B) The amount of sodium in a single hot dog should be 1300 milligrams.
- C) The minimum cost hot dog has 1300 milligrams more sodium than required.
- D) A hot dog should have at least 1300 milligrams of sodium.

Answer: C

Diff: 2 Page Ref: 53

Section Heading: A Minimization Model Example

Keywords: surplus

AACSB: Analytical thinking

- 84) Which of these statements is best?
- A) An unbounded problem is also infeasible.
- B) An infeasible problem is also unbounded.
- C) An unbounded problem has feasible solutions.
- D) An infeasible problem has unbounded solutions.

Answer: C

Diff: 2 Page Ref: 56

Section Heading: Irregular Types of Linear Programming Problems

Keywords: infeasible problem, infeasible solution

AACSB: Analytical thinking

- 85) The optimal solution to a linear programming model that has been solved using the graphical approach:
- A) is typically located at the origin.
- B) must be below and on the left side of all constraint lines.
- C) must be above and the right of all constraint lines.
- D) is typically at some corner of the feasible region.

Answer: D

Diff: 1 Page Ref: 40

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: solution

- 86) Without satisfying the non-negativity constraint, a solution that satisfies all the other constraints of a linear programming problem is called:
- A) feasible.
- B) infeasible.
- C) semi-feasible.
- D) optimal.

Answer: B

Diff: 3 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, feasibility

AACSB: Analytical thinking

87) An intern sets up a linear program to optimize the use of paper products in the men's washroom. The system of equations he develops is:

```
Max 2T + 3S + 4ST

s.t 3T + 6S \le 40

10T + 10S \le 66

10T + 15S \le 99
```

His mentor studies the model, frowns, and admonishes the intern for violating which of the following properties of linear programming models?

- A) divisibility
- B) proportionality
- C) certainty
- D) additivity

Answer: D

Diff: 1 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: additivity AACSB: Analytical thinking

- 88) Which of the following is not a typical characteristic of a linear programming problem?
- A) Restrictions exist.
- B) A choice among alternatives is required.
- C) The problem can be solved graphically.
- D) The problem has an objective.

Answer: C

Diff: 1 Page Ref: 57

Section Heading: Characteristics of Linear Programming Problems

Keywords: graphical solution AACSB: Analytical thinking

89) The production manager for the Coory soft drink company is considering the production of two kinds of soft drinks: regular and diet. Two of her limited resources are production time (8 hours = 480 minutes per day) and syrup (1 of the ingredients), limited to 675 gallons per day. To produce a regular case requires 2 minutes and 5 gallons of syrup, while a diet case needs 4 minutes and 3 gallons of syrup. Profits for regular soft drink are \$3.00 per case and profits for diet soft drink are \$2.00 per case. Which of the following is not a feasible production combination?

A) 90R and 75D

B) 135R and 0D

C) 75R and 90D

D) 40R and 100D

Answer: C

Diff: 3 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, feasibility

AACSB: Analytical thinking

90) The production manager for the Coory soft drink company is considering the production of two kinds of soft drinks: regular and diet. Two of her limited resources are production time (8 hours = 480 minutes per day) and syrup (1 of the ingredients), limited to 675 gallons per day. To produce a regular case requires 2 minutes and 5 gallons of syrup, while a diet case needs 4 minutes and 3 gallons of syrup. Profits for regular soft drink are \$3.00 per case and profits for diet soft drink are \$2.00 per case. What are the optimal daily production quantities of each product and the optimal daily profit?

A) R = 75, D = 90, Z = \$405

B) R = 135, D = 0, Z = \$405

C) R = 90, D = 75, Z = \$420

D) R = 40, D = 100, Z = \$320

Answer: C

Diff: 3 Page Ref: 42

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution AACSB: Analytical thinking

- 91) ______ is used to analyze changes in model parameters.
- A) Optimal solution
- B) Feasible solution
- C) Sensitivity analysis
- D) A slack variable

Answer: C

Diff: 2 Page Ref: 45

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: sensitivity analysis AACSB: Analytical thinking

- 92) Cully Furniture buys two products for resale: big shelves (B) and medium shelves (M). Each big shelf costs \$500 and requires 100 cubic feet of storage space, and each medium shelf costs \$300 and requires 90 cubic feet of storage space. The company has \$75,000 to invest in shelves this week, and the warehouse has 18,000 cubic feet available for storage. Profit for each big shelf is \$300 and for each medium shelf is \$150. Which of the following is not a feasible purchase combination?
- A) 100 big shelves and 82 medium shelves
- B) 150 big shelves and 0 medium shelves
- C) 100 big shelves and 100 medium shelves
- D) 100 big shelves and 0 medium shelves

Answer: C

Diff: 3 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: formulation, feasibility AACSB: Analytical thinking

- 93) Cully Furniture buys two products for resale: big shelves (B) and medium shelves (M). Each big shelf costs \$500 and requires 100 cubic feet of storage space, and each medium shelf costs \$300 and requires 90 cubic feet of storage space. The company has \$75,000 to invest in shelves this week, and the warehouse has 18,000 cubic feet available for storage. Profit for each big shelf is \$300 and for each medium shelf is \$150. What is the maximum profit?
- A) \$35,000
- B) \$45,000
- C) \$55,000
- D) \$65,000

Answer: B

Diff: 3 Page Ref: 41

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution AACSB: Analytical thinking

- 94) Cully Furniture buys two products for resale: big shelves (B) and medium shelves (M). Each big shelf costs \$500 and requires 100 cubic feet of storage space, and each medium shelf costs \$300 and requires 90 cubic feet of storage space. The company has \$75,000 to invest in shelves this week, and the warehouse has 18,000 cubic feet available for storage. Profit for each big shelf is \$300 and for each medium shelf is \$150. In order to maximize profit, how many big shelves (B) and how many medium shelves (M) should be purchased?
- A) B = 90, M = 75
- B) B = 150, M = 0
- C) B = 0, M = 200
- D) B = 100, M = 100

Answer: B

Diff: 3 Page Ref: 41

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution AACSB: Analytical thinking

- 95) The theoretical limit on the number of constraints that can be handled by a linear programming problem is:
- A) 2.
- B) 3.
- C) 4.
- D) unlimited.

Answer: D

Diff: 1 Page Ref: 32

Section Heading: Model Formulation

Keywords: constraints AACSB: Analytical thinking

96) Consider the following maximization problem.

$$MAX z = x + 2y$$
 s.t.

$$2x + 3y \le 6$$
$$5x + 6y \le 30$$
$$y \ge 1$$

The optimal solution:

- A) occurs where x = 4.67 and y = 1.11.
- B) occurs where x = 0 and y = 2.
- C) occurs where x = 6 and y = 0.
- D) results in an objective function value of 12.

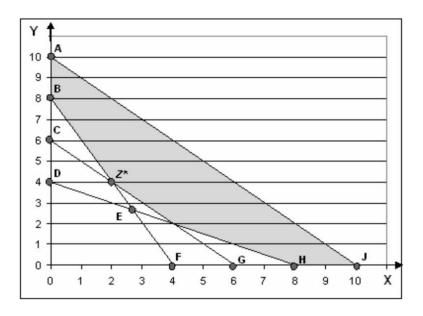
Answer: B

Diff: 1 Page Ref: 42

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, extreme points, feasible region

The following is a graph of a linear programming problem. The feasible solution space is shaded, and the optimal solution is at the point labeled Z^* .



- 97) This linear programming problem is a(n):
- A) maximization problem.
- B) minimization problem.
- C) irregular problem.
- D) cannot tell from the information given

Answer: B

Diff: 1 Page Ref: 50

Section Heading: A Minimization Model Example

Keywords: graphical solution AACSB: Analytical thinking

- 98) The equation for constraint DH is:
- A) $4X + 8Y \ge 32$.
- B) $8X + 4Y \ge 32$.
- C) $X + 2Y \ge 8$.
- D) $2X + Y \ge 8$.

Answer: C

Diff: 3 Page Ref: 50

Section Heading: A Minimization Model Example

Keywords: graphical solution, constraints

99) Which of the following points is *not* feasible?

A) A

B) B

C) H

D) G

Answer: D

Diff: 1 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, feasible point

AACSB: Analytical thinking

100) Which line is represented by the equation $2X + Y \ge 8$?

A) BF

B) CG

C) DH

D) AJ

Answer: A

Diff: 2 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: graphical solution, constraints

AACSB: Analytical thinking

101) Which of the following constraints has a surplus greater than 0?

A) BF

B) CG

C) DH

D) AJ

Answer: C

Diff: 2 Page Ref: 53-54

Section Heading: A Minimization Model Example

Keywords: graphical solution, constraints

AACSB: Analytical thinking

102) The constraint AJ:

A) is a binding constraint.

B) has no surplus.

C) does not contain feasible points.

D) contains the optimal solution.

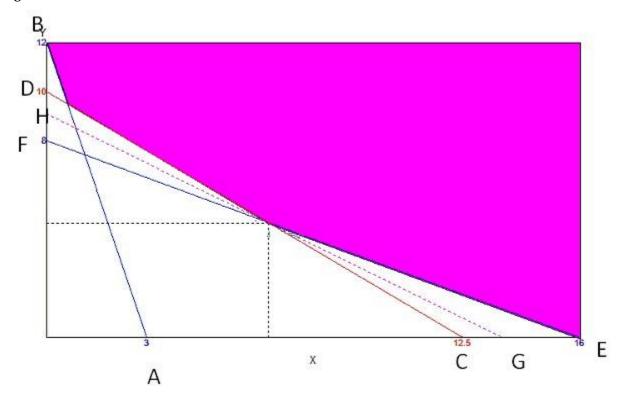
Answer: B

Diff: 3 Page Ref: 53-54

Section Heading: A Minimization Model Example

Keywords: graphical solution, constraints

Figure 2



- 103) Consider the optimization problem represented by this graph. Which of the following statements is best?
- A) This is a maximization problem with a feasible solution.
- B) This is a maximization problem with no feasible solution.
- C) This is a minimization problem with a feasible solution.
- D) This is a minimization problem with no feasible solution.

Answer: C

Diff: 1 Page Ref: 54

Section Heading: A Minimization Model Example

Keywords: graphical solution, feasibility

AACSB: Analytical thinking

104) Line segment GH represents the objective function. Which constraint has surplus?

A) AB

B) CD

C) EF

D) none of the constraints has surplus

Answer: A

Diff: 2 Page Ref: 53

Section Heading: A Minimization Model Example Keywords: graphical solution, surplus variable

105) What is the equation for the constraint AB?

A) $3X + 12Y \ge 15$

B) $X + 4Y \ge 12$

C) $X + Y \ge 15$

D) $12X + 3Y \ge 36$

Answer: D

Diff: 3 Page Ref: 51

Section Heading: A Minimization Model Example

Keywords: graphical solution, constraints

AACSB: Analytical thinking

106) What is the equation for constraint EF?

A) $4X + 8Y \ge 64$

B) $4X + 8Y \ge 12$

C) $16X + 8Y \ge 24$

D) $16X + 8Y \ge 32$

Answer: A

Diff: 3 Page Ref: 51

Section Heading: A Minimization Model Example

Keywords: graphical solution, constraints

AACSB: Analytical thinking

107) Consider the optimization problem represented by this graph. The objective function is represented by line GH. Where is the optimal solution?

- A) the intersection of lines AB and EF
- B) the intersection of lines AB and CD
- C) the intersection of lines CD and EF
- D) the upper right corner of the shaded region

Answer: C

Diff: 1 Page Ref: 51

Section Heading: A Minimization Model Example Keywords: graphical solution, objective function line

AACSB: Analytical thinking

- 108) Consider the optimization problem represented by this graph. Line GH represents the objective function. Which of the following statements is best?
- A) This is a single optimal solution.
- B) All points along GH are optimal.
- C) All points on lines AB, CD and DE that touch the shaded region are optimal.
- D) All points in the shaded region are optimal

Answer: A

Diff: 1 Page Ref: 51

Section Heading: A Minimization Model Example

Keywords: graphical solution, multiple optimal solutions

- 109) In order for an optimization problem to have multiple optimal solutions:
- A) the objective function and one constraint must have the same y-intercept.
- B) the objective function and one constraint must have the same slope.
- C) two or more of the constraints must not have intersection points.
- D) two or more of the constraints must have the same slope.

Answer: B

Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: graphical solutions, multiple optimal solutions

AACSB: Analytical thinking

- 110) An optimization problem that has multiple optimal solutions:
- A) means that there are actually no optimal solutions.
- B) is reflected by the entire feasible region being optimal
- C) means that the surplus for a third constraint cannot be calculated.
- D) provides the decision-maker with increased flexibility.

Answer: D

Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: graphical solutions, multiple optimal solutions

AACSB: Analytical thinking

- 111) How would multiple optimal solutions typically appear on a graphical solution?
- A) a point
- B) a line
- C) a plane
- D) a cube

Answer: B

Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: graphical solutions, multiple optimal solutions

AACSB: Analytical thinking

- 112) Which of the following statements about infeasible problems is best?
- A) All of the possible solutions violate at least one constraint.
- B) All of the possible solutions violate all of the constraints.
- C) At least one of the possible solutions violates all of the constraints.
- D) At least one of the possible solutions violates at least one of the constraints.

Answer: A

Diff: 1 Page Ref: 56

Section Heading: Irregular Types of Linear Programming Problems

Keywords: infeasible problem, infeasible solution

- 113) Greg, a young entrepreneur, has developed an aggressive business plan and is presenting his profit projections on the popular show *Shark Tank* in hopes of securing some venture capital. He concludes his presentation with an LP model of his planned product mix, and is convinced he will seal the deal by demonstrating that his profits are limitless since his LP model is unbounded. What should the sharks tell him?
- A) "Limitless profits sound fantastic, here's a blank check."
- B) "Limitless profits are possible only in minimization models, and we want you to maximize profits."
- C) "Unlimited profits aren't possible. You must have made a mistake in your LP model."
- D) "Limitless profits are possible only in maximization models, and we want you to minimize profits."

Answer: C

Diff: 1 Page Ref: 56

Section Heading: Irregular Types of Linear Programming Problems

Keywords: unbounded AACSB: Analytical thinking

- 114) Multiple optimal solutions can occur when the objective function is _____ a constraint line.
- A) unequal to
- B) equal to
- C) perpendicular to
- D) parallel to

Answer: D

Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: irregular types of linear programming problems

AACSB: Analytical thinking

- 115) A slack variable:
- A) is the amount by which the left side of a \geq constraint is larger than the right side.
- B) is the amount by which the left side of a \leq constraint is smaller than the right side.
- C) is the difference between the left and right side of a constraint.
- D) exists for each variable in a linear programming problem.

Answer: B

Diff: 2 Page Ref: 44

Section Heading: Slack Variables Keywords: slack variables

116) The production manager for the Coory soft drink company is considering the production of two kinds of soft drinks: regular and diet. Two of her limited resources are production time (8 hours = 480 minutes per day) and syrup (1 of the ingredients), limited to 675 gallons per day. To produce a regular case requires 2 minutes and 5 gallons of syrup, while a diet case needs 4 minutes and 3 gallons of syrup. Profits for regular soft drink are \$3.00 per case and profits for diet soft drink are \$2.00 per case. For the production combination of 135 cases of regular and 0 cases of diet soft drink, which resources will not be completely used?

A) only time

B) only syrup

C) time and syrup

D) neither time nor syrup

Answer: A

Diff: 2 Page Ref: 46

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: slack variables AACSB: Analytical thinking

117) Cully Furniture buys two products for resale: big shelves (B) and medium shelves (M). Each big shelf costs \$500 and requires 100 cubic feet of storage space, and each medium shelf costs \$300 and requires 90 cubic feet of storage space. The company has \$75,000 to invest in shelves this week, and the warehouse has 18,000 cubic feet available for storage. Profit for each big shelf is \$300 and for each medium shelf is \$150. If the furniture company purchases no big shelves and 200 medium shelves, which of the two resources will be completely used (at capacity)?

A) investment money only

B) storage space only

C) investment money and storage space

D) neither investment money nor storage space

Answer: B

Diff: 2 Page Ref: 39

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: slack variables AACSB: Analytical thinking 118) Consider the following linear program:

MAX
$$z = 5x + 3y$$

s.t. $x - y \le 6$
 $x \le 1$

The optimal solution:

- A) is infeasible.
- B) occurs where x = 1 and y = 0.
- C) occurs where x = 0 and y = 1.
- D) results in an objective function value of 5.

Answer: D

Diff: 2 Page Ref: 40

Section Heading: Graphical Solutions of Linear Programming Models

Keywords: slack variables AACSB: Analytical thinking

- 119) The first step in solving a graphical linear programming model is to:
- A) plot the model constraints as equations on the graph and indicate the feasible solution area.
- B) plot the objective function and move this line out from the origin to locate the optimal solution point.
- C) solve simultaneous equations at each corner point to find the solution values at each point.
- D) determine which constraints are binding.

Answer: A

Diff: 1 Page Ref: 37

Section Heading: Graphical Solutions of Linear Programming Models Keywords: graphic solution, steps for solving a graphical linear prog model

AACSB: Analytical thinking

- 120) The optimal solution of a minimization problem is at the extreme point _____ the origin.
- A) farthest from
- B) closest to
- C) exactly at
- D) parallel to

Answer: B

Diff: 2 Page Ref: 51

Section Heading: A Minimization Model Example

Keywords: minimization problem AACSB: Analytical thinking

- 121) Multiple optimal solutions provide _____ flexibility to the decision maker.
- A) greater
- B) less
- C) greater or equal
- D) less or equal

Answer: A

Diff: 2 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: irregular types of linear programming problems

- 122) Which of the following special cases *does not* require reformulation of the problem in order to obtain a solution?
- A) unboundedness
- B) infeasibility
- C) alternate optimality
- D) Each one of these cases requires reformulation.

Answer: C

Diff: 3 Page Ref: 55

Section Heading: Irregular Types of Linear Programming Problems

Keywords: irregular types of linear programming problems

AACSB: Analytical thinking

- 123) If the feasible region for a linear programming problem is unbounded, then the solution to the corresponding linear programming problem is _____ unbounded.
- A) always
- B) sometimes
- C) never
- D) There is not enough information to complete this statement.

Answer: B

Diff: 3 Page Ref: 56

Section Heading: Irregular Types of Linear Programming Problems

Keywords: irregular types of linear programming problems, unboundedness