

INSTRUCTOR'S SOLUTIONS MANUAL  
TO ACCOMPANY

# MECHANICS OF MATERIALS

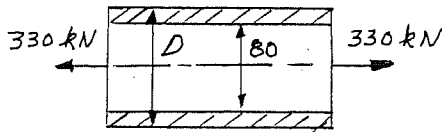
SECOND EDITION

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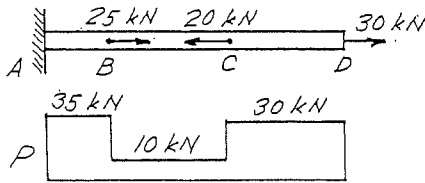
1.1



$$P = \sigma_w A \quad 330 \times 10^3 = (110 \times 10^6) \frac{\pi(D^2 - 0.08^2)}{4}$$

$$D = 0.1011 \text{ m} = 101.1 \text{ mm} \quad \blacktriangleleft$$

1.2

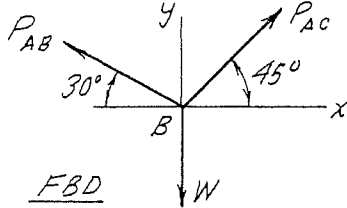


$$P_{\max} = P_{AB} = 35 \text{ kN}$$

$$\sigma_{\max} = \frac{P_{\max}}{A} = \frac{35 \times 10^3}{600 \times 10^{-6}} = 58.3 \times 10^6 \text{ Pa}$$

$$= 58.3 \text{ MPa} \quad \blacktriangleleft$$

1.3



$$\Sigma F_x = 0 \quad P_{AC} \cos 45^\circ - P_{AB} \cos 30^\circ = 0$$

$$\Sigma F_y = 0 \quad P_{AC} \sin 45^\circ + P_{AB} \sin 30^\circ - W = 0$$

The solution is

$$P_{AC} = 0.8966W \quad P_{AB} = 0.7321W$$

Assuming that stress in AC governs:

$$(\sigma_{AC})_w = \frac{P_{AC}}{A_{AC}} \quad 150 \times 10^6 = \frac{0.8966W}{200 \times 10^{-6}}$$

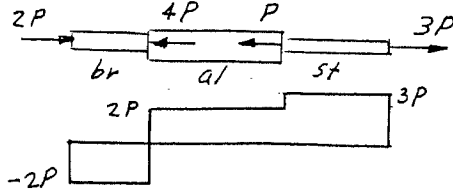
$$W = 33500 \text{ N} = 33.5 \text{ kN} \quad \blacktriangleleft$$

Assuming that stress in AB governs:

$$(\sigma_{AB})_w = \frac{P_{AB}}{A_{AB}} \quad 100 \times 10^6 = \frac{0.7321W}{400 \times 10^{-6}}$$

$$W = 54600 \text{ N} = 54.6 \text{ kN}$$

1.4



Axial force diagram

The axial forces in the segments are

$$P_{br} = 2P = 2(10) = 20 \text{ kN (C)}$$

$$P_{al} = 2P = 2(10) = 20 \text{ kN (T)}$$

$$P_{st} = 3P = 3(10) = 30 \text{ kN (T)}$$

$$\sigma_{br} = \frac{P_{br}}{A_{br}} = \frac{20 \times 10^3}{400 \times 10^{-6}} = 50 \times 10^6 \text{ Pa (C)} \quad \blacktriangleleft$$

$$\sigma_{al} = \frac{P_{al}}{A_{al}} = \frac{20 \times 10^3}{600 \times 10^{-6}} = 33.3 \times 10^6 \text{ Pa (T)} \quad \blacktriangleleft$$

$$\sigma_{st} = \frac{P_{st}}{A_{st}} = \frac{30 \times 10^3}{300 \times 10^{-6}} = 100 \times 10^6 \text{ Pa (T)} \quad \blacktriangleleft$$

1.5

Axial forces in the segments are (see solution of Prob.1.4)

$$P_{br} = 2P \text{ (C)} \quad P_{al} = 2P \text{ (T)} \quad P_{st} = 3P \text{ (T)}$$

Assuming that stress in bronze governs:

$$(\sigma_{br})_w = \frac{P_{br}}{A_{br}} \quad 110 \times 10^6 = \frac{2P}{400 \times 10^{-6}}$$

$$P = 22.0 \times 10^3 \text{ N} = 22.0 \text{ kN}$$

Assuming that stress in aluminum governs:

$$(\sigma_{al})_w = \frac{P_{al}}{A_{al}} \quad 68 \times 10^6 = \frac{2P}{600 \times 10^{-6}}$$

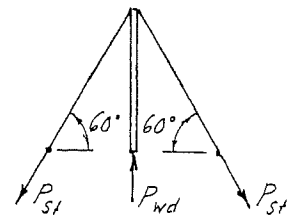
$$P = 20.4 \times 10^3 \text{ N} = 20.4 \text{ kN}$$

Assuming that stress in steel governs:

$$(\sigma_{st})_w = \frac{P_{st}}{A_{st}} \quad 120 \times 10^6 = \frac{3P}{300 \times 10^{-6}}$$

$$P = 12.0 \times 10^3 \text{ N} = 12.0 \text{ kN} \quad \blacktriangleleft$$

1.6



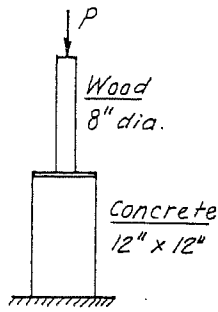
$$\Sigma F_y = 0 \quad P_{wd} - 2P_{st} \sin 60^\circ = 0$$

$$P_{wd} = 2P_{st} \sin 60^\circ = 2\sigma_{st} A_{st} \sin 60^\circ$$

$$= 2(60000) \frac{\pi(0.25)^2}{4} \sin 60^\circ = 5101 \text{ lb}$$

$$A_{wd} = \frac{P_{wd}}{\sigma_{wd}} \quad \frac{\pi d^2}{4} = \frac{5101}{200} \quad d = 5.70 \text{ in.} \quad \blacktriangleleft$$

1.7



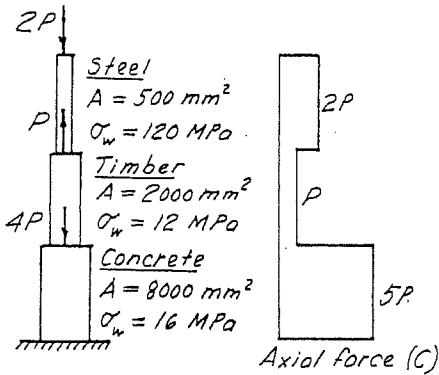
For concrete:

$$P = \sigma_{co} A_{co} = 450(12 \times 12) = 64800 \text{ lb}$$

For wood:

$$P = \sigma_{wd} A_{wd} = 1000 \frac{\pi(8)^2}{4} = 50300 \text{ lb} \leftarrow$$

1.8



For steel:

$$\frac{P_{st}}{A_{st}} = \sigma_{st} \quad \frac{2P}{500 \times 10^{-6}} = 120 \times 10^6 \quad P = 30.0 \times 10^3 \text{ N}$$

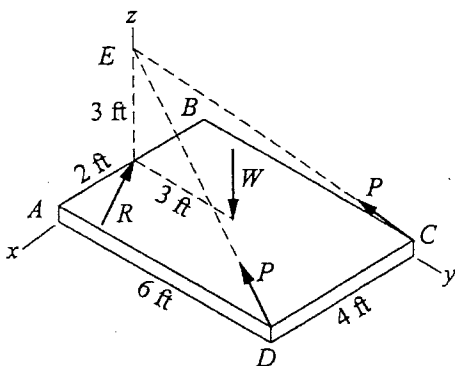
For timber:

$$\frac{P_{wd}}{A_{wd}} = \sigma_{wd} \quad \frac{P}{2000 \times 10^{-6}} = 12 \times 10^6 \quad P = 24.0 \times 10^3 \text{ N} \leftarrow$$

For concrete:

$$\frac{P_{co}}{A_{co}} = \sigma_{co} \quad \frac{5P}{8000 \times 10^{-6}} = 16 \times 10^6 \quad P = 25.6 \times 10^3 \text{ N}$$

1.9



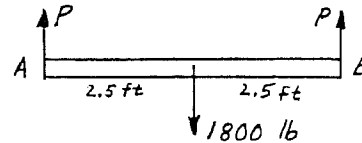
$$P_z = \frac{3}{\sqrt{2^2 + 6^2 + 3^2}} P = 0.4286P$$

$$M_{AB} = 0 \quad 2P_z(6) - W(3) = 0$$

$$2(0.4286P)(6) - 1200(3) = 0 \quad P = 700.0 \text{ lb}$$

$$\sigma_w \frac{\pi d^2}{4} = P \quad d = 2\sqrt{\frac{P}{\pi \sigma_w}} = 2\sqrt{\frac{700.0}{\pi(18000)}} = 0.223 \text{ in.} \leftarrow$$

1.10

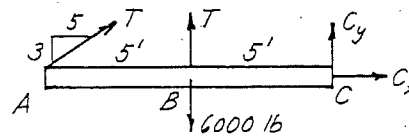


From symmetry, the axial force in each cable is  $P = 900 \text{ lb}$ .

$$A = \frac{P}{\sigma_w} = \frac{900}{18 \times 10^3} = 0.050 \text{ in}^2 \leftarrow$$

for both cables.

1.11

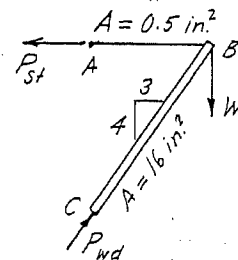


$$\Sigma M_C = 0 \quad \frac{3}{\sqrt{34}} T(10) + T(5) - 6000(5) = 0$$

$$T = 2957 \text{ lb}$$

$$\sigma = \frac{T}{A} = \frac{2957}{\pi(0.6)^2/4} = 10460 \text{ psi} \leftarrow$$

1.12



$$\Sigma F_y = 0 \quad \frac{4}{5} P_{wd} - W = 0 \quad P_{wd} = \frac{5}{4} W$$

$$\Sigma F_x = 0 \quad \frac{3}{5} P_{wd} - P_{st} = 0$$

$$P_{st} = \frac{3}{5} P_{wd} = \frac{3}{5} \left( \frac{5}{4} W \right) = \frac{3}{4} W$$

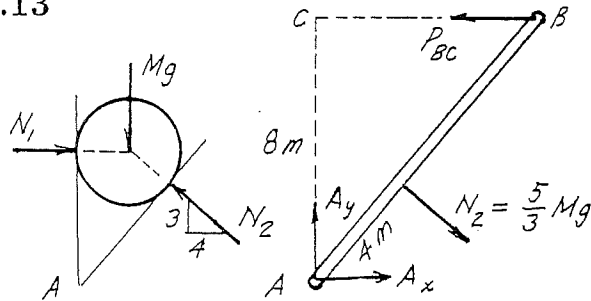
For steel cable:

$$\sigma_{st} A_{st} = P_{st} \quad 16000(0.5) = \frac{3}{4} W \quad W = 10670 \text{ lb}$$

For wood strut:

$$\sigma_{wd} A_{wd} = P_{wd} \quad 720(16) = \frac{5}{4} W \quad W = 9220 \text{ lb} \leftarrow$$

### 1.13



FBDs

From FBD of cylinder:

$$\Sigma F_y = 0 \quad \frac{3}{5} N_2 - Mg = 0 \quad N_2 = \frac{5}{3} Mg$$

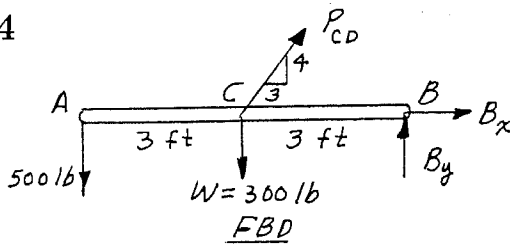
From FBD of bar AB:

$$\Sigma M_A = 0 \quad 4 \left( \frac{5}{3} Mg \right) - 8 P_{BC} = 0 \quad P_{BC} = \frac{5}{6} Mg$$

$$\sigma_w = \frac{P_{BC}}{A_{BC}} \quad 50 \times 10^6 = \frac{(5/6) Mg}{100 \times 10^{-6}}$$

$$Mg = 6000 \text{ N} \quad M = \frac{6000}{9.81} = 612 \text{ kg} \leftarrow$$

### 1.14

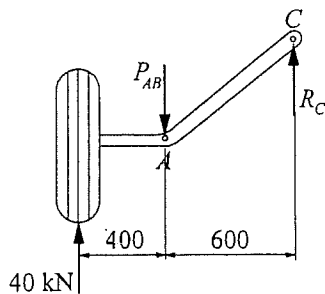


$$\Sigma M_B = 0 \quad 3 \left( \frac{4}{5} P_{CD} \right) - 3(300) - 6(500) = 0$$

$$P_{CD} = 1625 \text{ lb}$$

$$\sigma_{CD} = \frac{P_{CD}}{A_{CD}} = \frac{1625}{\pi(0.5)^2/4} = 8280 \text{ psi} \leftarrow$$

### 1.15



$$\Sigma M_C = 0 \quad + \circ \quad 600 P_{AB} - 40(1000) = 0$$

$$P_{AB} = 66.67 \text{ kN}$$

$$\sigma_{AB} = \frac{P_{AB}}{A_{AB}} = \frac{66.67}{\frac{\pi}{4}(0.05^2 - 0.04^2)} = 94.3 \times 10^3 \text{ kPa}$$

$$= 94.3 \text{ MPa} \leftarrow$$

### 1.16

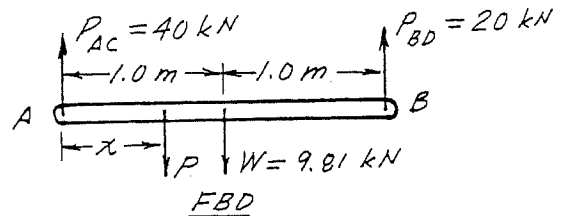
When  $P$  is maximized, both cables are stressed to the limiting values. The corresponding forces in the cables are

$$P_{AC} = (\sigma_{AC})_w A = (100 \times 10^6)(400 \times 10^{-6})$$

$$= 40 \times 10^3 \text{ N} = 40 \text{ kN}$$

$$P_{BD} = (\sigma_{BD})_w A = (50 \times 10^6)(400 \times 10^{-6})$$

$$= 20 \times 10^3 \text{ N} = 20 \text{ kN}$$

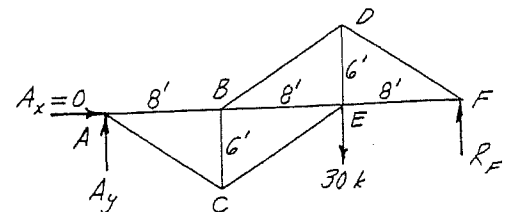


$$\Sigma F = 0 \quad 40 + 20 - 9.81 - P = 0 \quad P = 50.19 \text{ kN} \leftarrow$$

$$\Sigma M_A = 0 \quad 2(20) - 1.0(9.81) - x(50.19) = 0$$

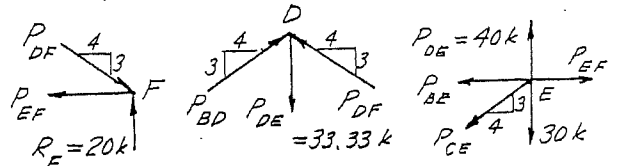
$$x = 0.602 \text{ m} = 602 \text{ mm} \leftarrow$$

### 1.17



From FBD of truss:

$$\Sigma M_A = 0 \quad 24 R_F - 16(30) = 0 \quad R_F = 20 \text{ kips}$$



From FBD of joint F:

$$\Sigma F_y = 0 \quad -\frac{3}{5} P_{DF} + 20 = 0 \quad P_{DF} = 33.33 \text{ kips}$$

$$\sigma_{DF} = \frac{P_{DF}}{A} = \frac{33.33}{1.8} = 18.52 \text{ ksi (C)} \leftarrow$$

From FBD of joint D:

$$P_{BD} = P_{DF} = 33.33 \text{ kips (due to symmetry)}$$

$$\Sigma F_y = 0 \quad 2 \left[ \frac{3}{5}(33.33) \right] - P_{DE} = 0$$

$$P_{DE} = 40 \text{ kips}$$

$$\sigma_{DE} = \frac{P_{DE}}{A} = \frac{40}{1.8} = 22.2 \text{ ksi (T)} \quad \blacktriangleleft$$

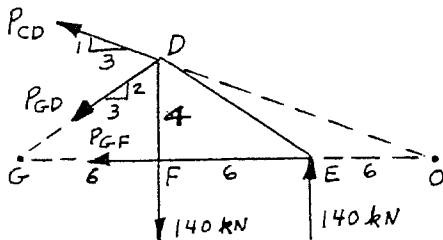
From FBD of joint E:

$$\Sigma F_y = 0 \quad 40 - 30 - \frac{3}{5}P_{CE} = 0$$

$$P_{CE} = 16.667 \text{ kips}$$

$$\sigma_{CE} = \frac{P_{CE}}{A} = \frac{16.667}{1.8} = 9.26 \text{ ksi (T)} \quad \blacktriangleleft$$

1.18



By symmetry, the reaction at the support E is 140 kN  $\uparrow$ .  
Using the FBD of the section shown:

$$\Sigma M_G = 0 \quad \frac{3}{\sqrt{10}}P_{CD}(6) + 140(12) - 140(6) = 0$$

$$P_{CD} = -147.6 \text{ kN} = 147.6 \text{ kN (C)}$$

$$A_{CD} = \frac{P_{CD}}{\sigma_{\text{comp}}} = \frac{147.6 \times 10^3}{100 \times 10^6} = 1.476 \times 10^{-3} \text{ m}^2$$

$$= 1476 \text{ mm}^2 \quad \blacktriangleleft$$

$$\Sigma M_D = 0 \quad 140(6) - P_{GF}(4) = 0$$

$$P_{GF} = 210 \text{ kN (T)}$$

$$A_{GF} = \frac{P_{GF}}{\sigma_{\text{tens}}} = \frac{210 \times 10^3}{140 \times 10^6} = 1.500 \times 10^{-3} \text{ m}^2$$

$$= 1500 \text{ mm}^2 \quad \blacktriangleleft$$

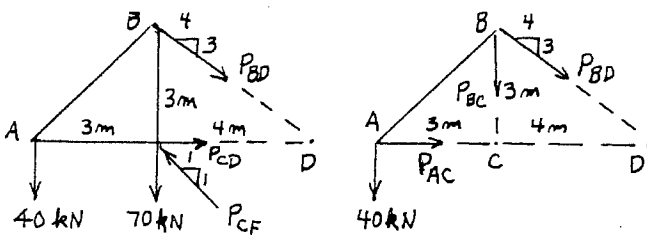
$$\Sigma M_O = 0 \quad \frac{2}{\sqrt{13}}P_{GD}(18) + 140(12) - 140(6) = 0$$

$$P_{GD} = -84.13 \text{ kN} = 84.13 \text{ kN (C)}$$

$$A_{GD} = \frac{P_{GD}}{\sigma_{\text{comp}}} = \frac{84.13 \times 10^3}{100 \times 10^6} = 0.841 \times 10^{-3} \text{ m}^2$$

$$= 841 \text{ mm}^2 \quad \blacktriangleleft$$

1.19



From FBD of portion ABC:

$$\Sigma M_D = 0 \quad 7(40) + 4(70) - 4 \left( \frac{1}{\sqrt{2}}P_{CF} \right) = 0$$

$$P_{CF} = 198.0 \text{ kN}$$

$$\sigma_{CF} = \frac{P_{CF}}{A} = \frac{198.0 \times 10^3}{1400 \times 10^{-6}} = 141.4 \times 10^6 \text{ Pa (C)} \quad \blacktriangleleft$$

$$\Sigma M_C = 0 \quad 3(40) - 3 \left( \frac{4}{5}P_{BD} \right) = 0 \quad P_{BD} = 50 \text{ kN}$$

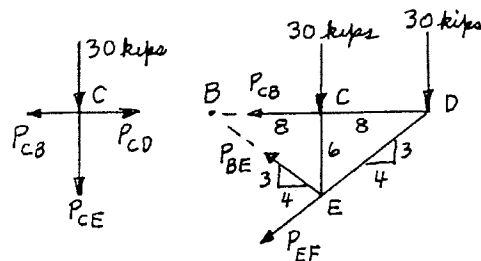
$$\sigma_{BD} = \frac{P_{BD}}{A} = \frac{50 \times 10^3}{1400 \times 10^{-6}} = 35.7 \times 10^6 \text{ Pa (T)} \quad \blacktriangleleft$$

From FBD of member AB:

$$\Sigma M_D = 0 \quad 7(40) - 4P_{BC} = 0 \quad P_{BC} = 70 \text{ kN}$$

$$\sigma_{BC} = \frac{P_{BC}}{A} = \frac{70 \times 10^3}{1400 \times 10^{-6}} = 50.0 \times 10^6 \text{ Pa (C)} \quad \blacktriangleleft$$

1.20



Using the FBD of joint C:

$$\Sigma F_y = 0 \quad -30 - P_{CE} = 0$$

$$P_{CE} = -30 \text{ kips} = 30 \text{ kips (C)}$$

$$A_{CE} = \frac{P_{CE}}{\sigma_{\text{comp}}} = \frac{30000}{14000} = 2.14 \text{ in.}^2 \quad \blacktriangleleft$$

Using the FBD of the section:

$$\Sigma M_D = 0 \quad 30(8) - \frac{3}{5}P_{BE}(16) = 0$$

$$P_{BE} = 25 \text{ kips} = 25 \text{ kips (T)}$$

$$A_{BE} = \frac{P_{BE}}{\sigma_{\text{tens}}} = \frac{25000}{20000} = 1.25 \text{ in.}^2 \quad \blacktriangleleft$$

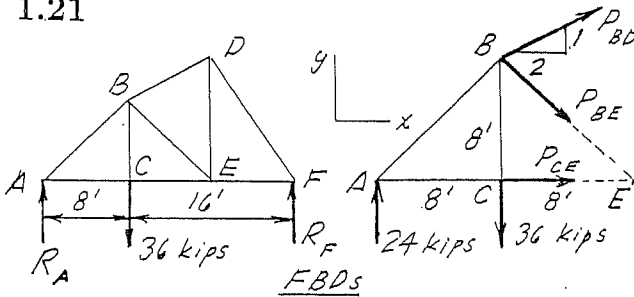
$$\Sigma M_B = 0 \quad -30(8) - 30(16) - \frac{3}{5}P_{EF}(16) = 0$$

$$P_{EF} = -75 \text{ kips} = 75 \text{ kips (C)}$$

$$A_{EF} = \frac{P_{EF}}{\sigma_{\text{comp}}} = \frac{75000}{14000} = 5.36 \text{ in.}^2 \quad \blacktriangleleft$$

$$\begin{aligned}
 A_{BE} &= \frac{P_{BE}}{(\sigma_T)_w} = \frac{62.5 \times 10^3}{100 \times 10^6} = 625 \times 10^{-6} \text{ m}^2 \\
 &= 625 \text{ mm}^2 \quad \blacktriangleleft \\
 A_{BF} &= \frac{P_{BF}}{(\sigma_T)_w} = \frac{42.72 \times 10^3}{100 \times 10^6} = 427 \times 10^{-6} \text{ m}^2 \\
 &= 427 \text{ mm}^2 \quad \blacktriangleleft \\
 A_{CF} &= \frac{|P_{CF}|}{(\sigma_C)_w} = \frac{52.5 \times 10^3}{80 \times 10^6} = 656 \times 10^{-6} \text{ m}^2 \\
 &= 656 \text{ mm}^2 \quad \blacktriangleleft
 \end{aligned}$$

### 1.21



From FBD of truss

$$\Sigma M_F = 0 \quad 24R_A - 16(36) = 0 \quad R_A = 24 \text{ kips}$$

From FBD of portion ABC

$$\Sigma M_B = 0:$$

$$8(24) - 8P_{CE} = 0$$

$$\Sigma M_E = 0:$$

$$16(24) - 8(36) + 8\left(\frac{1}{\sqrt{5}}P_{BD}\right) + 8\left(\frac{2}{\sqrt{5}}P_{BD}\right) = 0$$

$$\Sigma F_x = 0:$$

$$\frac{2}{\sqrt{5}}P_{BD} + \frac{1}{\sqrt{2}}P_{BE} + P_{CE} = 0$$

Solution is

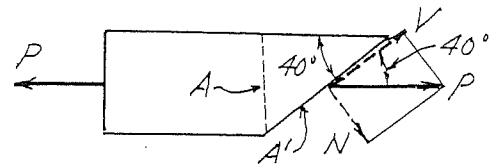
$$P_{CE} = 24.0 \text{ kN} \quad P_{BD} = -8.944 \text{ kN} \quad P_{BE} = -22.63 \text{ kN}$$

$$A_{CE} = \frac{P_{CE}}{(\sigma_T)_w} = \frac{24.0 \times 10^3}{20 \times 10^3} = 1.2 \text{ in.}^2 \quad \blacktriangleleft$$

$$A_{BD} = \frac{|P_{BD}|}{(\sigma_C)_w} = \frac{8.944 \times 10^3}{12 \times 10^3} = 0.745 \text{ in.}^2 \quad \blacktriangleleft$$

$$A_{BE} = \frac{|P_{BE}|}{(\sigma_C)_w} = \frac{22.63 \times 10^3}{12 \times 10^3} = 1.886 \text{ in.}^2 \quad \blacktriangleleft$$

### 1.22

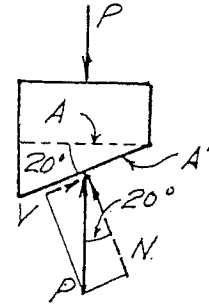


$$A' = \frac{A}{\sin 40^\circ} = \frac{2 \times 4}{\sin 40^\circ} = 12.446 \text{ in.}^2$$

$$V = P \cos 40^\circ = 0.7660P$$

$$\tau_w = \frac{V}{A'} \quad 250 = \frac{0.7660P}{12.446} \quad P = 4060 \text{ lb} \quad \blacktriangleleft$$

### 1.23



$$A' = \frac{A}{\cos 20^\circ} = \frac{0.05 \times 0.1}{\cos 20^\circ} = 5.321 \times 10^{-3} \text{ m}^2$$

$$N = P \cos 20^\circ = 0.9397P \quad V = P \sin 20^\circ = 0.3420P$$

Assuming that compression governs:

$$\sigma_w = \frac{N}{A'} \quad 18 \times 10^6 = \frac{0.9397P}{5.321 \times 10^{-3}}$$

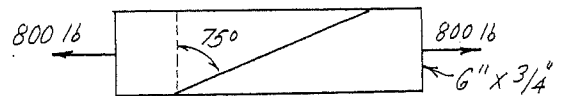
$$P = 101.9 \times 10^3 \text{ N} = 101.9 \text{ kN}$$

Assuming that shear governs:

$$\tau_w = \frac{V}{A'} \quad 4 \times 10^6 = \frac{0.3420P}{5.321 \times 10^{-3}}$$

$$P = 62.2 \times 10^3 \text{ N} = 62.2 \text{ kN} \quad \blacktriangleleft$$

### 1.24



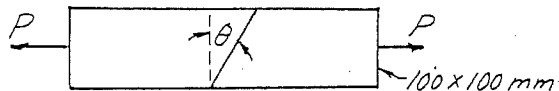
Equivalent joint

From Eqs. (1.5):

$$\sigma = \frac{P}{A} \cos^2 \theta = \frac{800}{6 \times 3/4} \cos^2 75^\circ = 11.91 \text{ psi} \quad \blacktriangleleft$$

$$\tau = \frac{P}{2A} \sin 2\theta = \frac{800}{2(6 \times 3/4)} \sin 150^\circ = 44.4 \text{ psi} \quad \blacktriangleleft$$

1.25



Assuming that tension in wood governs:

$$(\sigma_w)_{wd} = \frac{P}{A} \quad 20 = \frac{P}{0.1^2} \quad P = 0.2 \text{ MN}$$

Assuming that tension in glue governs:

$$(\sigma_w)_{gl} = \frac{P}{A} \cos^2 \theta \quad 8 = \frac{P}{0.1^2} \cos^2 50^\circ$$

$$P = 0.1936 \text{ MN}$$

Assuming that shear in glue governs:

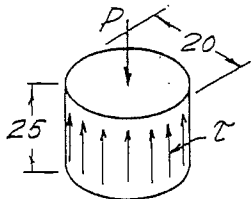
$$(\tau_w)_{gl} = \frac{P}{2A} \sin 2\theta \quad 12 = \frac{P}{2(0.1)^2} \sin 100^\circ$$

$$P = 0.244 \text{ MN}$$

The largest allowable  $P$  is determined by tension in glue:

$$P = 193.6 \text{ kN} \quad \blacktriangleleft$$

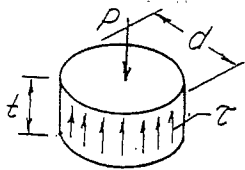
1.26



$$P = \tau A = \tau(\pi d \times t)$$

$$= (350 \times 10^6) \pi(0.02)(0.025) = 550 \times 10^3 \text{ N} \quad \blacktriangleleft$$

1.27



$$P = \tau A \quad \sigma_w \frac{\pi d^2}{4} = \tau(\pi d \times t) \quad \frac{\sigma_w d}{4} = t\tau$$

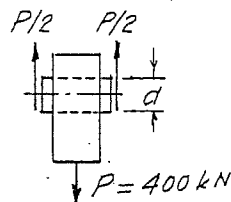
(a)  $d = 2.5 \text{ in.}$

$$t = \frac{\sigma_w d}{4\tau} = \frac{50(2.5)}{4(40)} = 0.781 \text{ in.} \quad \blacktriangleleft$$

(b)  $t = 0.25 \text{ in.}$

$$d = \frac{4t\tau}{\sigma_w} = \frac{4(0.25)(40)}{50} = 0.800 \text{ in.} \quad \blacktriangleleft$$

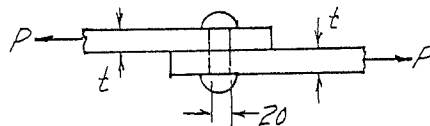
1.28



$$\tau_w A = \frac{P}{2} \quad (300 \times 10^6) \frac{\pi d^2}{4} = \frac{400 \times 10^3}{2}$$

$$d = 0.0291 \text{ m} = 29.1 \text{ mm} \quad \blacktriangleleft$$

1.29



Shear in rivet determines upper limit on  $P$ :

$$P = \tau A_s = (60 \times 10^6) \frac{\pi(0.02)^2}{4} = 18850 \text{ N}$$

Plate thickness is determined by bearing stress:

$$P = \sigma_b A_b \quad 18850 = (120 \times 10^6)(0.02t)$$

$$t = 7.85 \times 10^{-3} \text{ m} = 7.85 \text{ mm} \quad \blacktriangleleft$$

1.30

(a)

$$\tau = \frac{P}{3A} = \frac{50 \times 10^3}{3 \frac{\pi(0.02)^2}{4}} = 53.1 \times 10^6 \text{ Pa} = 53.1 \text{ MPa} \quad \blacktriangleleft$$

(b)

$$\sigma_b = \frac{P}{3td} = \frac{50 \times 10^3}{3(0.025)(0.02)} = 33.3 \times 10^6 \text{ Pa} = 33.3 \text{ MPa} \quad \blacktriangleleft$$

(c)

$$\sigma = \frac{P}{t(w-d)} = \frac{50 \times 10^3}{0.025(0.13-0.02)} = 18.18 \times 10^6 \text{ Pa}$$

$$= 18.18 \text{ MPa} \quad \blacktriangleleft$$



### 1.31

Assuming that shear in rivets governs:

$$P = 3A\tau_w = 3 \frac{\pi(0.02)^2}{4} (40 \times 10^6)$$

$$= 37.7 \times 10^3 \text{ N} = 37.7 \text{ kN} \quad \blacktriangleleft$$

Assuming that bearing stress governs:

$$P = 3td(\sigma_b)_w = 3(0.025)(0.02)(90 \times 10^6)$$

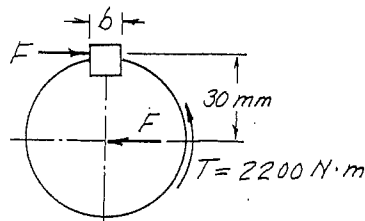
$$= 135 \times 10^3 = 135 \text{ kN}$$

Assuming that tension in plates governs:

$$P = t(w-d)\sigma_w = 0.025(0.13 - 0.02)(120 \times 10^6)$$

$$= 330 \times 10^3 \text{ N} = 330 \text{ kN}$$

### 1.32

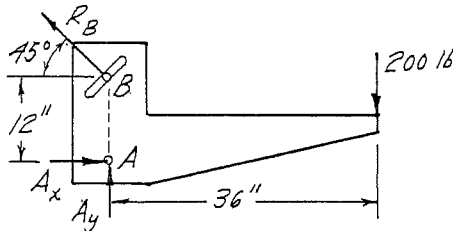


$$F = \frac{T}{r} = \frac{2200}{0.03} = 73.33 \times 10^3 \text{ N}$$

$$F = \tau_w A \quad 73.33 \times 10^3 = (60 \times 10^6)(0.07b)$$

$$b = 0.01746 \text{ m} = 17.46 \text{ mm} \quad \blacktriangleleft$$

### 1.33



$$\begin{aligned} \Sigma M_B = 0 & \quad 12A_x - 36(200) = 0 \\ \Sigma F_x = 0 & \quad A_x - R_B \cos 45^\circ = 0 \\ \Sigma F_y = 0 & \quad A_y + R_B \sin 45^\circ - 200 = 0 \end{aligned}$$

$$A_x = 600 \text{ lb} \quad A_y = -400 \text{ lb} \quad R_B = 848.5 \text{ lb}$$

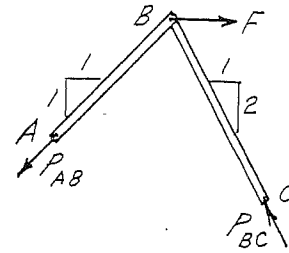
$$R_A = \sqrt{600^2 + (-400)^2} = 721.1 \text{ lb}$$

$$A = \frac{\pi d^2}{4} = \frac{\pi(0.5)^2}{4} = 0.19635 \text{ in.}^2$$

$$\tau_A = \frac{R_A}{A} = \frac{721.1}{0.19635} = 3670 \text{ psi} \quad \blacktriangleleft$$

$$\tau_B = \frac{R_B}{A} = \frac{848.5}{0.19635} = 4320 \text{ psi} \quad \blacktriangleleft$$

### 1.34



$$\Sigma F_x = 0 \quad -\frac{1}{\sqrt{2}}P_{AB} - \frac{1}{\sqrt{5}}P_{BC} + F = 0$$

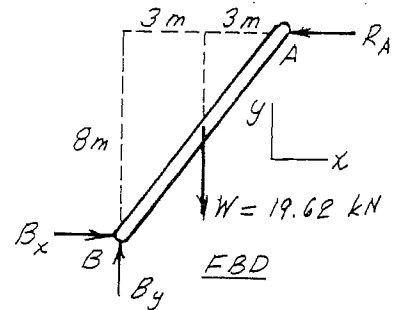
$$\Sigma F_y = 0 \quad -\frac{1}{\sqrt{2}}P_{AB} + \frac{2}{\sqrt{5}}P_{BC} = 0$$

$$P_{AB} = \frac{2\sqrt{2}}{3}F = 0.9428F \quad P_{BC} = \frac{\sqrt{5}}{3}F = 0.7454F$$

$$\tau_w A = P_{AB} \quad (5000) \frac{\pi(7/8)^2}{4} = 0.9428F$$

$$F = 3190 \text{ lb} \quad \blacktriangleleft$$

### 1.35



$$\begin{aligned} \Sigma F_y = 0 & \quad B_y - 19.62 = 0 \\ \Sigma M_A = 0 & \quad 6B_y - 8B_x - 3(19.62) = 0 \end{aligned}$$

Solution is

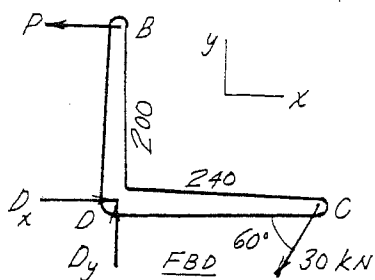
$$B_x = 7.358 \text{ kN} \quad B_y = 19.62 \text{ kN}$$

$$B = \sqrt{7.358^2 + 19.62^2} = 20.95 \text{ kN}$$

$$\tau_w = \frac{B}{2A} \quad 60 \times 10^6 = \frac{20.95 \times 10^3}{2 \frac{\pi d^2}{4}}$$

$$d = 14.91 \times 10^{-3} \text{ m} = 14.91 \text{ mm}$$

1.36



$$M_D = 0 \quad 240(30 \sin 60^\circ) - 200P = 0 \quad P = 31.18 \text{ kN}$$

$$\Sigma F_x = 0 \quad D_x - P - 30 \cos 60^\circ = 0 \quad D_x = 46.18 \text{ kN}$$

$$\Sigma F_y = 0 \quad D_y - 30 \sin 60^\circ = 0 \quad D_y = 25.98 \text{ kN}$$

$$D = \sqrt{46.18^2 + 25.98^2} = 52.99 \text{ kN}$$

(a)

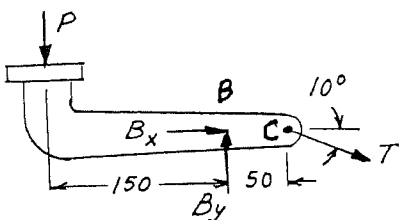
$$\sigma_w = \frac{P}{A} \quad 100 \times 10^6 = \frac{31.18 \times 10^3}{\frac{\pi d^2}{4}}$$

$$d = 19.92 \times 10^{-3} \text{ m} = 19.92 \text{ mm} \blacktriangleleft$$

(b)

$$\tau = \frac{D}{2A} = \frac{52.99 \times 10^3}{2 \frac{\pi(0.02)^2}{4}} = 84.3 \times 10^6 \text{ Pa} = 84.3 \text{ MPa} \blacktriangleleft$$

1.37



$$\Sigma M_B = 0 \quad 150P - 50(T \sin 10^\circ) = 0$$

$$\Sigma M_C = 0 \quad 200P - 50B_y = 0$$

$$\Sigma F_x = 0 \quad B_x + T \cos 10^\circ = 0$$

$$T = 17.276P \quad B_x = -17.014P \quad B_y = 4P$$

Assuming that cable governs:  $T = \sigma_w A_{\text{cab}}$

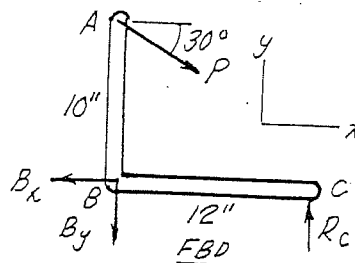
$$17.276P = (140 \times 10^6) \frac{\pi(0.003)^2}{4} \quad P = 57.3 \text{ N}$$

Assuming that pin B governs:  $R_B = \tau_w A_{\text{pin}}$

$$P \sqrt{(-17.014)^2 + 4^2} = (28 \times 10^6) \frac{\pi(0.006)^2}{4}$$

$$P = 45.3 \text{ N} \blacktriangleleft$$

1.38



$$\Sigma F_x = 0 \quad P \cos 30^\circ - B_x = 0$$

$$\Sigma M_C = 0 \quad 10(P \cos 30^\circ) - 12(P \sin 30^\circ) - 12B_y = 0$$

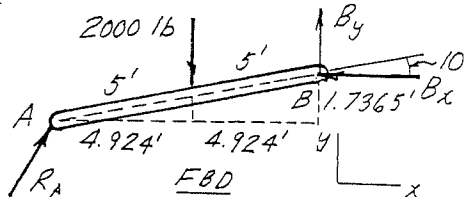
Solution is

$$B_x = 0.8660P \quad B_y = 0.2217P$$

$$B = P \sqrt{0.8660^2 + 0.2217^2} = 0.8939P$$

$$\tau_w = \frac{B}{2A} \quad 20000 = \frac{0.8939P}{2 \frac{\pi(0.75)^2}{4}} \quad P = 19770 \text{ lb} \blacktriangleleft$$

1.39



$$\Sigma M_B = 0$$

$$9.848(R_A \sin 60^\circ) - 1.7365(R_A \cos 60^\circ) - 4.924(2000) = 0$$

$$\Sigma F_x = 0 \quad R_A \cos 60^\circ - B_x = 0$$

$$\Sigma F_y = 0 \quad R_A \sin 60^\circ - 2000 + B_y = 0$$

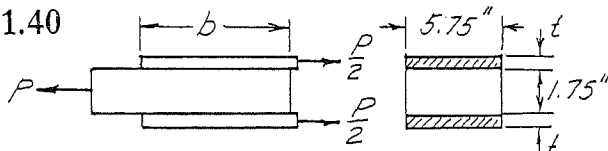
Solution is

$$R_A = 1285.6 \text{ lb} \quad B_x = 642.8 \text{ lb} \quad B_y = 886.6 \text{ lb}$$

$$B = \sqrt{642.8^2 + 886.6^2} = 1095.1 \text{ lb}$$

$$\tau = \frac{B}{2A} = \frac{1095.1}{2 \frac{\pi(7/8)^2}{4}} = 911 \text{ psi} \blacktriangleleft$$

1.40



Strength of boards is

$$P = \sigma_{bd} A_{bd} = 700(5.75 \times 1.75) = 7044 \text{ lb}$$

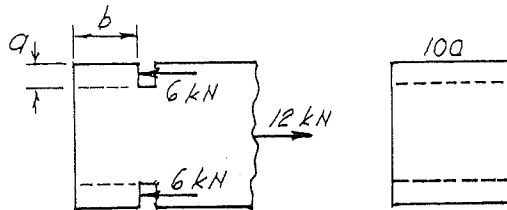
For plywood:

$$\frac{P}{2} = \sigma_{pw} A_{pw} \quad \frac{7044}{2} = 1200(5.75t) \quad t = 0.510 \text{ in.} \leftarrow$$

For glue (double shear):

$$\frac{P}{2} = \tau A_{gl} \quad \frac{7044}{2} = 50(5.75b) \quad b = 12.25 \text{ in.} \leftarrow$$

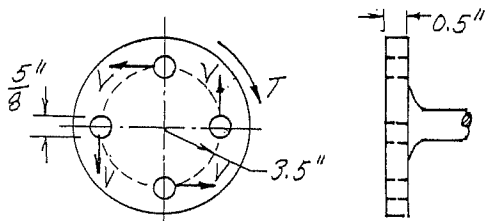
1.41



$$P = \tau A_s \quad 6 \times 10^3 = (1.8 \times 10^6)(0.1b) \\ b = 0.0333 \text{ m} = 33.3 \text{ mm} \leftarrow$$

$$P = \sigma_b A_b \quad 6 \times 10^3 = (5.5 \times 10^6)(0.1a) \\ a = 0.01091 \text{ m} = 10.91 \text{ mm} \leftarrow$$

1.42



First find the maximum safe shear force  $V$  in each bolt. Assuming that bearing stress governs:

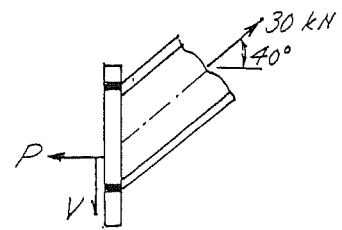
$$V = \sigma_b A_b = (15 \times 10^3) \left( \frac{5}{8} \times 0.5 \right) = 4688 \text{ lb}$$

Assuming that shear stress governs:

$$V = \tau A_s = (12 \times 10^3) \frac{\pi(5/8)^2}{4} = 3682 \text{ lb}$$

$$T = 4V\tau = 4(3682)(3.5) = 51500 \text{ lb} \cdot \text{in.} \leftarrow$$

1.43



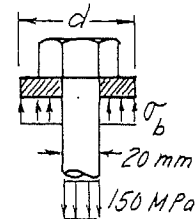
Total area of the bolts is

$$A = 4 \left[ \frac{\pi(0.01)^2}{4} \right] = 314.2 \times 10^{-6} \text{ m}^2$$

$$\sigma = \frac{P}{A} = \frac{(30 \times 10^3) \cos 40^\circ}{314.2 \times 10^{-6}} = 73.1 \times 10^6 \text{ Pa} \leftarrow$$

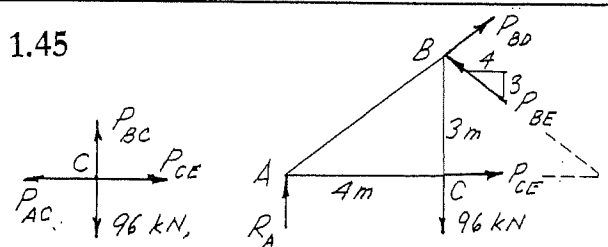
$$\tau = \frac{V}{A} = \frac{(30 \times 10^3) \sin 40^\circ}{314.2 \times 10^{-6}} = 61.4 \times 10^6 \text{ Pa} \leftarrow$$

1.44



$$\sigma A = \sigma_b A_b \\ (150 \times 10^6) \frac{\pi(0.02)^2}{4} = (13 \times 10^6) \frac{\pi(d^2 - 0.02^2)}{4} \\ d = 0.0708 \text{ m} = 70.8 \text{ mm} \leftarrow$$

1.45



$d = 19 \text{ mm}$  (rivet diameter);  $t = 6 \text{ mm}$  for  $BC$  and  $t = 13 \text{ mm}$  for  $BE$  (wall thickness). Because the gusset plate is thicker than the members, bearing between the rivets and the plate does not have to be considered.

(a) From FBD of joint  $C$ :  $P_{BC} = 96 \text{ kN}$

$$n\tau \frac{\pi d^2}{4} = P_{BC} \quad n(70 \times 10^6) \frac{\pi(0.019)^2}{4} = 96 \times 10^3 \\ n = 4.84$$

$$n\sigma_b(td) = P_{BC} \quad n(140 \times 10^6)(0.006 \times 0.019) = 96 \times 10^3$$

$$n = 6.02$$

Use 7 rivets ◀

(b) From FBD of portion ABC:

$$\Sigma M_A = 0 \quad 8 \left( \frac{3}{5} P_{BE} \right) - 4(96) = 0 \quad P_{BE} = 80 \text{ kN}$$

$$n\tau \frac{\pi d^2}{4} = P_{BE} \quad n(70 \times 10^6) \frac{\pi(0.019)^2}{4} = 80 \times 10^3$$

$$n = 4.03$$

$$n\sigma_b(td) = P_{BE} \quad n(140 \times 10^6)(0.013 \times 0.019) = 80 \times 10^3$$

$$n = 2.31$$

Use 5 rivets ◀

### 1.46

Repeat Prob. 1.45 with  $d = 22 \text{ mm}$ .

(a)  $P_{BC} = 96 \text{ kN}$  (from solution of Prob. 1.45)

$$n\tau A_s = P_{BC} \quad n(70 \times 10^6) \frac{\pi(0.022)^2}{4} = 96 \times 10^3$$

$$n = 3.61$$

$$n\sigma_b A_b = P_{BC} \quad n(140 \times 10^6)(0.006 \times 0.022) = 96 \times 10^3$$

$$n = 5.19$$

Use 6 rivets ◀

(b)  $P_{BE} = 80 \text{ kN}$  (from solution of Prob. 1.45)

$$n\tau A_s = P_{BE} \quad n(70 \times 10^6) \frac{\pi(0.022)^2}{4} = 80 \times 10^3$$

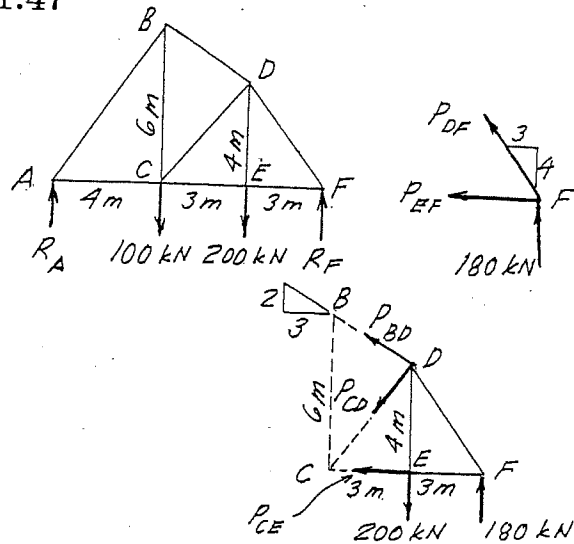
$$n = 3.01$$

$$n\sigma_b A_b = P_{BE} \quad n(140 \times 10^6)(0.013 \times 0.022) = 80 \times 10^3$$

$$n = 2.00$$

Use 4 rivets ◀

### 1.47



From FBD of truss:

$$\Sigma M_A = 0 \quad 10R_F - 4(100) - 7(200) = 0$$

$$R_F = 180 \text{ kN}$$

From FBD of joint F:

$$\Sigma F_y = 0 \quad \frac{4}{5} P_{DF} + 180 = 0 \quad P_{DF} = -225 \text{ kN}$$

From FBD of portion EDF:

$$\Sigma M_D = 0 \quad 4P_{CE} - 3(180) = 0 \quad P_{CE} = 135 \text{ kN}$$

$$\Sigma M_C = 0$$

$$4 \left( \frac{3}{\sqrt{13}} P_{BD} \right) + 3 \left( \frac{2}{\sqrt{13}} P_{BD} \right) + 6(180) - 3(200) = 0$$

$$P_{BD} = -96.15 \text{ kN}$$

$$\sigma_{DF} = \frac{P_{DF}}{A} = -\frac{225 \times 10^3}{1200 \times 10^{-6}} = -187.5 \times 10^6 \text{ Pa}$$

$$= 187.5 \text{ MPa (C)} \quad \blacktriangleleft$$

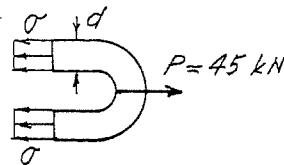
$$\sigma_{CE} = \frac{P_{CE}}{A} = \frac{135 \times 10^3}{1200 \times 10^{-6}} = 112.5 \times 10^6 \text{ Pa}$$

$$= 112.5 \text{ MPa (T)} \quad \blacktriangleleft$$

$$\sigma_{BD} = \frac{P_{BD}}{A} = -\frac{96.15 \times 10^3}{1200 \times 10^{-6}} = -80.1 \times 10^6 \text{ Pa}$$

$$= 80.1 \text{ MPa (C)} \quad \blacktriangleleft$$

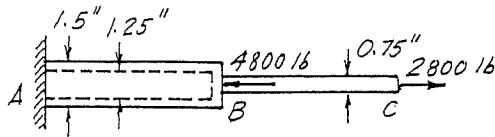
### 1.48



$$P = \sigma_w A \quad 45 \times 10^3 = (300 \times 10^6) \left( 2 \frac{\pi d^2}{4} \right)$$

$$d = 9.77 \times 10^{-3} \text{ m} = 9.77 \text{ mm} \quad \blacktriangleleft$$

1.49

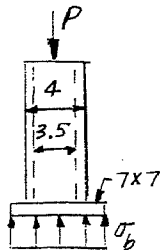


$$P_{AB} = 4800 - 2800 = 2000 \text{ lb (C)} \quad P_{BC} = 2800 \text{ lb (T)}$$

$$\sigma_{AB} = \left(\frac{P}{A}\right)_{AB} = \frac{2000}{(\pi/4)(1.5^2 - 1.25^2)} = 3700 \text{ psi (C)} \blacktriangleleft$$

$$\sigma_{BC} = \left(\frac{P}{A}\right)_{BC} = \frac{2800}{(\pi/4)(0.75)^2} = 6340 \text{ psi (T)} \blacktriangleleft$$

1.50



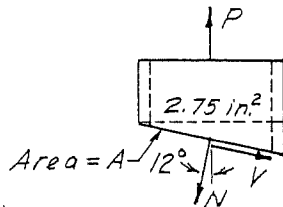
Assuming that stress in steel column governs:

$$P = \sigma_{st} A_{st} = (26\,000) \frac{\pi(4^2 - 3.5^2)}{4} = 76\,600 \text{ lb}$$

Assuming that bearing stress on concrete governs:

$$P = \sigma_b A_{pl} = 1200(7)^2 = 58\,800 \text{ lb} \blacktriangleleft$$

1.51



$$A = \frac{2.75}{\cos 12^\circ} = 2.811 \text{ in.}^2 \text{ (inclined cross-sectional area)}$$

(a)

$$\sigma = \frac{N}{A} \quad 12 = \frac{P \cos 12^\circ}{2.811} \quad P = 34.49 \text{ kips} \blacktriangleleft$$

(b)

$$\tau = \frac{V}{A} = \frac{P \sin 12^\circ}{A} = \frac{34.49 \sin 12^\circ}{2.811} = 2.55 \text{ ksi} \blacktriangleleft$$

1.52

Maximum axial force equals weight of cable:

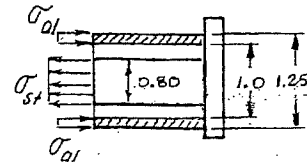
$$P_{\max} = \rho g A L \quad \sigma_{\max} = \frac{P_{\max}}{A} = \rho g L$$

$$390 \times 10^6 = 2700(9.81)L$$

$$L = 14\,720 \text{ m} = 14.72 \text{ km} \blacktriangleleft$$

Result is independent of diameter of cable.

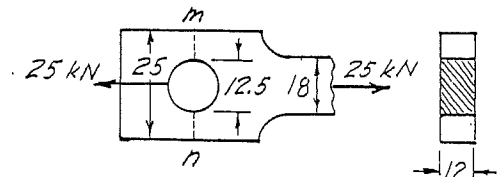
1.53



$$\sigma_{st} A_{st} = \sigma_{al} A_{al} \quad (12\,000) \frac{\pi(0.8)^2}{4} = \sigma_{al} \frac{\pi(1.25^2 - 1.00^2)}{4}$$

$$\sigma_{al} = 13\,700 \text{ psi} \blacktriangleleft$$

1.54



(a) Largest bearing stress is between pin and 12-mm thick member.

$$\sigma_b = \frac{P}{td} = \frac{25 \times 10^3}{0.012(0.0125)} = 166.7 \times 10^6 \text{ Pa} \blacktriangleleft$$

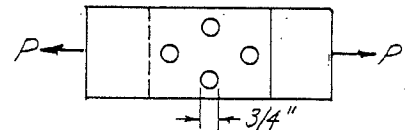
(b) Pin is in double shear.

$$\tau = \frac{P}{2(\pi d^2/4)} = \frac{25 \times 10^3}{2\pi(0.0125)^2/4} = 101.9 \times 10^6 \text{ Pa} \blacktriangleleft$$

(c) Largest normal stress is in 12-mm thick member at section m-n.

$$\sigma = \frac{P}{t(b-d)} = \frac{25 \times 10^3}{0.012(0.025 - 0.0125)} = 166.7 \times 10^6 \text{ Pa} \blacktriangleleft$$

1.55



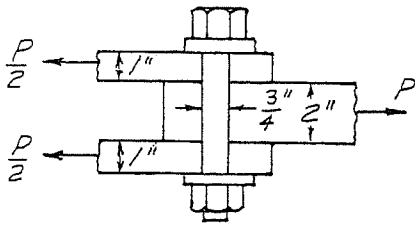
Assuming that shear stress in rivets governs:

$$P = 4\tau \frac{\pi d^2}{4} = 4(14) \frac{\pi(3/4)^2}{4} = 24.7 \text{ kips} \blacktriangleleft$$

Assuming that bearing stress governs:

$$P = 4\sigma_b(td) = 4(18) \left(\frac{7}{8} \times \frac{3}{4}\right) = 47.3 \text{ kips}$$

1.56



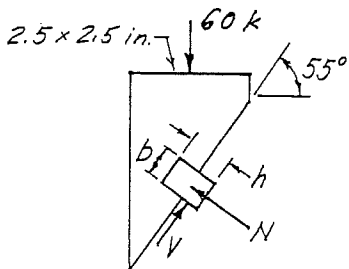
Assuming that normal stress in wood governs:

$$P = \sigma(tt) = 800(2 \times 4) = 6400 \text{ lb}$$

Assuming that bearing stress on wood governs:

$$P = \sigma_b(td) = 1500 \left( 2 \times \frac{3}{4} \right) = 2250 \text{ lb} \quad \blacktriangleleft$$

1.57



$N$  is carried by surface between cast iron pieces;  $V$  is carried by key.

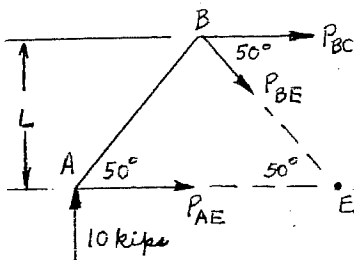
$$V = 60 \sin 55^\circ = 49.15 \text{ kips}$$

$$V = \tau(wb) \quad 49.15 = 50(2.5b) \quad b = 0.393 \text{ in.} \quad \blacktriangleleft$$

$$V = \sigma_b \left( w \frac{h}{2} \right) \quad 49.15 = 40 \left( 2.5 \frac{h}{2} \right)$$

$$h = 0.983 \text{ in.} \quad \blacktriangleleft$$

1.58



By symmetry, the reaction at the support A is 10 kips  $\uparrow$ .  
Using the FBD of the section shown:

$$\Sigma M_E = 0 \quad -10(2L/\tan 50^\circ) - P_{BC}(L) = 0$$

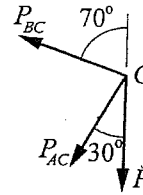
$$P_{BC} = -20/\tan 50^\circ = -16.78 \text{ kips}$$

$$\sigma_{BC} = \frac{P_{BC}}{A_{BC}} = \frac{16780}{4.2} = 4000 \text{ psi (C)} \quad \blacktriangleleft$$

$$\Sigma F_y = 0 \quad 10 - P_{BE} \sin 50^\circ = 0 \quad P_{BE} = 13050 \text{ kips}$$

$$\sigma_{BC} = \frac{P_{BC}}{A_{BC}} = \frac{13050}{4.2} = 3110 \text{ psi (T)} \quad \blacktriangleleft$$

1.59



$$\Sigma F_x = 0 \quad + \leftarrow P_{AC} \sin 30^\circ + P_{BC} \sin 70^\circ = 0$$

$$\Sigma F_y = 0 \quad + \downarrow P_{AC} \cos 30^\circ - P_{BC} \cos 70^\circ + P = 0$$

$$P_{AC} = -0.9542P = 0.9542P \text{ (C)} \quad P_{BC} = 0.5077P \text{ (T)}$$

Boom in compression:

$$\sigma_w A = P_{AC} \quad 18(4^2 - 3.5^2) = 0.9542P$$

$$P = 70.74 \text{ kips}$$

Cable in tension:

$$\sigma_w A = P_{BC} \quad 25 \frac{\pi(0.375)^2}{4} = 0.5077P$$

$$P = 5.439 \text{ kips}$$

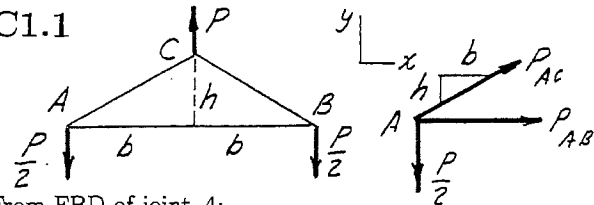
Pin in double shear:

$$2\tau_w A = P_{AC} \quad 2(13.6) \frac{\pi(0.5)^2}{4} = 0.9542P$$

$$P = 5.597 \text{ kips}$$

The largest safe load is  $P = 5.44$  kips determined by cable tension.  $\blacktriangleleft$

C1.1



From FBD of joint A:

$$\Sigma F_y = 0 \quad P_{AC} \frac{h}{\sqrt{b^2 + h^2}} - \frac{P}{2} = 0$$

$$\Sigma F_x = 0 \quad P_{AC} \frac{b}{\sqrt{b^2 + h^2}} + P_{AB} = 0$$

$$P_{AC} = P \frac{\sqrt{b^2 + h^2}}{2h} \text{ (T)} \quad P_{AB} = -P \frac{b}{2h} = P \frac{b}{2h} \text{ (C)}$$

### C1.1 MathCad worksheet

Given:

$$P := 120 \cdot 10^3 \cdot \text{lbf} \quad b := 6 \cdot \text{ft}$$

$$\sigma_t := 18 \cdot 10^3 \cdot \text{psi} \quad \sigma_c := 12 \cdot 10^3 \cdot \text{psi}$$

Computations:

$$P_{AC}(h) := P \cdot \frac{\sqrt{b^2 + h^2}}{2 \cdot h} \quad P_{AB}(h) := P \cdot \frac{b}{2 \cdot h}$$

Axial forces (from equilibrium)

$$A_{AC}(h) := \frac{P_{AC}(h)}{\sigma_c} \quad A_{AB}(h) := \frac{P_{AB}(h)}{\sigma_t}$$

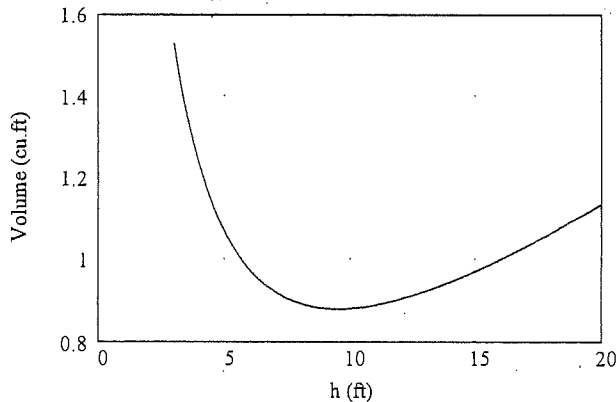
Required cross-sectional areas

$$V(h) := 2 \cdot A_{AC}(h) \cdot \sqrt{b^2 + h^2} + 2 \cdot A_{AB}(h) \cdot b$$

Volume of material

$$h := 0.5 \cdot b, 0.52 \cdot b .. 4 \cdot b$$

Plot range and increment



Find optimal value of  $h$ :

$$h := 3 \cdot b \quad (\text{initial value used in solution})$$

$$\text{Given } \frac{d}{dh} V(h) = 0 \quad h_{\text{opt}} := \text{Find}(h) \quad h_{\text{opt}} = 9.487 \text{ft}$$

### C1.2

The forces computed in the solution of Prob. C1.1 are reversed. Thus

$$P_{AC} = P \frac{\sqrt{b^2 + h^2}}{2h} \quad (C) \quad P_{AB} = P \frac{b}{2h} \quad (T)$$

### C1.2 MathCad worksheet

Given:

$$P := 120 \cdot 10^3 \cdot \text{lbf} \quad b := 6 \cdot \text{ft}$$

$$\sigma_t := 18 \cdot 10^3 \cdot \text{psi} \quad \sigma_c := 12 \cdot 10^3 \cdot \text{psi}$$

Computations:

$$P_{AC}(h) := P \cdot \frac{\sqrt{b^2 + h^2}}{2 \cdot h} \quad P_{AB}(h) := P \cdot \frac{b}{2 \cdot h}$$

Axial forces (from equilibrium)

$$A_{AC}(h) := \frac{P_{AC}(h)}{\sigma_c} \quad A_{AB}(h) := \frac{P_{AB}(h)}{\sigma_t}$$

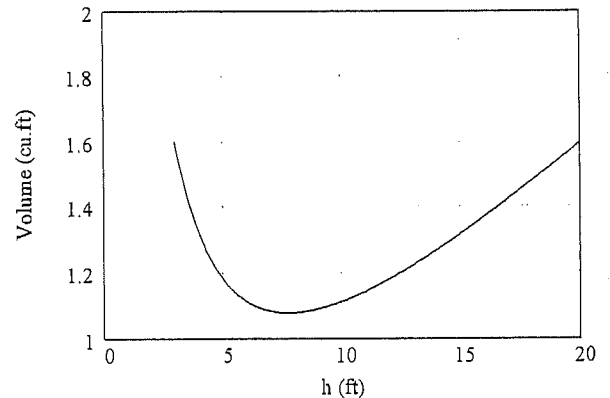
Required cross-sectional areas

$$V(h) := 2 \cdot A_{AC}(h) \cdot \sqrt{b^2 + h^2} + 2 \cdot A_{AB}(h) \cdot b$$

Volume of material

$$h := 0.5 \cdot b, 0.52 \cdot b .. 4 \cdot b$$

Plot range and increment

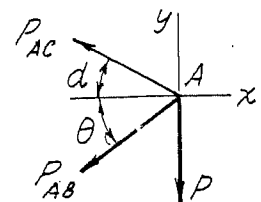


Find optimal value of  $h$ :

$$h := 3 \cdot b \quad (\text{initial value used in solution})$$

$$\text{Given } \frac{d}{dh} V(h) = 0 \quad h_{\text{opt}} := \text{Find}(h) \quad h_{\text{opt}} = 7.746 \text{ft}$$

### C1.3



From FBD of joint A:

$$\Sigma F_x = 0 \quad -P_{AB} \cos \theta - P_{AC} \cos \alpha = 0$$

$$\Sigma F_y = 0 \quad -P_{AB} \sin \theta + P_{AC} \sin \alpha - P = 0$$

$$P_{AB} = -\frac{P}{\cos \theta \tan \alpha + \sin \theta} = \frac{P}{\cos \theta \tan \alpha + \sin \theta} \quad (C)$$

$$P_{AC} = \frac{P}{\cos \alpha \tan \theta + \sin \alpha} \quad (T)$$

### C1.3 MathCad worksheet

Given:

$$P := 530 \cdot 10^3 \cdot \text{N} \quad b := 1.8 \cdot \text{m} \quad \alpha := 30 \cdot \text{deg}$$

$$\sigma_t := 125 \cdot 10^6 \cdot \text{Pa} \quad \sigma_c := 85 \cdot 10^6 \cdot \text{Pa}$$