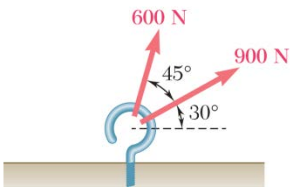
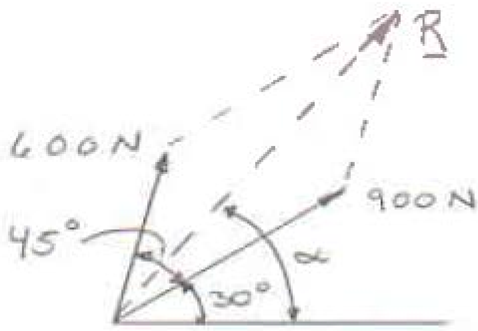


PROBLEM 2.1

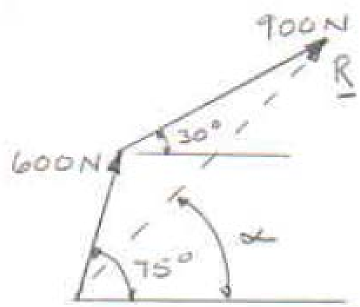
Two forces are applied as shown to a hook. Determine graphically the magnitude and direction of their resultant using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

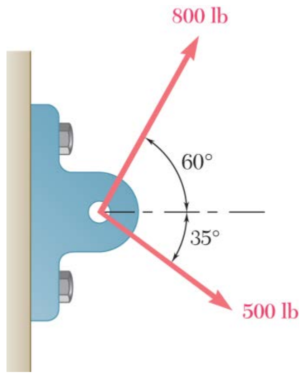
(*a*) Parallelogram law:



(*b*) Triangle rule:



We measure: $R = 1391\text{ kN}, \quad \alpha = 47.8°$ $\quad$ $\mathbf{R} = 1391\text{ N}$ ∠ $47.8°$ ◀

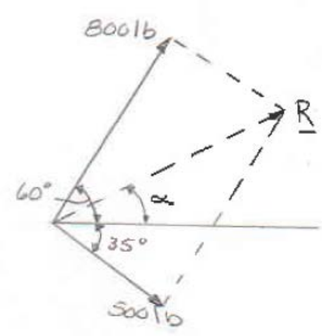


PROBLEM 2.2

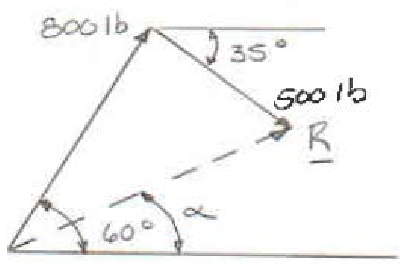
Two forces are applied as shown to a bracket support. Determine graphically the magnitude and direction of their resultant using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

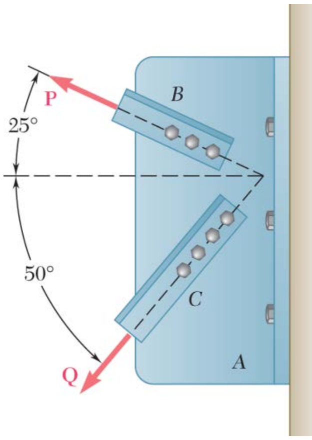
(*a*) Parallelogram law:



(*b*) Triangle rule:



We measure: $R = 906$ lb, $\alpha = 26.6°$ $R = 906 \text{ lb} \measuredangle 26.6°$ ◀

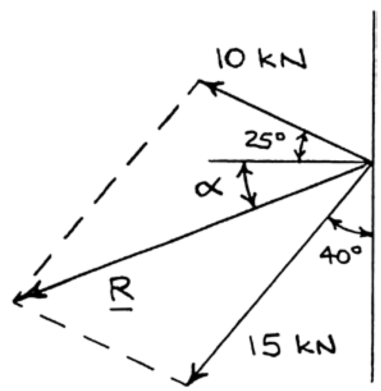


PROBLEM 2.3

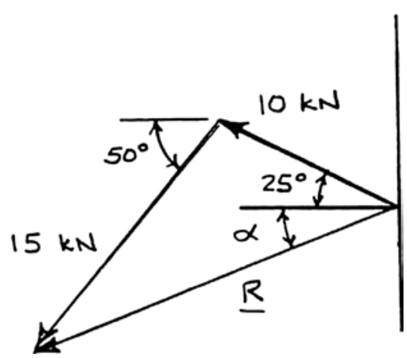
Two structural members *B* and *C* are bolted to bracket *A*. Knowing that both members are in tension and that $P = 10$ kN and $Q = 15$ kN, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

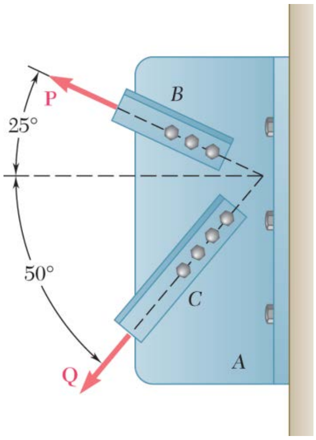
(*a*) Parallelogram law:



(*b*) Triangle rule:



We measure: $R = 20.1$ kN, $\alpha = 21.2°$ **R** = 20.1 kN ⦨ 21.2° ◀

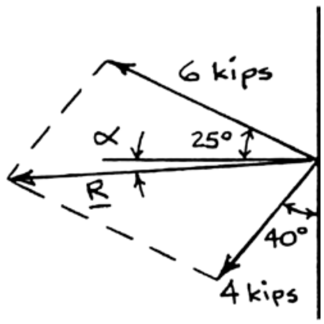


PROBLEM 2.4

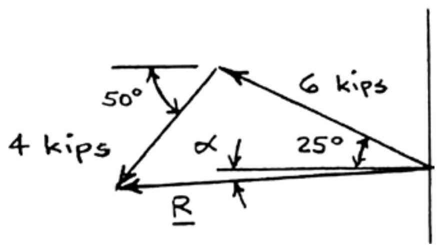
Two structural members B and C are bolted to bracket A. Knowing that both members are in tension and that P = 6 kips and Q = 4 kips, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

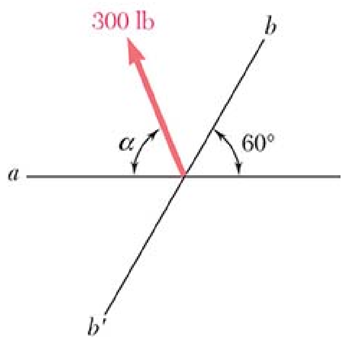
(*a*) Parallelogram law:



(*b*) Triangle rule:



We measure: $R = 8.03$ kips, $\alpha = 3.8°$ **R** $= 8.03$ kips ↙ 3.8° ◀

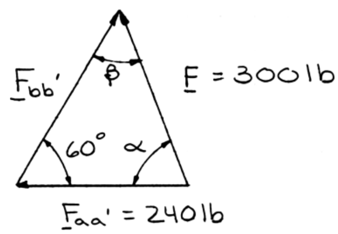


PROBLEM 2.5

The 300-lb force is to be resolved into components along lines *a-a′* and *b-b′*. (*a*) Determine the angle α by trigonometry knowing that the component along line *a-a′* is to be 240 lb. (*b*) What is the corresponding value of the component along *b-b′*?

SOLUTION

(*a*) Using the triangle rule and law of sines:



$$\frac{\sin\beta}{240 \text{ lb}} = \frac{\sin 60°}{300 \text{ lb}}$$

$$\sin\beta = 0.69282$$

$$\beta = 43.854°$$

$$\alpha + \beta + 60° = 180°$$

$$\alpha = 180° - 60° - 43.854°$$

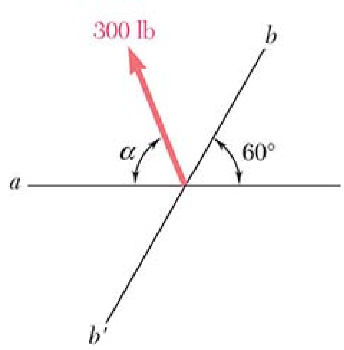
$$= 76.146°$$

$\alpha = 76.1°$ ◀

(*b*) Law of sines:

$$\frac{F_{bb'}}{\sin 76.146°} = \frac{300 \text{ lb}}{\sin 60°}$$

$F_{bb'} = 336$ lb ◀

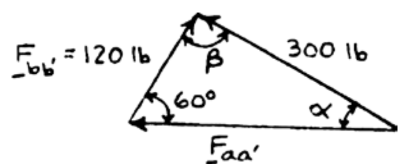


PROBLEM 2.6

The 300-lb force is to be resolved into components along lines *a-a*′ and *b-b*′. (*a*) Determine the angle α by trigonometry knowing that the component along line *b-b*′ is to be 120 lb. (*b*) What is the corresponding value of the component along *a-a*′?

SOLUTION

Using the triangle rule and law of sines:



(*a*)

$$\frac{\sin\alpha}{120 \text{ lb}} = \frac{\sin 60°}{300 \text{ lb}}$$

$$\sin\alpha = 0.34641$$

$$\alpha = 20.268°$$

$\alpha = 20.3°$ ◀

(*b*)

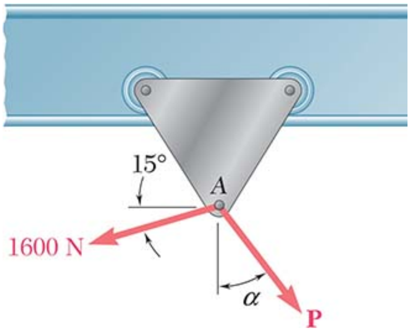
$$\alpha + \beta + 60° = 180°$$

$$\beta = 180° - 60° - 20.268°$$

$$= 99.732°$$

$$\frac{F_{aa'}}{\sin 99.732°} = \frac{300 \text{ lb}}{\sin 60°}$$

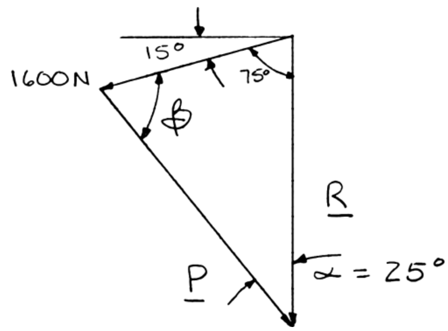
$F_{aa'} = 341$ lb ◀



PROBLEM 2.7

A trolley that moves along a horizontal beam is acted upon by two forces as shown. (*a*) Knowing that $\alpha = 25°$, determine by trigonometry the magnitude of the force **P** so that the resultant force exerted on the trolley is vertical. (*b*) What is the corresponding magnitude of the resultant?

SOLUTION

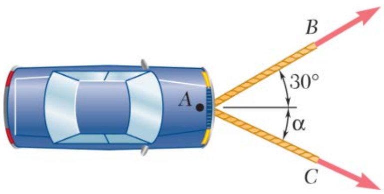


Using the triangle rule and the law of sines:

(*a*) $$\frac{1600\text{ N}}{\sin 25°} = \frac{P}{\sin 75°}$$ $P = 3660\text{ N}$ ◀

(*b*) $$25° + \beta + 75° = 180°$$
$$\beta = 180° - 25° - 75°$$
$$= 80°$$

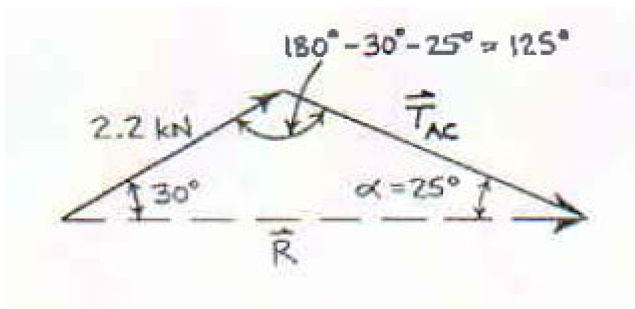
$$\frac{1600\text{ N}}{\sin 25°} = \frac{R}{\sin 80°}$$ $R = 3730\text{ N}$ ◀



PROBLEM 2.8

A disabled automobile is pulled by means of two ropes as shown. The tension in rope *AB* is 2.2 kN, and the angle α is 25°. Knowing that the resultant of the two forces applied at *A* is directed along the axis of the automobile, determine by trigonometry (*a*) the tension in rope *AC*, (*b*) the magnitude of the resultant of the two forces applied at *A*.

SOLUTION



Using the law of sines:

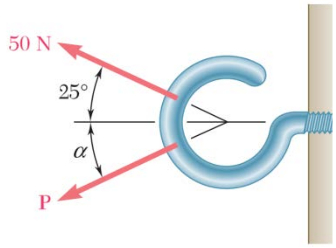
$$\frac{T_{AC}}{\sin 30°} = \frac{R}{\sin 125°} = \frac{2.2 \text{ kN}}{\sin 25°}$$

$$T_{AC} = 2.603 \text{ kN}$$

$$R = 4.264 \text{ kN}$$

(*a*) $T_{AC} = 2.60 \text{ kN}$ ◀

(*b*) $R = 4.26 \text{ kN}$ ◀

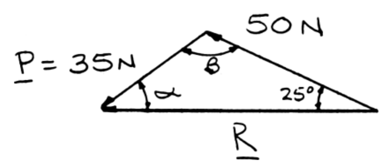


PROBLEM 2.9

Two forces are applied as shown to a hook support. Knowing that the magnitude of **P** is 35 N, determine by trigonometry (*a*) the required angle α if the resultant **R** of the two forces applied to the support is to be horizontal, (*b*) the corresponding magnitude of **R**.

SOLUTION

Using the triangle rule and law of sines:



(*a*)

$$\frac{\sin\alpha}{50\text{ N}} = \frac{\sin 25^\circ}{35\text{ N}}$$

$$\sin\alpha = 0.60374$$

$$\alpha = 37.138^\circ$$

$\alpha = 37.1^\circ$ ◀

(*b*)

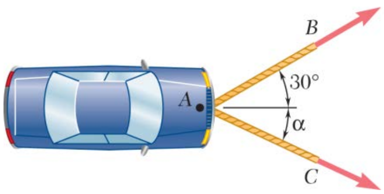
$$\alpha + \beta + 25^\circ = 180^\circ$$

$$\beta = 180^\circ - 25^\circ - 37.138^\circ$$

$$= 117.862^\circ$$

$$\frac{R}{\sin 117.862^\circ} = \frac{35\text{ N}}{\sin 25^\circ}$$

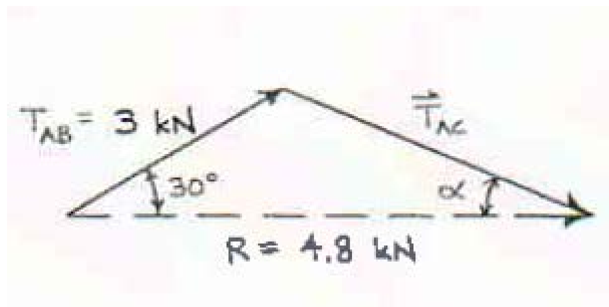
$R = 73.2\text{ N}$ ◀



PROBLEM 2.10

A disabled automobile is pulled by means of two ropes as shown. Knowing that the tension in rope *AB* is 3 kN, determine by trigonometry the tension in rope *AC* and the value of α so that the resultant force exerted at *A* is a 4.8-kN force directed along the axis of the automobile.

SOLUTION



Using the law of cosines:

$$T_{AC}^2 = (3\text{ kN})^2 + (4.8\text{ kN})^2 - 2(3\text{ kN})(4.8\text{ kN})\cos 30°$$

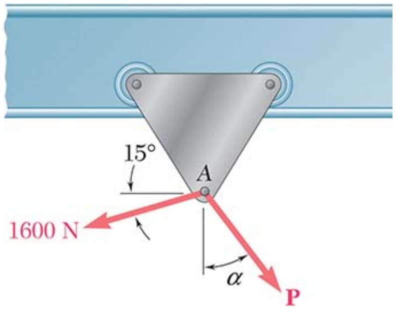
$$T_{AC} = 2.6643\text{ kN}$$

Using the law of sines:

$$\frac{\sin\alpha}{3\text{ kN}} = \frac{\sin 30°}{2.6643\text{ kN}}$$

$$\alpha = 34.3°$$

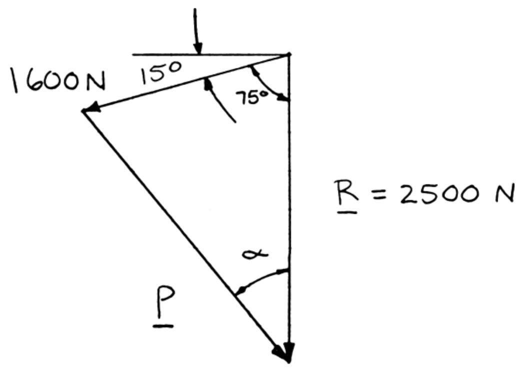
$$\mathbf{T}_{AC} = 2.66\text{ kN} \nwarrow 34.3° \blacktriangleleft$$



PROBLEM 2.11

A trolley that moves along a horizontal beam is acted upon by two forces as shown. Determine by trigonometry the magnitude and direction of the force **P** so that the resultant is a vertical force of 2500 N.

SOLUTION



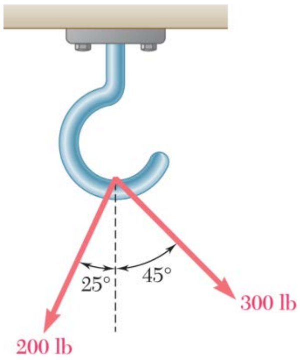
Using the law of cosines: $P^2 = (1600 \text{ N})^2 + (2500 \text{ N})^2 - 2(1600 \text{ N})(2500 \text{ N})\cos 75°$

$P = 2596 \text{ N}$

Using the law of sines: $\dfrac{\sin\alpha}{1600 \text{ N}} = \dfrac{\sin 75°}{2596 \text{ N}}$

$\alpha = 36.5°$

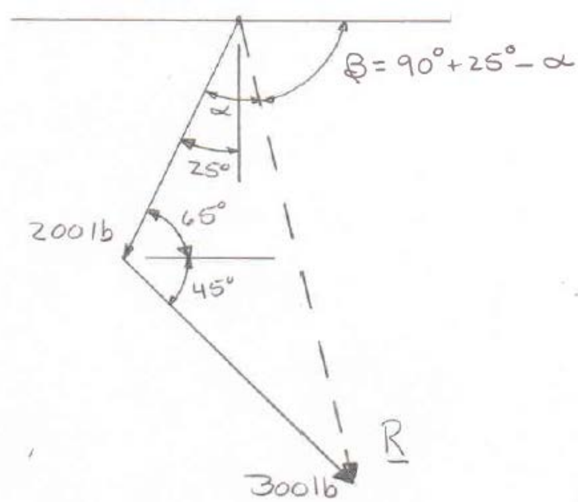
P is directed $90° - 36.5°$ or $53.5°$ below the horizontal. **P** = 2600 N ⦨ 53.5° ◀



PROBLEM 2.12

For the hook support shown, determine by trigonometry the magnitude and direction of the resultant of the two forces applied to the support.

SOLUTION



Using the law of cosines:

$$R^2 = (200\text{ lb})^2 + (300\text{ lb})^2 - 2(200\text{ lb})(300\text{ lb})\cos(45^\circ + 65^\circ)$$

$$R = 413.57\text{ lb}$$

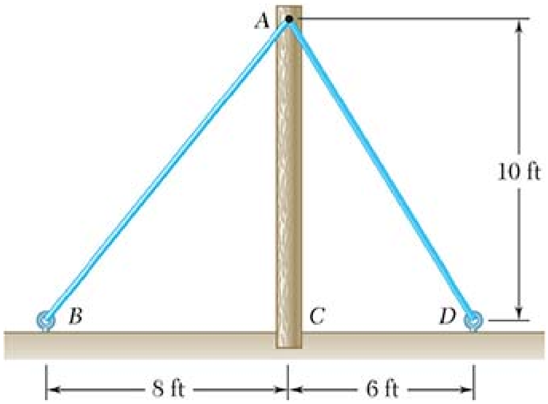
Using the law of sines:

$$\frac{\sin\alpha}{300\text{ lb}} = \frac{\sin(45^\circ + 65^\circ)}{413.57\text{ lb}}$$

$$\alpha = 42.972^\circ$$

$$\beta = 90^\circ + 25^\circ - 42.972^\circ$$

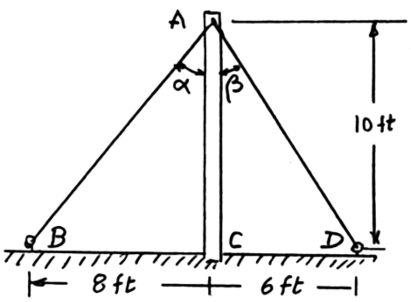
R = 414 lb ◥ 72.0° ◀

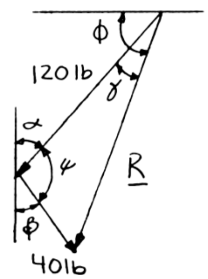


PROBLEM 2.13

The cable stays *AB* and *AD* help support pole *AC*. Knowing that the tension is 120 lb in *AB* and 40 lb in *AD*, determine graphically the magnitude and direction of the resultant of the forces exerted by the stays at *A* using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION





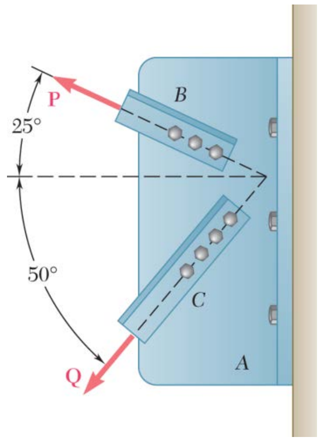
$$\tan\alpha = \frac{8}{10}$$
$$\alpha = 38.66^\circ$$
$$\tan\beta = \frac{6}{10}$$
$$\beta = 30.96^\circ$$

Using the triangle rule:
$$\alpha + \beta + \psi = 180^\circ$$
$$38.66^\circ + 30.96^\circ + \psi = 180^\circ$$
$$\psi = 110.38^\circ$$

Using the law of cosines:
$$R^2 = (120 \text{ lb})^2 + (40 \text{ lb})^2 - 2(120 \text{ lb})(40 \text{ lb})\cos 110.38^\circ$$
$$R = 139.08 \text{ lb}$$

Using the law of sines:
$$\frac{\sin\gamma}{40 \text{ lb}} = \frac{\sin 110.38^\circ}{139.08 \text{ lb}}$$
$$\gamma = 15.64^\circ$$
$$\phi = (90^\circ - \alpha) + \gamma$$
$$\phi = (90^\circ - 38.66^\circ) + 15.64^\circ$$
$$\phi = 66.98^\circ$$

$\mathbf{R} = 139.1 \text{ lb} \measuredangle 67.0^\circ$ ◀



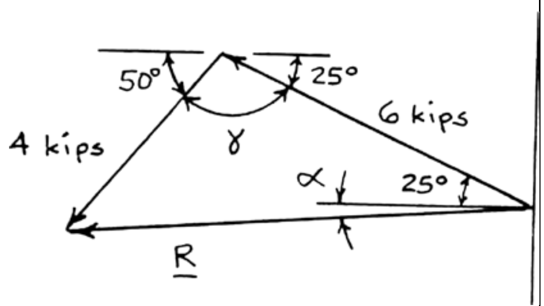
PROBLEM 2.14

Solve Problem 2.4 by trigonometry.

PROBLEM 2.4: Two structural members *B* and *C* are bolted to bracket *A*. Knowing that both members are in tension and that *P* = 6 kips and *Q* = 4 kips, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

Using the force triangle and the laws of cosines and sines:



We have:

$$\gamma = 180° - (50° + 25°)$$
$$= 105°$$

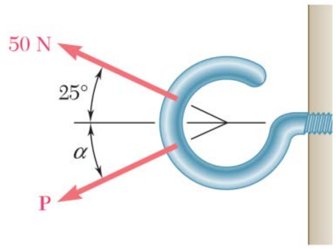
Then

$$R^2 = (4\text{ kips})^2 + (6\text{ kips})^2 - 2(4\text{ kips})(6\text{ kips})\cos 105°$$
$$= 64.423\text{ kips}^2$$
$$R = 8.0264\text{ kips}$$

And

$$\frac{4\text{ kips}}{\sin(25° + \alpha)} = \frac{8.0264\text{ kips}}{\sin 105°}$$
$$\sin(25° + \alpha) = 0.48137$$
$$25° + \alpha = 28.775°$$
$$\alpha = 3.775°$$

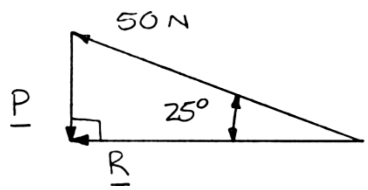
$\mathbf{R} = 8.03\text{ kips}$ ⦪ $3.8°$ ◀



PROBLEM 2.15

For the hook support of Prob. 2.9, determine by trigonometry (*a*) the magnitude and direction of the smallest force **P** for which the resultant **R** of the two forces applied to the support is horizontal, (*b*) the corresponding magnitude of **R**.

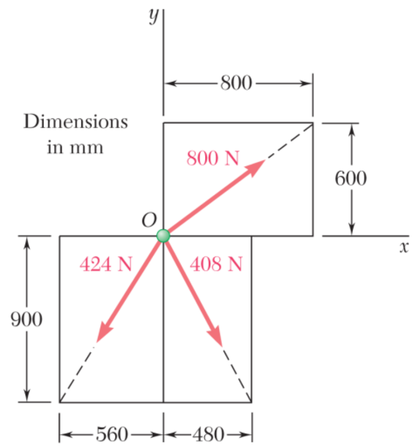
SOLUTION



The smallest force *P* will be perpendicular to *R*.

(*a*) $P = (50\text{ N})\sin 25°$ **P** = 21.1 N ↓ ◀

(*b*) $R = (50\text{ N})\cos 25°$ $R = 45.3$ N ◀

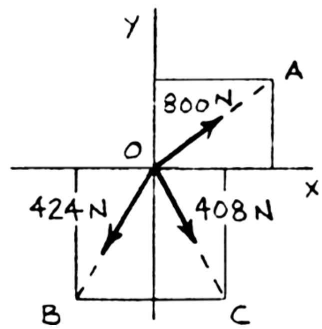


PROBLEM 2.16

Determine the x and y components of each of the forces shown.

SOLUTION

Compute the following distances:



$$OA = \sqrt{(600)^2 + (800)^2}$$
$$= 1000 \text{ mm}$$
$$OB = \sqrt{(560)^2 + (900)^2}$$
$$= 1060 \text{ mm}$$
$$OC = \sqrt{(480)^2 + (900)^2}$$
$$= 1020 \text{ mm}$$

800-N Force: $F_x = +(800 \text{ N})\frac{800}{1000}$ $\quad F_x = +640 \text{ N}$ ◀

$F_y = +(800 \text{ N})\frac{600}{1000}$ $\quad F_y = +480 \text{ N}$ ◀

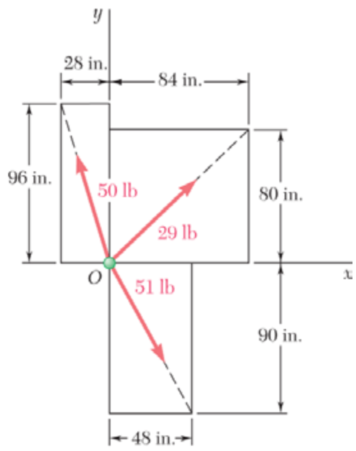
424-N Force: $F_x = -(424 \text{ N})\frac{560}{1060}$ $\quad F_x = -224 \text{ N}$ ◀

$F_y = -(424 \text{ N})\frac{900}{1060}$ $\quad F_y = -360 \text{ N}$ ◀

408-N Force: $F_x = +(408 \text{ N})\frac{480}{1020}$ $\quad F_x = +192.0 \text{ N}$ ◀

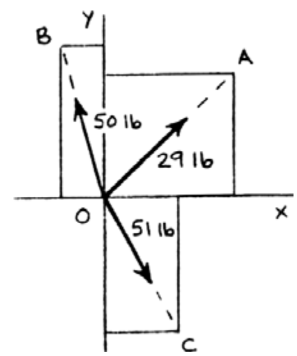
$F_y = -(408 \text{ N})\frac{900}{1020}$ $\quad F_y = -360 \text{ N}$ ◀

PROBLEM 2.17



Determine the x and y components of each of the forces shown.

SOLUTION



Compute the following distances:

$$OA = \sqrt{(84)^2 + (80)^2}$$
$$= 116 \text{ in.}$$
$$OB = \sqrt{(28)^2 + (96)^2}$$
$$= 100 \text{ in.}$$
$$OC = \sqrt{(48)^2 + (90)^2}$$
$$= 102 \text{ in.}$$

29-lb Force:

$$F_x = +(29 \text{ lb})\frac{84}{116} \qquad F_x = +21.0 \text{ lb} \blacktriangleleft$$

$$F_y = +(29 \text{ lb})\frac{80}{116} \qquad F_y = +20.0 \text{ lb} \blacktriangleleft$$

50-lb Force:

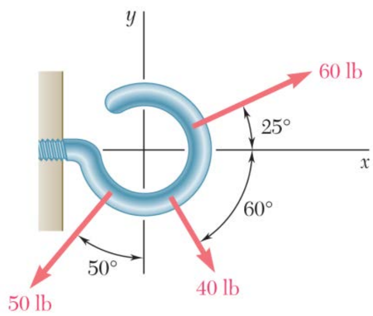
$$F_x = -(50 \text{ lb})\frac{28}{100} \qquad F_x = -14.00 \text{ lb} \blacktriangleleft$$

$$F_y = +(50 \text{ lb})\frac{96}{100} \qquad F_y = +48.0 \text{ lb} \blacktriangleleft$$

51-lb Force:

$$F_x = +(51 \text{ lb})\frac{48}{102} \qquad F_x = +24.0 \text{ lb} \blacktriangleleft$$

$$F_y = -(51 \text{ lb})\frac{90}{102} \qquad F_y = -45.0 \text{ lb} \blacktriangleleft$$

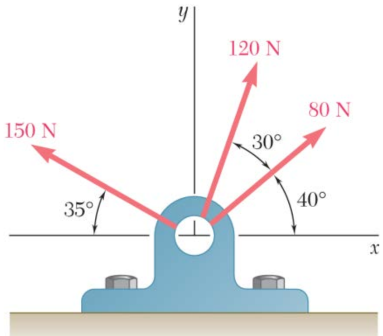


PROBLEM 2.18

Determine the x and y components of each of the forces shown.

SOLUTION

40-lb Force:	$F_x = +(40\text{ lb})\cos 60°$	$F_x = 20.0\text{ lb}$ ◀
	$F_y = -(40\text{ lb})\sin 60°$	$F_y = -34.6\text{ lb}$ ◀
50-lb Force:	$F_x = -(50\text{ lb})\sin 50°$	$F_x = -38.3\text{ lb}$ ◀
	$F_y = -(50\text{ lb})\cos 50°$	$F_y = -32.1\text{ lb}$ ◀
60-lb Force:	$F_x = +(60\text{ lb})\cos 25°$	$F_x = 54.4\text{ lb}$ ◀
	$F_y = +(60\text{ lb})\sin 25°$	$F_y = 25.4\text{ lb}$ ◀

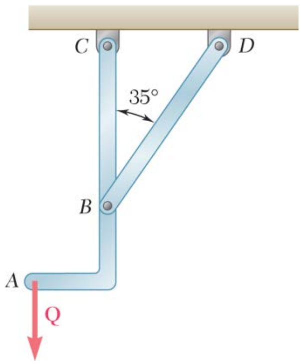


PROBLEM 2.19

Determine the x and y components of each of the forces shown.

SOLUTION

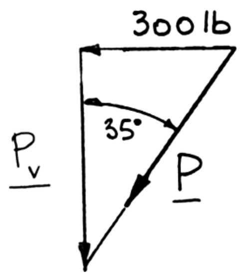
80-N Force:	$F_x = +(80\text{ N})\cos 40°$	$F_x = 61.3\text{ N}$ ◀
	$F_y = +(80\text{ N})\sin 40°$	$F_y = 51.4\text{ N}$ ◀
120-N Force:	$F_x = +(120\text{ N})\cos 70°$	$F_x = 41.0\text{ N}$ ◀
	$F_y = +(120\text{ N})\sin 70°$	$F_y = 112.8\text{ N}$ ◀
150-N Force:	$F_x = -(150\text{ N})\cos 35°$	$F_x = -122.9\text{ N}$ ◀
	$F_y = +(150\text{ N})\sin 35°$	$F_y = 86.0\text{ N}$ ◀



PROBLEM 2.20

Member *BD* exerts on member *ABC* a force **P** directed along line *BD*. Knowing that **P** must have a 300-lb horizontal component, determine (*a*) the magnitude of the force **P**, (*b*) its vertical component.

SOLUTION



(*a*)

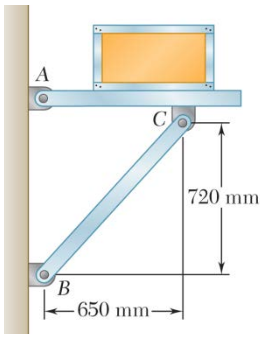
$$P \sin 35° = 300 \text{ lb}$$

$$P = \frac{300 \text{ lb}}{\sin 35°} \qquad P = 523 \text{ lb} \blacktriangleleft$$

(*b*) Vertical component

$$P_v = P \cos 35°$$

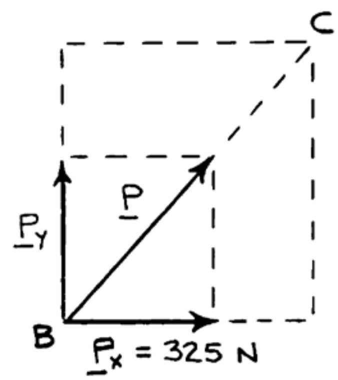
$$= (523 \text{ lb}) \cos 35° \qquad P_v = 428 \text{ lb} \blacktriangleleft$$



PROBLEM 2.21

Member *BC* exerts on member *AC* a force **P** directed along line *BC*. Knowing that **P** must have a 325-N horizontal component, determine (*a*) the magnitude of the force **P**, (*b*) its vertical component.

SOLUTION



$$BC = \sqrt{(650\text{ mm})^2 + (720\text{ mm})^2}$$
$$= 970\text{ mm}$$

(*a*)

$$P_x = P\left(\frac{650}{970}\right)$$

or

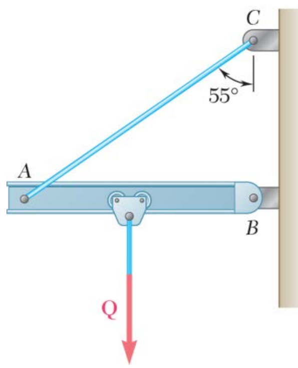
$$P = P_x\left(\frac{970}{650}\right)$$
$$= 325\text{ N}\left(\frac{970}{650}\right)$$
$$= 485\text{ N}$$

$P = 485$ N ◀

(*b*)

$$P_y = P\left(\frac{720}{970}\right)$$
$$= 485\text{ N}\left(\frac{720}{970}\right)$$
$$= 360\text{ N}$$

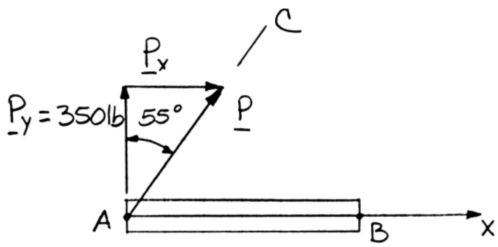
$P_y = 970$ N ◀



PROBLEM 2.22

Cable *AC* exerts on beam *AB* a force **P** directed along line *AC*. Knowing that **P** must have a 350-lb vertical component, determine (*a*) the magnitude of the force **P**, (*b*) its horizontal component.

SOLUTION



(*a*)

$$P = \frac{P_y}{\cos 55°}$$

$$= \frac{350 \text{ lb}}{\cos 55°}$$

$$= 610.21 \text{ lb}$$

$P = 610 \text{ lb}$ ◀

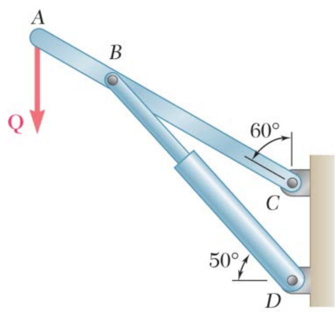
(*b*)

$$P_x = P \sin 55°$$

$$= (610.21 \text{ lb}) \sin 55°$$

$$= 499.85 \text{ lb}$$

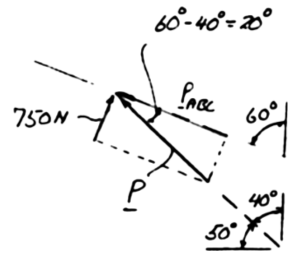
$P_x = 500 \text{ lb}$ ◀



PROBLEM 2.23

The hydraulic cylinder *BD* exerts on member *ABC* a force **P** directed along line *BD*. Knowing that **P** must have a 750-N component perpendicular to member *ABC*, determine (*a*) the magnitude of the force **P**, (*b*) its component parallel to *ABC*.

SOLUTION



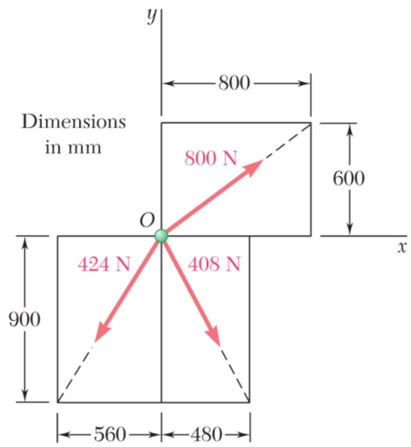
(*a*) $$750\text{ N} = P\sin 20°$$

$$P = 2192.9\text{ N}$$ $P = 2190\text{ N}$ ◀

(*b*) $$P_{ABC} = P\cos 20°$$

$$= (2192.9\text{ N})\cos 20°$$ $P_{ABC} = 2060\text{ N}$ ◀

PROBLEM 2.24



Determine the resultant of the three forces of Problem 2.16.

PROBLEM 2.16 Determine the x and y components of each of the forces shown.

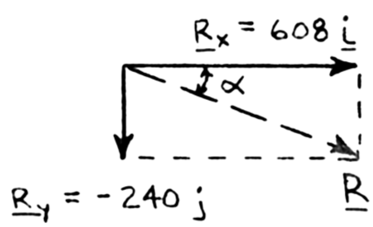
SOLUTION

Components of the forces were determined in Problem 2.16:

Force	x Comp. (N)	y Comp. (N)
800 lb	+640	+480
424 lb	–224	–360
408 lb	+192	–360
	$R_x = +608$	$R_y = -240$

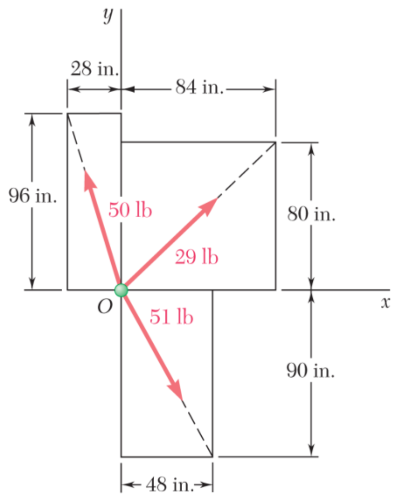
$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$
$$= (608 \text{ lb})\mathbf{i} + (-240 \text{ lb})\mathbf{j}$$

$$\tan\alpha = \frac{R_y}{R_x}$$
$$= \frac{240}{608}$$
$$\alpha = 21.541°$$
$$R = \frac{240 \text{ N}}{\sin(21.541°)}$$
$$= 653.65 \text{ N}$$



R = 654 N 21.5° ◀

PROBLEM 2.25



Determine the resultant of the three forces of Problem 2.17.

PROBLEM 2.17 Determine the x and y components of each of the forces shown.

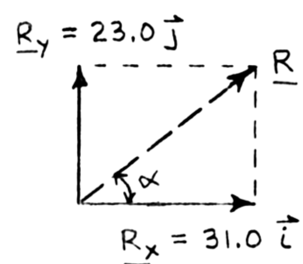
SOLUTION

Components of the forces were determined in Problem 2.17:

Force	x Comp. (lb)	y Comp. (lb)
29 lb	+21.0	+20.0
50 lb	–14.00	+48.0
51 lb	+24.0	–45.0
	$R_x = +31.0$	$R_y = +23.0$

$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$

$$= (31.0\text{ lb})\mathbf{i} + (23.0\text{ lb})\mathbf{j}$$



$$\tan\alpha = \frac{R_y}{R_x}$$

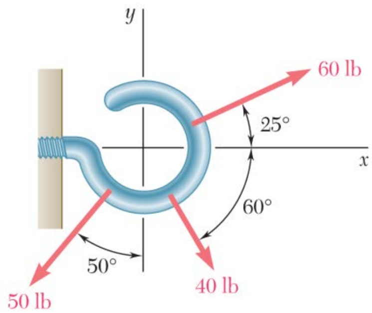
$$= \frac{23.0}{31.0}$$

$$\alpha = 36.573°$$

$$R = \frac{23.0\text{ lb}}{\sin(36.573°)}$$

$$= 38.601\text{ lb}$$

$\mathbf{R} = 38.6\text{ lb} \measuredangle 36.6°$ ◀



PROBLEM 2.26

Determine the resultant of the three forces of Problem 2.18.

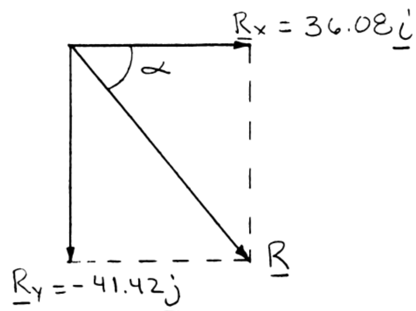
PROBLEM 2.18 Determine the *x* and *y* components of each of the forces shown.

SOLUTION

Force	*x* Comp. (lb)	*y* Comp. (lb)
40 lb	+20.00	–34.64
50 lb	–38.30	–32.14
60 lb	+54.38	+25.36
	$R_x = +36.08$	$R_y = -41.42$

$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$

$$= (+36.08\text{ lb})\mathbf{i} + (-41.42\text{ lb})\mathbf{j}$$



$$\tan\alpha = \frac{R_y}{R_x}$$

$$\tan\alpha = \frac{41.42\text{ lb}}{36.08\text{ lb}}$$

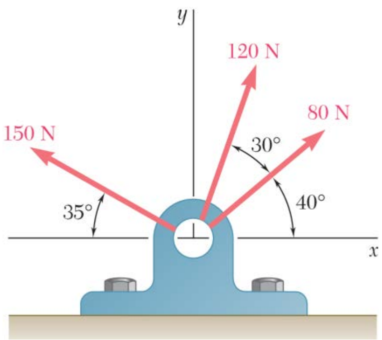
$$\tan\alpha = 1.14800$$

$$\alpha = 48.942°$$

$$R = \frac{41.42\text{ lb}}{\sin 48.942°}$$

$\mathbf{R}$ = 54.9 lb ⦪ 48.9° ◀

PROBLEM 2.27



Determine the resultant of the three forces of Problem 2.19.

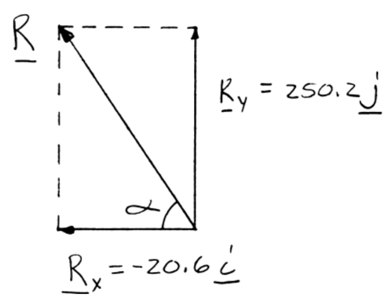
PROBLEM 2.19 Determine the x and y components of each of the forces shown.

SOLUTION

Components of the forces were determined in Problem 2.19:

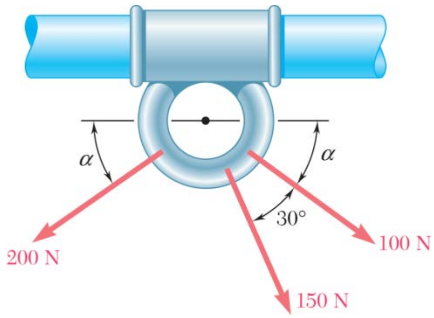
Force	x Comp. (N)	y Comp. (N)
80 N	+61.3	+51.4
120 N	+41.0	+112.8
150 N	–122.9	+86.0
	$R_x = -20.6$	$R_y = +250.2$

$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$
$$= (-20.6\text{ N})\mathbf{i} + (250.2\text{ N})\mathbf{j}$$



$$\tan\alpha = \frac{R_y}{R_x}$$
$$\tan\alpha = \frac{250.2\text{ N}}{20.6\text{ N}}$$
$$\tan\alpha = 12.1456$$
$$\alpha = 85.293°$$
$$R = \frac{250.2\text{ N}}{\sin 85.293°}$$

R = 251 N ⦪ 85.3° ◀



PROBLEM 2.28

For the collar loaded as shown, determine (*a*) the required value of α if the resultant of the three forces shown is to be vertical, (*b*) the corresponding magnitude of the resultant.

SOLUTION

$$R_x = \Sigma F_x$$
$$= (100\text{ N})\cos\alpha + (150\text{ N})\cos(\alpha + 30°) - (200\text{ N})\cos\alpha$$
$$R_x = -(100\text{ N})\cos\alpha + (150\text{ N})\cos(\alpha + 30°) \qquad (1)$$

$$R_y = \Sigma F_y$$
$$= -(100\text{ N})\sin\alpha - (150\text{ N})\sin(\alpha + 30°) - (200\text{ N})\sin\alpha$$
$$R_y = -(300\text{ N})\sin\alpha - (150\text{ N})\sin(\alpha + 30°) \qquad (2)$$

(*a*) For **R** to be vertical, we must have $R_x = 0$. We make $R_x = 0$ in Eq. (1):

$$-100\cos\alpha + 150\cos(\alpha + 30°) = 0$$
$$-100\cos\alpha + 150(\cos\alpha\cos 30° - \sin\alpha\sin 30°) = 0$$
$$29.904\cos\alpha = 75\sin\alpha$$

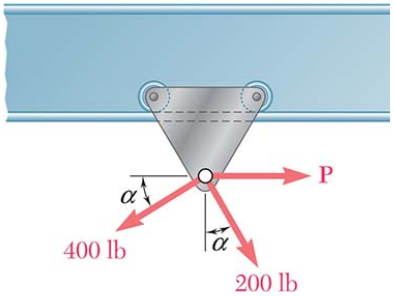
$$\tan\alpha = \frac{29.904}{75}$$
$$= 0.39872$$
$$\alpha = 21.738°$$

$\alpha = 21.7°$ ◀

(*b*) Substituting for α in Eq. (2):

$$R_y = -300\sin 21.738° - 150\sin 51.738°$$
$$= -228.89\text{ N}$$
$$R = |R_y| = 228.89\text{ N}$$

$R = 229\text{ N}$ ◀



PROBLEM 2.29

A hoist trolley is subjected to the three forces shown. Knowing that $\alpha = 40°$, determine (a) the required magnitude of the force **P** if the resultant of the three forces is to be vertical, (b) the corresponding magnitude of the resultant.

SOLUTION

$$R_x = \xrightarrow{+} \Sigma F_x = P + (200 \text{ lb})\sin 40° - (400 \text{ lb})\cos 40°$$

$$R_x = P - 177.860 \text{ lb} \quad (1)$$

$$R_y = +\!\downarrow \Sigma F_y = (200 \text{ lb})\cos 40° + (400 \text{ lb})\sin 40°$$

$$R_y = 410.32 \text{ lb} \quad (2)$$

(a) For **R** to be vertical, we must have $R_x = 0$.

Set $R_x = 0$ in Eq. (1)

$$0 = P - 177.860 \text{ lb}$$

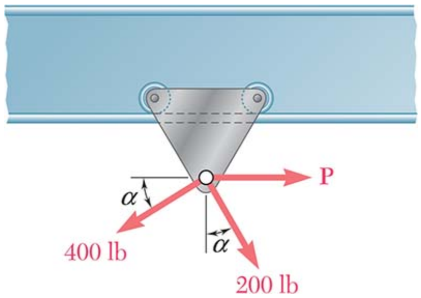
$$P = 177.860 \text{ lb}$$

$P = 177.9$ lb ◀

(b) Since **R** is to be vertical:

$$R = R_y = 410 \text{ lb}$$

$R = 410$ lb ◀



PROBLEM 2.30

A hoist trolley is subjected to the three forces shown. Knowing that P = 250 lb, determine (a) the required value of α if the resultant of the three forces is to be vertical, (b) the corresponding magnitude of the resultant.

SOLUTION

$$R_x = \xrightarrow{+} \Sigma F_x = 250 \text{ lb} + (200 \text{ lb})\sin\alpha - (400 \text{ lb})\cos\alpha$$

$$R_x = 250 \text{ lb} + (200 \text{ lb})\sin\alpha - (400 \text{ lb})\cos\alpha \qquad (1)$$

$$R_y = +\!\downarrow \Sigma F_y = (200 \text{ lb})\cos\alpha + (400 \text{ lb})\sin\alpha$$

(a) For **R** to be vertical, we must have $R_x = 0$.

Set $\quad R_x = 0$ in Eq. (1)

$$0 = 250 \text{ lb} + (200 \text{ lb})\sin\alpha - (400 \text{ lb})\cos\alpha$$

$$(400 \text{ lb})\cos\alpha = (200 \text{ lb})\sin\alpha + 250 \text{ lb}$$

$$2\cos\alpha = \sin\alpha + 1.25$$

$$4\cos^2\alpha = \sin^2\alpha + 2.5\sin\alpha + 1.5625$$

$$4(1-\sin^2\alpha) = \sin^2\alpha + 2.5\sin\alpha + 1.5625$$

$$0 = 5\sin^2\alpha + 2.5\sin\alpha - 2.4375$$

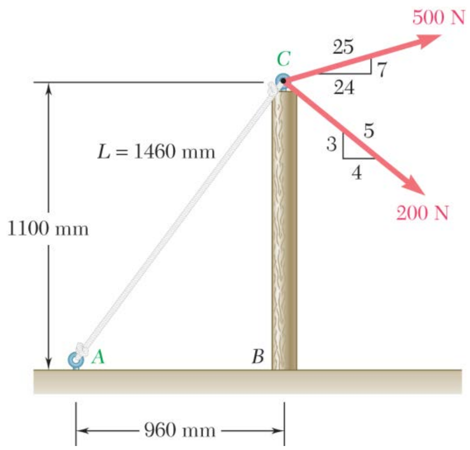
Using the quadratic formula to solve for the roots gives

$$\sin\alpha = 0.49162$$

or $\quad \alpha = 29.447° \qquad \alpha = 29.4°$ ◀

(b) Since **R** is to be vertical:

$$R = R_y = (200 \text{ lb})\cos 29.447° + (400 \text{ lb})\sin 29.447° \qquad \mathbf{R} = 371 \text{ lb}$$ ◀



PROBLEM 2.31

For the post loaded as shown, determine (*a*) the required tension in rope *AC* if the resultant of the three forces exerted at point *C* is to be horizontal, (*b*) the corresponding magnitude of the resultant.

SOLUTION

$$R_x = \Sigma F_x = -\frac{960}{1460}T_{AC} + \frac{24}{25}(500\text{ N}) + \frac{4}{5}(200\text{ N})$$

$$R_x = -\frac{48}{73}T_{AC} + 640\text{ N} \qquad (1)$$

$$R_y = \Sigma F_y = -\frac{1100}{1460}T_{AC} + \frac{7}{25}(500\text{ N}) - \frac{3}{5}(200\text{ N})$$

$$R_y = -\frac{55}{73}T_{AC} + 20\text{ N} \qquad (2)$$

(*a*) For **R** to be horizontal, we must have $R_y = 0$.

Set $R_y = 0$ in Eq. (2):

$$-\frac{55}{73}T_{AC} + 20\text{ N} = 0$$

$$T_{AC} = 26.545\text{ N}$$

$T_{AC} = 26.5\text{ N}$ ◀

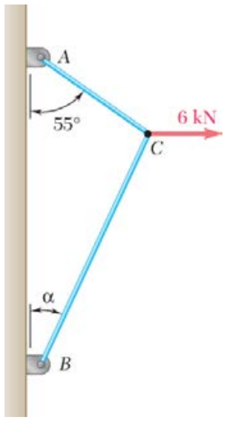
(*b*) Substituting for T_{AC} into Eq. (1) gives

$$R_x = -\frac{48}{73}(26.545\text{ N}) + 640\text{ N}$$

$$R_x = 622.55\text{ N}$$

$$R = R_x = 623\text{ N}$$

$R = 623\text{ N}$ ◀

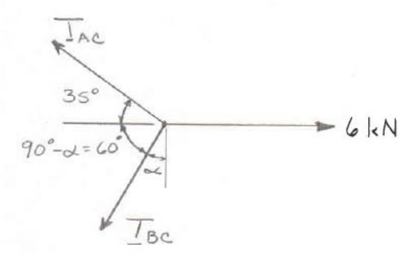


PROBLEM 2.32

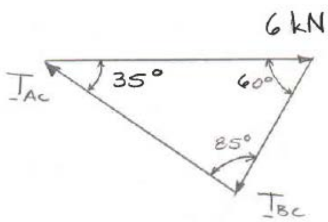
Two cables are tied together at C and are loaded as shown. Knowing that α = 30°, determine the tension (a) in cable AC, (b) in cable BC.

SOLUTION

Free-Body Diagram



Force Triangle

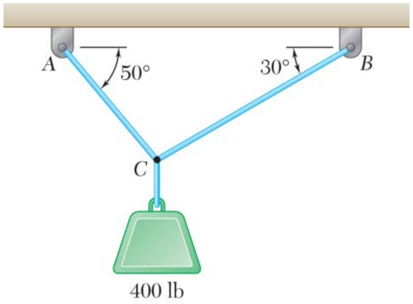


Law of sines:

$$\frac{T_{AC}}{\sin 60^\circ} = \frac{T_{BC}}{\sin 35^\circ} = \frac{6\text{ kN}}{\sin 85^\circ}$$

(a) $$T_{AC} = \frac{6\text{ kN}}{\sin 85^\circ}(\sin 60^\circ)$$ $T_{AC} = 5.22$ kN ◀

(b) $$T_{BC} = \frac{6\text{ kN}}{\sin 85^\circ}(\sin 35^\circ)$$ $T_{BC} = 3.45$ kN ◀

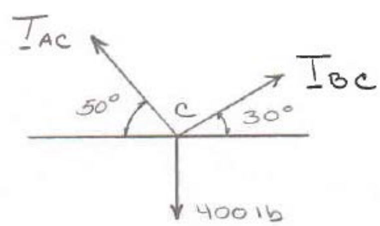


PROBLEM 2.33

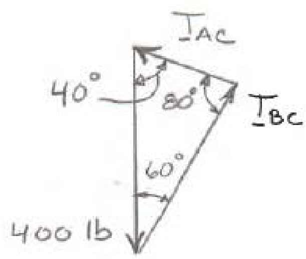
Two cables are tied together at C and are loaded as shown. Determine the tension (a) in cable AC, (b) in cable BC.

SOLUTION

Free-Body Diagram



Force Triangle



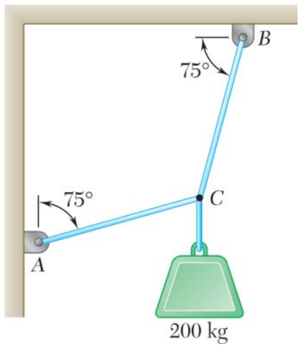
Law of sines:

$$\frac{T_{AC}}{\sin 60^\circ} = \frac{T_{BC}}{\sin 40^\circ} = \frac{400 \text{ lb}}{\sin 80^\circ}$$

(a) $$T_{AC} = \frac{400 \text{ lb}}{\sin 80^\circ}(\sin 60^\circ)$$ $T_{AC} = 352 \text{ lb}$ ◀

(b) $$T_{BC} = \frac{400 \text{ lb}}{\sin 80^\circ}(\sin 40^\circ)$$ $T_{BC} = 261 \text{ lb}$ ◀

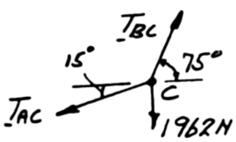
PROBLEM 2.34



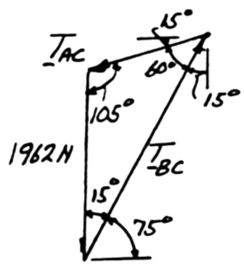
Two cables are tied together at C and are loaded as shown. Determine the tension (a) in cable AC, (b) in cable BC.

SOLUTION

Free-Body Diagram



Force Triangle



$$W = mg$$
$$= (200\text{ kg})(9.81\text{ m/s}^2)$$
$$= 1962\text{ N}$$

Law of sines:

$$\frac{T_{AC}}{\sin 15°} = \frac{T_{BC}}{\sin 105°} = \frac{1962\text{ N}}{\sin 60°}$$

(a)

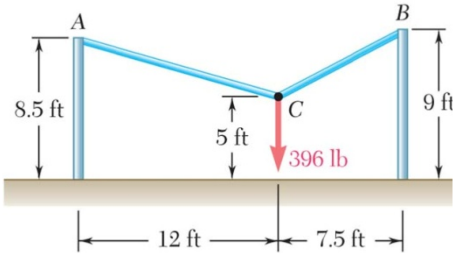
$$T_{AC} = \frac{(1962\text{ N})\sin 15°}{\sin 60°}$$

$T_{AC} = 586$ N ◀

(b)

$$T_{BC} = \frac{(1962\text{ N})\sin 105°}{\sin 60°}$$

$T_{BC} = 2190$ N ◀

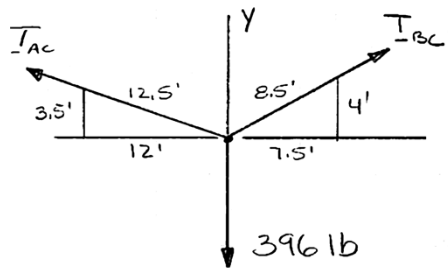


PROBLEM 2.35

Two cables are tied together at *C* and loaded as shown. Determine the tension (*a*) in cable *AC*, (*b*) in cable *BC*.

SOLUTION

Free Body Diagram at *C*:



$$\Sigma F_x = 0: \quad -\frac{12 \text{ ft}}{12.5 \text{ ft}} T_{AC} + \frac{7.5 \text{ ft}}{8.5 \text{ ft}} T_{BC} = 0$$

$$T_{BC} = 1.08800 T_{AC}$$

$$\Sigma F_y = 0: \quad \frac{3.5 \text{ ft}}{12 \text{ ft}} T_{AC} + \frac{4 \text{ ft}}{8.5 \text{ ft}} T_{BC} - 396 \text{ lb} = 0$$

(*a*)

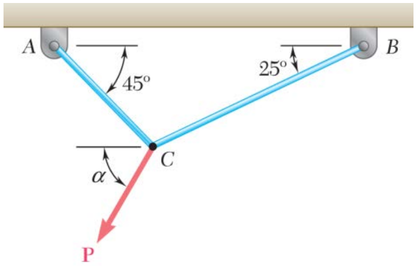
$$\frac{3.5 \text{ ft}}{12.5 \text{ ft}} T_{AC} + \frac{4 \text{ ft}}{8.5 \text{ ft}} (1.08800 T_{AC}) - 396 \text{ lb} = 0$$

$$(0.28000 + 0.51200) T_{AC} = 396 \text{ lb}$$

$$T_{AC} = 500.0 \text{ lb} \qquad T_{AC} = 500 \text{ lb} \blacktriangleleft$$

(*b*)

$$T_{BC} = (1.08800)(500.0 \text{ lb}) \qquad T_{BC} = 544 \text{ lb} \blacktriangleleft$$

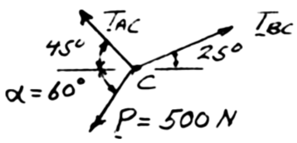


PROBLEM 2.36

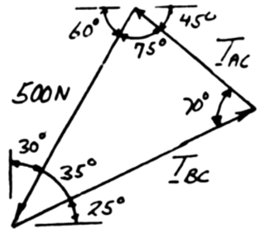
Two cables are tied together at C and are loaded as shown. Knowing that $\mathbf{P}$ = 500 N and α = 60°, determine the tension in (a) in cable AC, (b) in cable BC.

SOLUTION

Free-Body Diagram



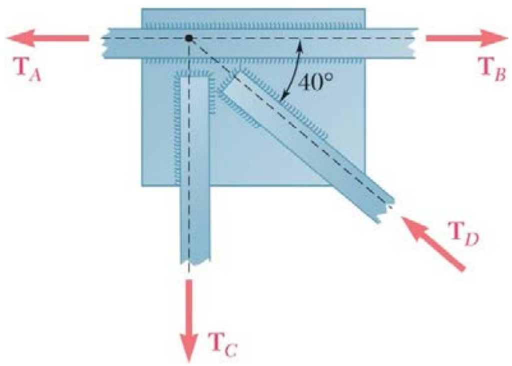
Force Triangle



Law of sines: $$\frac{T_{AC}}{\sin 35°} = \frac{T_{BC}}{\sin 75°} = \frac{500\text{ N}}{\sin 70°}$$

(a) $$T_{AC} = \frac{500\text{ N}}{\sin 70°}\sin 35°$$ $T_{AC} = 305$ N ◀

(b) $$T_{BC} = \frac{500\text{ N}}{\sin 70°}\sin 75°$$ $T_{BC} = 514$ N ◀

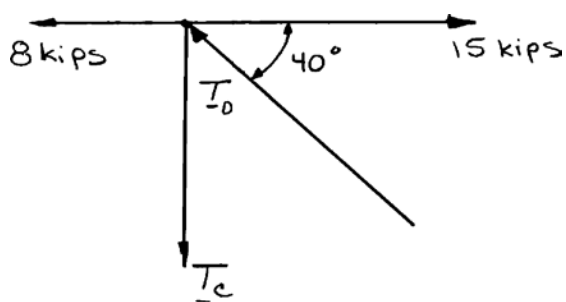


PROBLEM 2.37

Two forces of magnitude T_A = 8 kips and T_B = 15 kips are applied as shown to a welded connection. Knowing that the connection is in equilibrium, determine the magnitudes of the forces T_C and T_D.

SOLUTION

Free-Body Diagram



$\xrightarrow{+} \Sigma F_x = 0 \qquad 15 \text{ kips} - 8 \text{ kips} - T_D \cos 40° = 0$

$$T_D = 9.1379 \text{ kips}$$

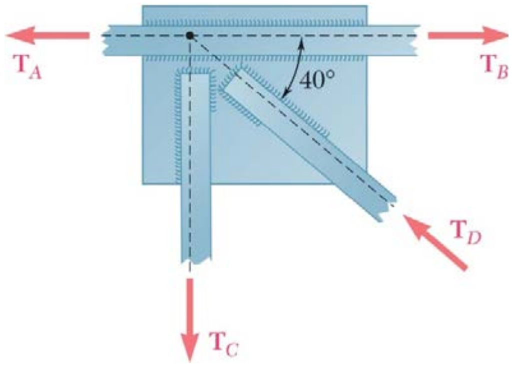
$+\uparrow \Sigma F_y = 0 \qquad T_D \sin 40° - T_C = 0$

$$(9.1379 \text{ kips}) \sin 40° - T_C = 0$$

$$T_C = 5.8737 \text{ kips}$$

$T_C = 5.87$ kips ◀

$T_D = 9.14$ kips ◀

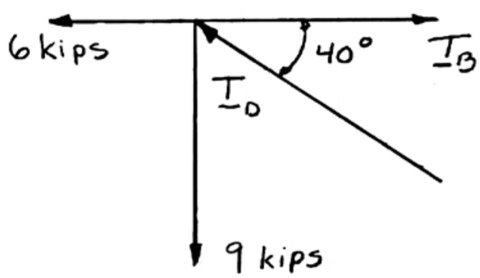


PROBLEM 2.38

Two forces of magnitude T_A = 6 kips and T_C = 9 kips are applied as shown to a welded connection. Knowing that the connection is in equilibrium, determine the magnitudes of the forces T_B and T_D.

SOLUTION

Free-Body Diagram



$\xrightarrow{+} \Sigma F_x = 0$ $$T_B - 6\text{ kips} - T_D \cos 40° = 0 \quad (1)$$

$+\uparrow \Sigma F_y = 0$ $$T_D \sin 40° - 9\text{ kips} = 0$$

$$T_D = \frac{9\text{ kips}}{\sin 40°}$$

$$T_D = 14.0015\text{ kips}$$

Substituting for T_D into Eq. (1) gives:

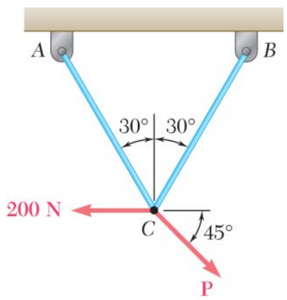
$$T_B - 6\text{ kips} - (14.0015\text{ kips})\cos 40° = 0$$

$$T_B = 16.7258\text{ kips}$$

$$T_B = 16.73\text{ kips} \blacktriangleleft$$

$$T_D = 14.00\text{ kips} \blacktriangleleft$$

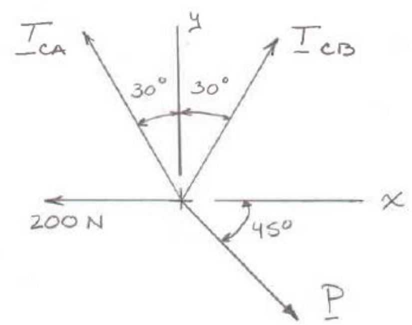
PROBLEM 2.39



Two cables are tied together at C and are loaded as shown. Knowing that P = 300 N, determine the tension in cables AC and BC.

SOLUTION

Free-Body Diagram



$\xrightarrow{+} \Sigma F_x = 0 \qquad -T_{CA}\sin 30^\circ + T_{CB}\sin 30^\circ - P\cos 45^\circ - 200\text{N} = 0$

For $P = 200\text{N}$ we have,

$$-0.5T_{CA} + 0.5T_{CB} + 212.13 - 200 = 0 \quad (1)$$

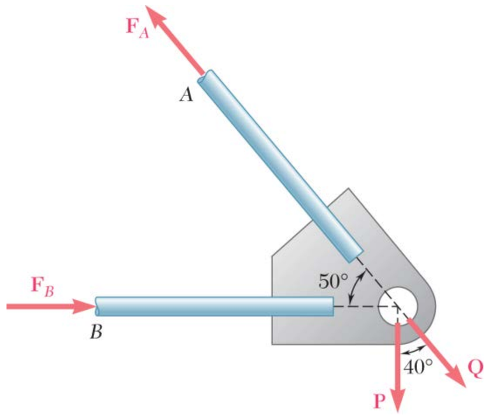
$+\uparrow \Sigma F_y = 0 \qquad T_{CA}\cos 30^\circ - T_{CB}\cos 30^\circ - P\sin 45^\circ = 0$

$$0.86603T_{CA} + 0.86603T_{CB} - 212.13 = 0 \quad (2)$$

Solving equations (1) and (2) simultaneously gives,

$T_{CA} = 134.6\text{ N}$ ◀

$T_{CB} = 110.4\text{ N}$ ◀

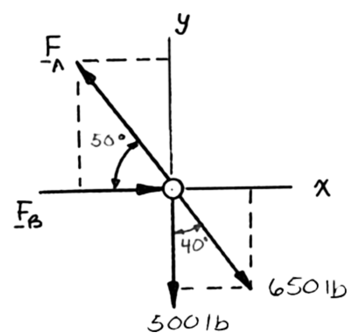


PROBLEM 2.40

Two forces **P** and **Q** are applied as shown to an aircraft connection. Knowing that the connection is in equilibrium and that $P = 500$ lb and $Q = 650$ lb, determine the magnitudes of the forces exerted on the rods *A* and *B*.

SOLUTION

Free-Body Diagram



Resolving the forces into *x*- and *y*-directions:

$$\mathbf{R} = \mathbf{P} + \mathbf{Q} + \mathbf{F}_A + \mathbf{F}_B = 0$$

Substituting components:

$$\mathbf{R} = -(500\text{ lb})\mathbf{j} + [(650\text{ lb})\cos 50°]\mathbf{i} - [(650\text{ lb})\sin 50°]\mathbf{j} + F_B\mathbf{i} - (F_A\cos 50°)\mathbf{i} + (F_A\sin 50°)\mathbf{j} = 0$$

In the *y*-direction (one unknown force):

$$-500\text{ lb} - (650\text{ lb})\sin 50° + F_A\sin 50° = 0$$

Thus,

$$F_A = \frac{500\text{ lb} + (650\text{ lb})\sin 50°}{\sin 50°}$$

$$= 1302.70\text{ lb}$$

$F_A = 1303$ lb ◀

In the *x*-direction:

$$(650\text{ lb})\cos 50° + F_B - F_A\cos 50° = 0$$

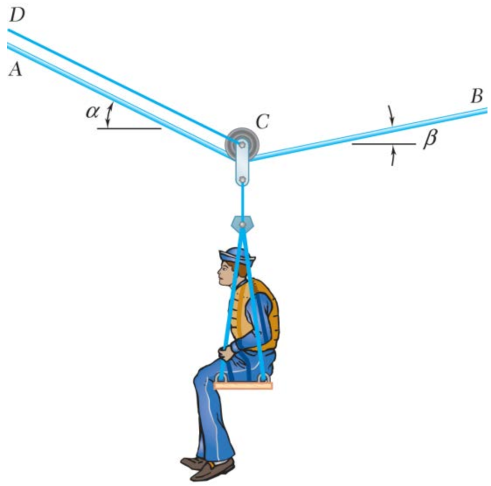
Thus,

$$F_B = F_A\cos 50° - (650\text{ lb})\cos 50°$$

$$= (1302.70\text{ lb})\cos 50° - (650\text{ lb})\cos 50°$$

$$= 419.55\text{ lb}$$

$F_B = 420$ lb ◀

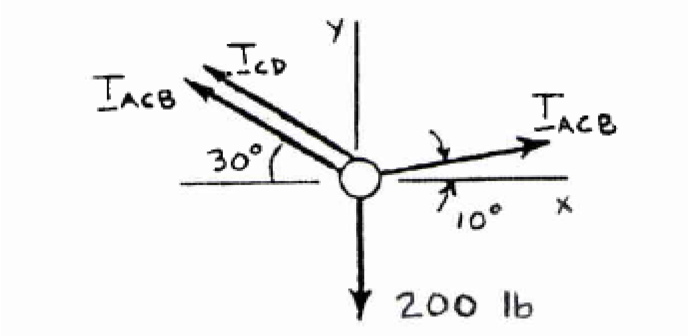


PROBLEM 2.41

A sailor is being rescued using a boatswain's chair that is suspended from a pulley that can roll freely on the support cable *ACB* and is pulled at a constant speed by cable *CD*. Knowing that $\alpha = 30°$ and $\beta = 10°$ and that the combined weight of the boatswain's chair and the sailor is 200 lb, determine the tension (*a*) in the support cable *ACB*, (*b*) in the traction cable *CD*.

SOLUTION

Free-Body Diagram



$$\xrightarrow{+} \Sigma F_x = 0: \quad T_{ACB} \cos 10° - T_{ACB} \cos 30° - T_{CD} \cos 30° = 0$$

$$T_{CD} = 0.137158 T_{ACB} \tag{1}$$

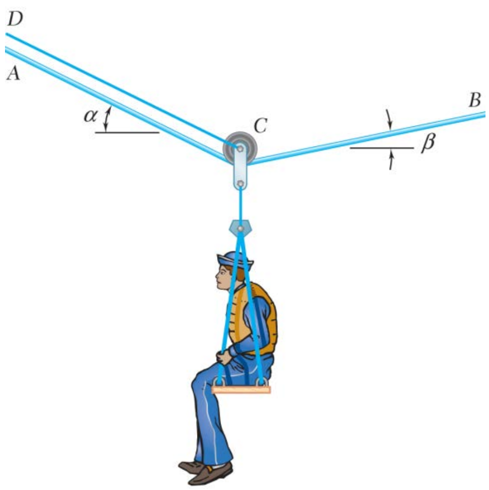
$$+\!\uparrow \Sigma F_y = 0: \quad T_{ACB} \sin 10° + T_{ACB} \sin 30° + T_{CD} \sin 30° - 200 = 0$$

$$0.67365 T_{ACB} + 0.5 T_{CD} = 200 \tag{2}$$

(*a*) Substitute (1) into (2): $0.67365 T_{ACB} + 0.5(0.137158 T_{ACB}) = 200$

$T_{ACB} = 269.46$ lb $\qquad T_{ACB} = 269$ lb ◀

(*b*) From (1): $T_{CD} = 0.137158(269.46 \text{ lb})$ $\qquad T_{CD} = 37.0$ lb ◀

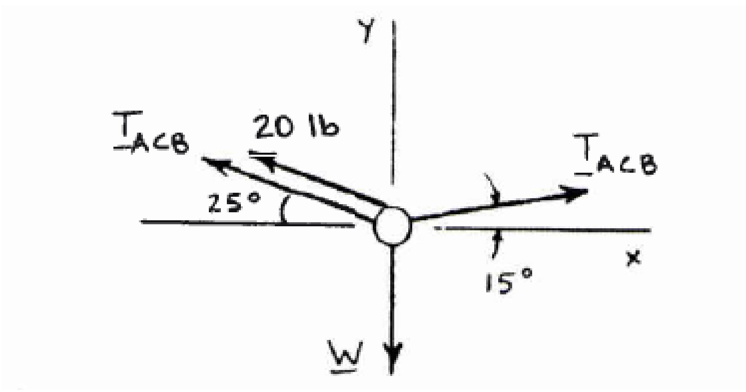


PROBLEM 2.42

A sailor is being rescued using a boatswain's chair that is suspended from a pulley that can roll freely on the support cable *ACB* and is pulled at a constant speed by cable *CD*. Knowing that $\alpha = 25°$ and $\beta = 15°$ and that the tension in cable *CD* is 20 lb, determine (*a*) the combined weight of the boatswain's chair and the sailor, (*b*) the tension in the support cable *ACB*.

SOLUTION

Free-Body Diagram



$$\xrightarrow{+} \Sigma F_x = 0: \quad T_{ACB}\cos 15° - T_{ACB}\cos 25° - (20\text{ lb})\cos 25° = 0$$

$$T_{ACB} = 304.04\text{ lb}$$

$$+\uparrow \Sigma F_y = 0: \quad (304.04\text{ lb})\sin 15° + (304.04\text{ lb})\sin 25°$$

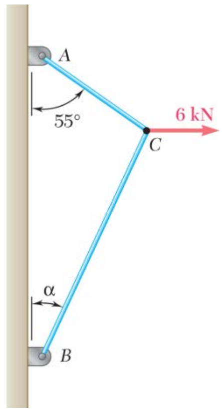
$$+(20\text{ lb})\sin 25° - W = 0$$

$$W = 215.64\text{ lb}$$

(*a*) $W = 216\text{ lb}$ ◀

(*b*) $T_{ACB} = 304\text{ lb}$ ◀

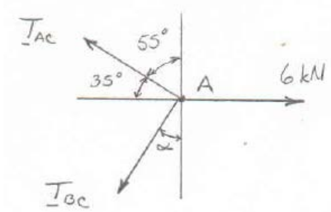
PROBLEM 2.43



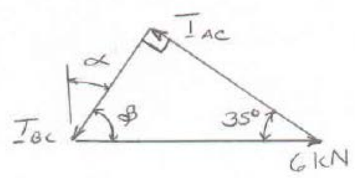
For the cables of prob. 2.32, find the value of α for which the tension is as small as possible (*a*) in cable *bc*, (*b*) in both cables simultaneously. In each case determine the tension in each cable.

SOLUTION

Free-Body Diagram



Force Triangle



(*a*) For a minimum tension in cable *BC*, set angle between cables to 90 degrees.

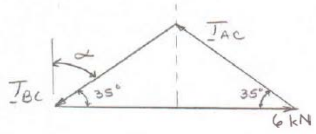
By inspection, $\alpha = 35.0^\circ$ ◀

$$T_{AC} = (6\text{ kN})\cos 35^\circ \qquad T_{AC} = 4.91\text{ kN} \blacktriangleleft$$

$$T_{BC} = (6\text{ kN})\sin 35^\circ \qquad T_{BC} = 3.44\text{ kN} \blacktriangleleft$$

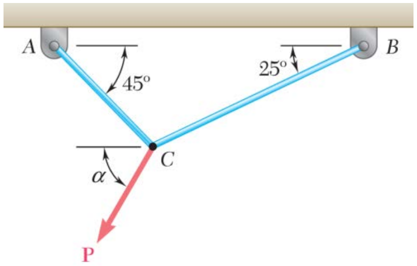
(*b*) For equal tension in both cables, the force triangle will be an isosceles.

Therefore, by inspection, $\alpha = 55.0^\circ$ ◀



$$T_{AC} = T_{BC} = (1/2)\frac{6\text{ kN}}{\cos 35^\circ} \qquad T_{AC} = T_{BC} = 3.66\text{ kN} \blacktriangleleft$$

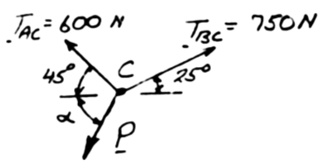
PROBLEM 2.44



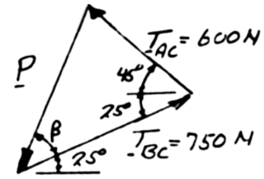
For the cables of Problem 2.36, it is known that the maximum allowable tension is 600 N in cable *AC* and 750 N in cable *BC*. Determine (*a*) the maximum force **P** that can be applied at *C*, (*b*) the corresponding value of *α*.

SOLUTION

Free-Body Diagram



Force Triangle

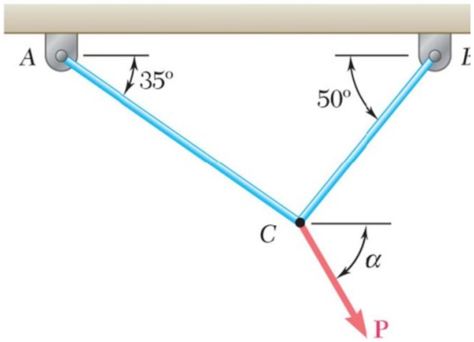


(*a*) Law of cosines $P^2 = (600)^2 + (750)^2 - 2(600)(750)\cos(25° + 45°)$

$P = 784.02 \text{ N}$ $P = 784 \text{ N}$ ◀

(*b*) Law of sines $\dfrac{\sin\beta}{600 \text{ N}} = \dfrac{\sin(25° + 45°)}{784.02 \text{ N}}$

$\beta = 46.0°$ $\therefore \alpha = 46.0° + 25°$ $\alpha = 71.0°$ ◀

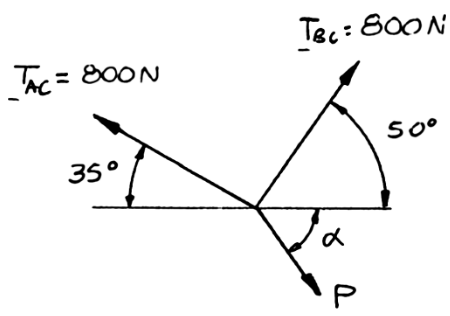


PROBLEM 2.45

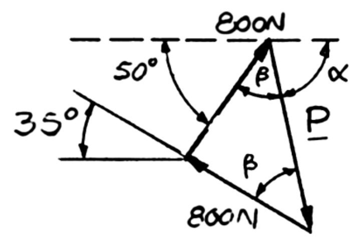
Two cables tied together at C are loaded as shown. Knowing that the maximum allowable tension in each cable is 800 N, determine (*a*) the magnitude of the largest force **P** that can be applied at C, (*b*) the corresponding value of α.

SOLUTION

Free-Body Diagram: *C*



Force Triangle



Force triangle is isosceles with

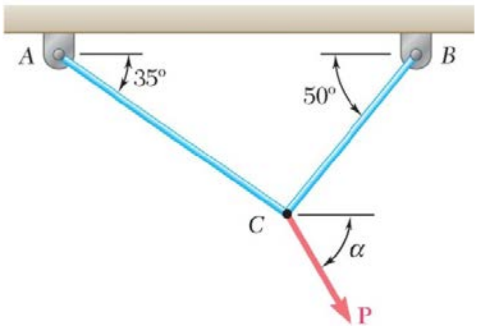
$$2\beta = 180° - 85°$$

$$\beta = 47.5°$$

(*a*) $$P = 2(800\text{ N})\cos 47.5° = 1081\text{ N}$$

Since $P > 0$, the solution is correct. $P = 1081\text{ N}$ ◀

(*b*) $$\alpha = 180° - 50° - 47.5° = 82.5°$$ $\alpha = 82.5°$ ◀

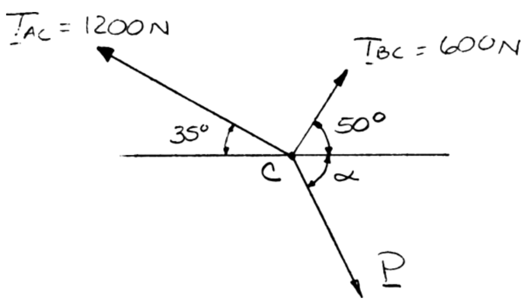


PROBLEM 2.46

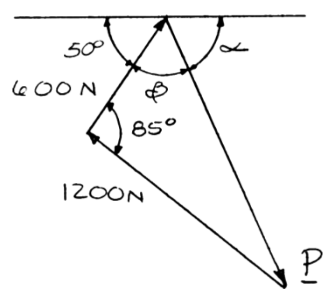
Two cables tied together at *C* are loaded as shown. Knowing that the maximum allowable tension is 1200 N in cable *AC* and 600 N in cable *BC*, determine (*a*) the magnitude of the largest force **P** that can be applied at *C*, (*b*) the corresponding value of α.

SOLUTION

Free-Body Diagram



Force Triangle



(*a*) Law of cosines:

$$P^2 = (1200\text{ N})^2 + (600\text{ N})^2 - 2(1200\text{ N})(600\text{ N})\cos 85°$$

$$P = 1294\text{ N}$$

Since $P.$ 1200 N, the solution is correct.

$P = 1294$ N ◀

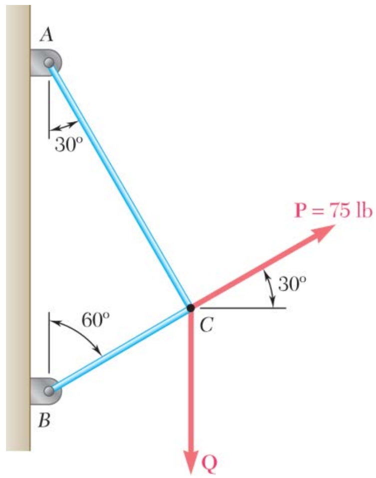
(*b*) Law of sines:

$$\frac{\sin\beta}{1200\text{ N}} = \frac{\sin 85°}{1294\text{ N}}$$

$$\beta = 67.5°$$

$$\alpha = 180° - 50° - 67.5°$$

$\alpha = 62.5°$ ◀

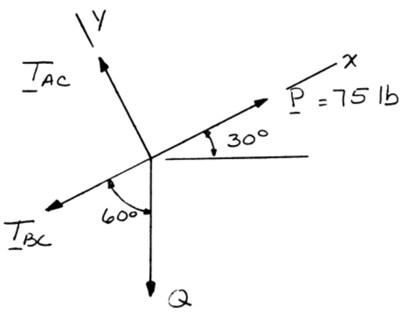


PROBLEM 2.47

Two cables tied together at C are loaded as shown. Determine the range of values of Q for which the tension will not exceed 60 lb in either cable.

SOLUTION

Free-Body Diagram



$\Sigma F_x = 0$: $-T_{BC} - Q\cos 60° + 75 \text{ lb} = 0$

$$T_{BC} = 75 \text{ lb} - Q\cos 60° \qquad (1)$$

$\Sigma F_y = 0$: $T_{AC} - Q\sin 60° = 0$

$$T_{AC} = Q\sin 60° \qquad (2)$$

Requirement: $T_{AC} = 60$ lb:

From Eq. (2): $Q\sin 60° = 60$ lb

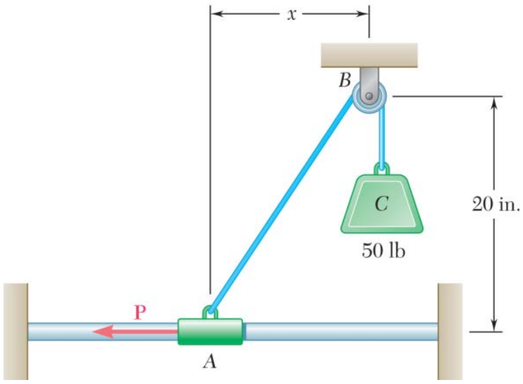
$$Q = 69.3 \text{ lb}$$

Requirement: $T_{BC} = 60$ lb:

From Eq. (1): $75 \text{ lb} - Q\cos 60° = 60$ lb

$$Q = 30.0 \text{ lb} \quad 30.0 \text{ lb} \le Q \le 69.3 \text{ lb} \blacktriangleleft$$

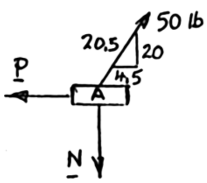
PROBLEM 2.48



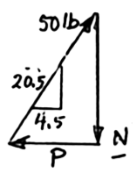
Collar *A* is connected as shown to a 50-lb load and can slide on a frictionless horizontal rod. Determine the magnitude of the force **P** required to maintain the equilibrium of the collar when (*a*) $x = 4.5$ in., (*b*) $x = 15$ in.

SOLUTION

(*a*) **Free Body: Collar *A***



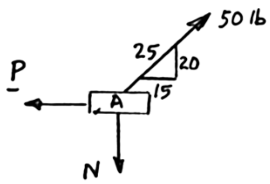
Force Triangle



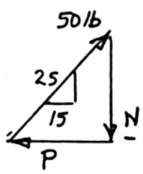
$$\frac{P}{4.5} = \frac{50 \text{ lb}}{20.5}$$

$P = 10.98$ lb ◀

(*b*) **Free Body: Collar *A***

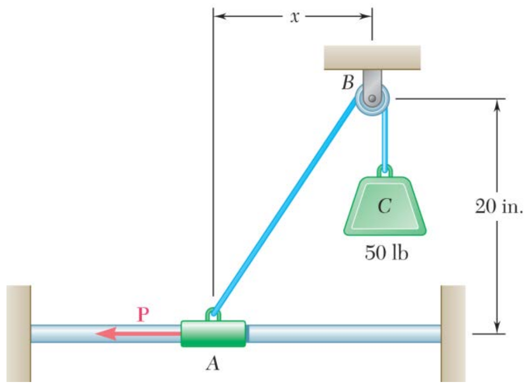


Force Triangle



$$\frac{P}{15} = \frac{50 \text{ lb}}{25}$$

$P = 30.0$ lb ◀

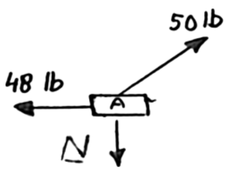


PROBLEM 2.49

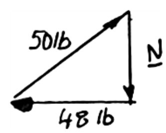
Collar A is connected as shown to a 50-lb load and can slide on a frictionless horizontal rod. Determine the distance x for which the collar is in equilibrium when $P = 48$ lb.

SOLUTION

Free Body: Collar *A*



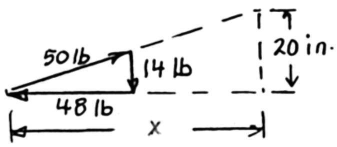
Force Triangle



$$N^2 = (50)^2 - (48)^2 = 196$$

$$N = 14.00 \text{ lb}$$

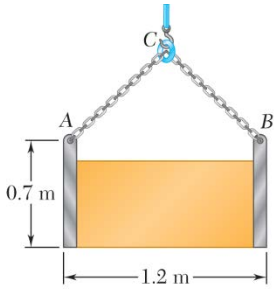
Similar Triangles



$$\frac{x}{20 \text{ in.}} = \frac{48 \text{ lb}}{14 \text{ lb}}$$

$x = 68.6$ in. ◀

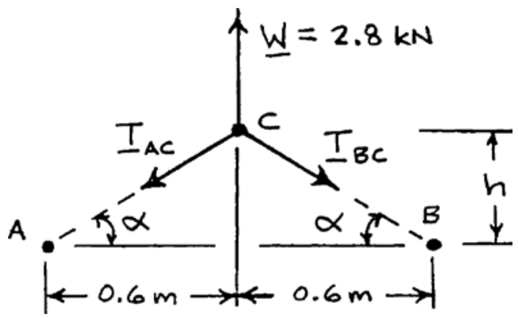
PROBLEM 2.50



A movable bin and its contents have a combined weight of 2.8 kN. Determine the shortest chain sling *ACB* that can be used to lift the loaded bin if the tension in the chain is not to exceed 5 kN.

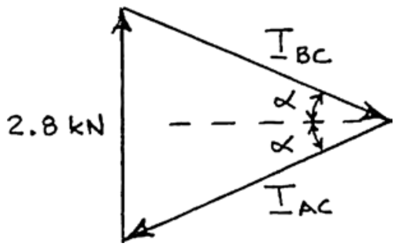
SOLUTION

Free-Body Diagram



$$\tan\alpha = \frac{h}{0.6\text{ m}} \qquad (1)$$

Isosceles Force Triangle



Law of sines: $\sin\alpha = \dfrac{\frac{1}{2}(2.8\text{ kN})}{T_{AC}}$

$$T_{AC} = 5\text{ kN}$$

$$\sin\alpha = \frac{\frac{1}{2}(2.8\text{ kN})}{5\text{ kN}}$$

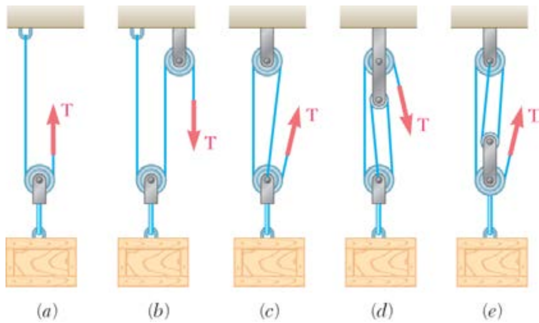
$$\alpha = 16.2602°$$

From Eq. (1): $\tan 16.2602° = \dfrac{h}{0.6\text{ m}}$ $\quad\therefore\quad h = 0.175000\text{ m}$

Half-length of chain $= AC = \sqrt{(0.6\text{ m})^2 + (0.175\text{ m})^2}$

$= 0.625\text{ m}$

Total length: $= 2 \times 0.625\text{ m}$ **1.250 m** ◀



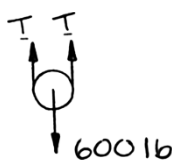
PROBLEM 2.51

A 600-lb crate is supported by several rope-and-pulley arrangements as shown. Determine for each arrangement the tension in the rope. (*Hint:* The tension in the rope is the same on each side of a simple pulley. This can be proved by the methods of Ch. 4.)

SOLUTION

Free-Body Diagram of Pulley

(*a*)

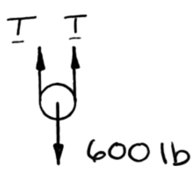


$$+\!\uparrow \Sigma F_y = 0: \quad 2T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{2}(600 \text{ lb})$$

$T = 300$ lb ◀

(*b*)

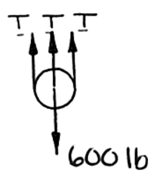


$$+\!\uparrow \Sigma F_y = 0: \quad 2T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{2}(600 \text{ lb})$$

$T = 300$ lb ◀

(*c*)

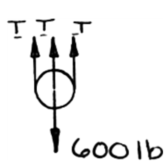


$$+\!\uparrow \Sigma F_y = 0: \quad 3T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{3}(600 \text{ lb})$$

$T = 200$ lb ◀

(*d*)

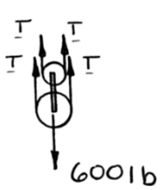


$$+\!\uparrow \Sigma F_y = 0: \quad 3T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{3}(600 \text{ lb})$$

$T = 200$ lb ◀

(*e*)

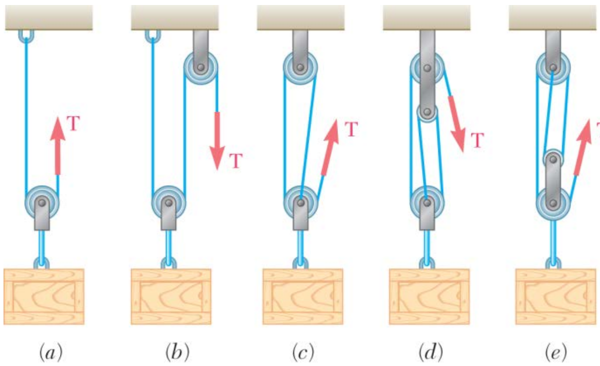


$$+\!\uparrow \Sigma F_y = 0: \quad 4T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{4}(600 \text{ lb})$$

$T = 150.0$ lb ◀

PROBLEM 2.52



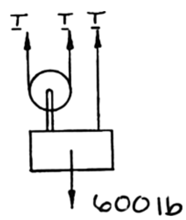
Solve Parts *b* and *d* of Problem 2.51, assuming that the free end of the rope is attached to the crate.

PROBLEM 2.51 A 600-lb crate is supported by several rope-and-pulley arrangements as shown. Determine for each arrangement the tension in the rope. . (*Hint:* The tension in the rope is the same on each side of a simple pulley. This can be proved by the methods of Ch. 4.)

SOLUTION

Free-Body Diagram of Pulley and Crate

(*b*)

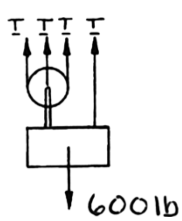


$$+\!\uparrow \Sigma F_y = 0: \quad 3T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{3}(600 \text{ lb})$$

$$T = 200 \text{ lb} \blacktriangleleft$$

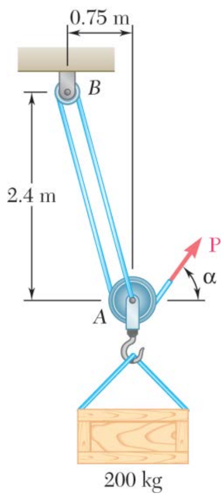
(*d*)



$$+\!\uparrow \Sigma F_y = 0: \quad 4T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{4}(600 \text{ lb})$$

$$T = 150.0 \text{ lb} \blacktriangleleft$$

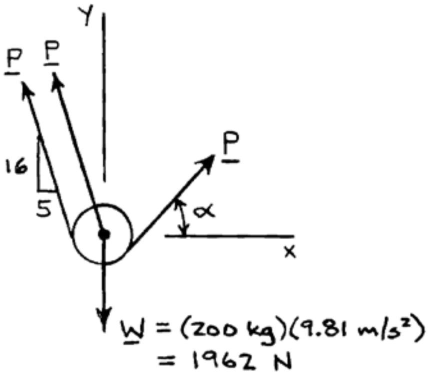


PROBLEM 2.53

A 200-kg crate is to be supported by the rope-and-pulley arrangement shown. Determine the magnitude and direction of the force **P** that must be exerted on the free end of the rope to maintain equilibrium. (See the hint for Prob. 2.51.)

SOLUTION

Free-Body Diagram: Pulley *A*



$$\xrightarrow{+} \Sigma F_x = 0: \quad -2P\left(\frac{5}{\sqrt{281}}\right) + P\cos\alpha = 0$$

$$\cos\alpha = 0.59655$$

$$\alpha = \pm 53.377°$$

For $\alpha = +53.377°$:

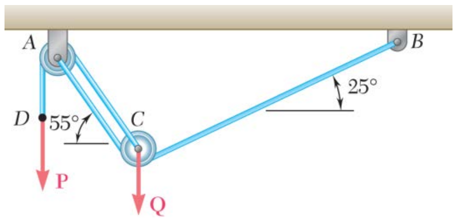
$$+\uparrow \Sigma F_y = 0: \quad 2P\left(\frac{16}{\sqrt{281}}\right) + P\sin 53.377° - 1962\text{ N} = 0$$

$$\mathbf{P} = 724\text{ N} \measuredangle 53.4° \blacktriangleleft$$

For $\alpha = -53.377°$:

$$+\uparrow \Sigma F_y = 0: \quad 2P\left(\frac{16}{\sqrt{281}}\right) + P\sin(-53.377°) - 1962\text{ N} = 0$$

$$\mathbf{P} = 1773 \searrow 53.4° \blacktriangleleft$$

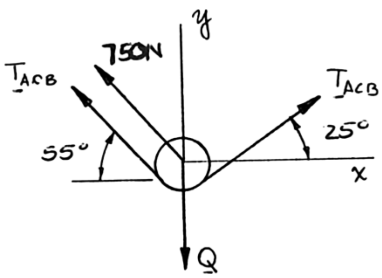


PROBLEM 2.54

A load **Q** is applied to the pulley *C*, which can roll on the cable *ACB*. The pulley is held in the position shown by a second cable *CAD*, which passes over the pulley *A* and supports a load **P**. Knowing that $P = 750$ N, determine (*a*) the tension in cable *ACB*, (*b*) the magnitude of load **Q**.

SOLUTION

Free-Body Diagram: Pulley *C*



(*a*) $\xrightarrow{+} \Sigma F_x = 0$: $T_{ACB}(\cos 25° - \cos 55°) - (750 \text{ N})\cos 55° = 0$

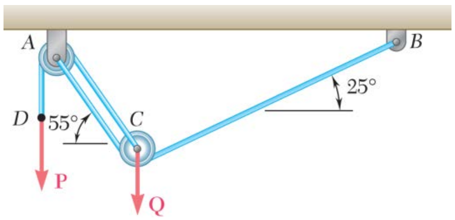
Hence: $T_{ACB} = 1292.88$ N

$T_{ACB} = 1293$ N ◀

(*b*) $+\uparrow \Sigma F_y = 0$: $T_{ACB}(\sin 25° + \sin 55°) + (750 \text{ N})\sin 55° - Q = 0$

$$(1292.88 \text{ N})(\sin 25° + \sin 55°) + (750 \text{ N})\sin 55° - Q = 0$$

or $Q = 2219.8$ N $\qquad Q = 2220$ N ◀

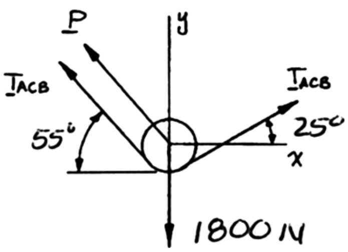


PROBLEM 2.55

An 1800-N load **Q** is applied to the pulley *C*, which can roll on the cable *ACB*. The pulley is held in the position shown by a second cable *CAD*, which passes over the pulley *A* and supports a load **P**. Determine (*a*) the tension in cable *ACB*, (*b*) the magnitude of load **P**.

SOLUTION

Free-Body Diagram: Pulley *C*



$$\xrightarrow{+} \Sigma F_x = 0: \quad T_{ACB}(\cos 25° - \cos 55°) - P\cos 55° = 0$$

or

$$P = 0.58010 T_{ACB} \quad (1)$$

$$+\uparrow \Sigma F_y = 0: \quad T_{ACB}(\sin 25° + \sin 55°) + P\sin 55° - 1800 \text{ N} = 0$$

or

$$1.24177 T_{ACB} + 0.81915 P = 1800 \text{ N} \quad (2)$$

(*a*) Substitute Equation (1) into Equation (2):

$$1.24177 T_{ACB} + 0.81915(0.58010 T_{ACB}) = 1800 \text{ N}$$

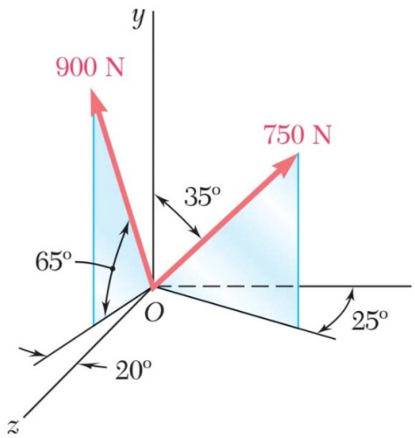
Hence: $T_{ACB} = 1048.37$ N

$$T_{ACB} = 1048 \text{ N} \blacktriangleleft$$

(*b*) Using (1), $P = 0.58010(1048.37 \text{ N}) = 608.16$ N

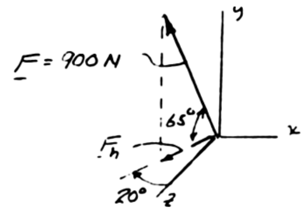
$$P = 608 \text{ N} \blacktriangleleft$$

PROBLEM 2.56



Determine (*a*) the *x*, *y*, and *z* components of the 900-N force, (*b*) the angles θ_x, θ_y, and θ_z that the force forms with the coordinate axes.

SOLUTION



$$F_h = F\cos 65°$$
$$= (900\text{ N})\cos 65°$$
$$F_h = 380.36\text{ N}$$

(*a*)

$$F_x = F_h \sin 20°$$
$$= (380.36\text{ N})\sin 20°$$
$$F_x = -130.091\text{ N}, \qquad F_x = -130.1\text{ N} ◀$$

$$F_y = F\sin 65°$$
$$= (900\text{ N})\sin 65°$$
$$F_y = +815.68\text{ N}, \qquad F_y = +816\text{ N} ◀$$

$$F_z = F_h \cos 20°$$
$$= (380.36\text{ N})\cos 20°$$
$$F_z = +357.42\text{ N} \qquad F_z = +357\text{ N} ◀$$

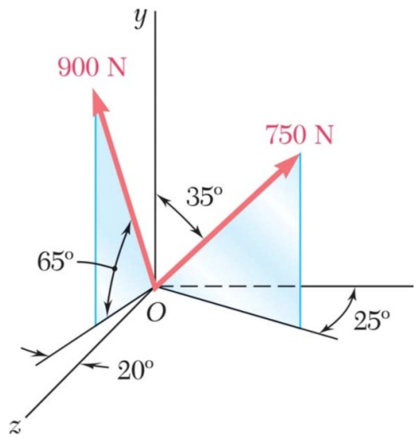
(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{-130.091\text{ N}}{900\text{ N}} \qquad \theta_x = 98.3° ◀$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{+815.68\text{ N}}{900\text{ N}} \qquad \theta_y = 25.0° ◀$$

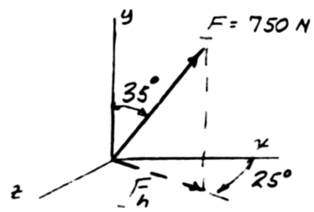
$$\cos\theta_z = \frac{F_z}{F} = \frac{+357.42\text{ N}}{900\text{ N}} \qquad \theta_z = 66.6° ◀$$

PROBLEM 2.57



Determine (*a*) the *x*, *y*, and *z* components of the 750-N force, (*b*) the angles θ_x, θ_y, and θ_z that the force forms with the coordinate axes.

SOLUTION



$$F_h = F \sin 35°$$
$$= (750 \text{ N}) \sin 35°$$
$$F_h = 430.18 \text{ N}$$

(*a*)

$$F_x = F_h \cos 25°$$
$$= (430.18 \text{ N}) \cos 25°$$
$$F_x = +389.88 \text{ N}, \qquad F_x = +390 \text{ N} \blacktriangleleft$$

$$F_y = F \cos 35°$$
$$= (750 \text{ N}) \cos 35°$$
$$F_y = +614.36 \text{ N}, \qquad F_y = +614 \text{ N} \blacktriangleleft$$

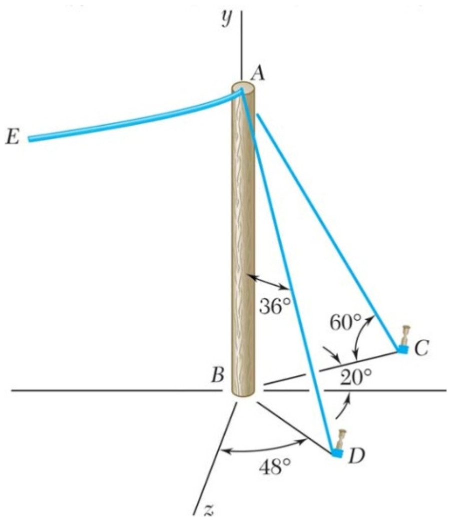
$$F_z = F_h \sin 25°$$
$$= (430.18 \text{ N}) \sin 25° \qquad F_z = +181.8 \text{ N} \blacktriangleleft$$
$$F_z = +181.802 \text{ N}$$

(*b*)

$$\cos \theta_x = \frac{F_x}{F} = \frac{+389.88 \text{ N}}{750 \text{ N}} \qquad \theta_x = 58.7° \blacktriangleleft$$

$$\cos \theta_y = \frac{F_y}{F} = \frac{+614.36 \text{ N}}{750 \text{ N}} \qquad \theta_y = 35.0° \blacktriangleleft$$

$$\cos \theta_z = \frac{F_z}{F} = \frac{+181.802 \text{ N}}{750 \text{ N}} \qquad \theta_z = 76.0° \blacktriangleleft$$



PROBLEM 2.58

The end of the coaxial cable *AE* is attached to the pole *AB*, which is strengthened by the guy wires *AC* and *AD*. Knowing that the tension in wire *AC* is 120 lb, determine (*a*) the components of the force exerted by this wire on the pole, (*b*) the angles θ_x, θ_y, and θ_z that the force forms with the coordinate axes.

SOLUTION

(*a*)

$$F_x = (120\text{ lb})\cos 60° \cos 20°$$

$$F_x = 56.382\text{ lb} \qquad F_x = +56.4\text{ lb} \blacktriangleleft$$

$$F_y = -(120\text{ lb})\sin 60°$$

$$F_y = -103.923\text{ lb} \qquad F_y = -103.9\text{ lb} \blacktriangleleft$$

$$F_z = -(120\text{ lb})\cos 60° \sin 20°$$

$$F_z = -20.521\text{ lb} \qquad F_z = -20.5\text{ lb} \blacktriangleleft$$

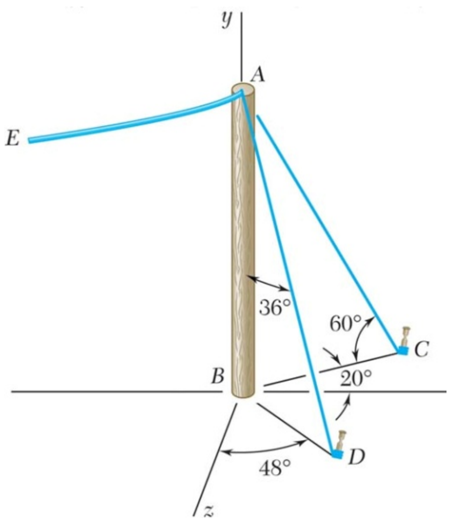
(*b*)

$$\cos \theta_x = \frac{F_x}{F} = \frac{56.382\text{ lb}}{120\text{ lb}} \qquad \theta_x = 62.0° \blacktriangleleft$$

$$\cos \theta_y = \frac{F_y}{F} = \frac{-103.923\text{ lb}}{120\text{ lb}} \qquad \theta_y = 150.0° \blacktriangleleft$$

$$\cos \theta_z = \frac{F_z}{F} = \frac{-20.52\text{ lb}}{120\text{ lb}} \qquad \theta_z = 99.8° \blacktriangleleft$$

PROBLEM 2.59



The end of the coaxial cable *AE* is attached to the pole *AB*, which is strengthened by the guy wires *AC* and *AD*. Knowing that the tension in wire *AD* is 85 lb, determine (*a*) the components of the force exerted by this wire on the pole, (*b*) the angles θ_x, θ_y, and θ_z that the force forms with the coordinate axes.

SOLUTION

(*a*)

$$F_x = (85 \text{ lb}) \sin 36° \sin 48°$$

$$= 37.129 \text{ lb} \qquad F_x = 37.1 \text{ lb} \blacktriangleleft$$

$$F_y = -(85 \text{ lb}) \cos 36°$$

$$= -68.766 \text{ lb} \qquad F_y = -68.8 \text{ lb} \blacktriangleleft$$

$$F_z = (85 \text{ lb}) \sin 36° \cos 48°$$

$$= 33.431 \text{ lb} \qquad F_z = 33.4 \text{ lb} \blacktriangleleft$$

(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{37.129 \text{ lb}}{85 \text{ lb}} \qquad \theta_x = 64.1° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{-68.766 \text{ lb}}{85 \text{ lb}} \qquad \theta_y = 144.0° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{33.431 \text{ lb}}{85 \text{ lb}} \qquad \theta_z = 66.8° \blacktriangleleft$$

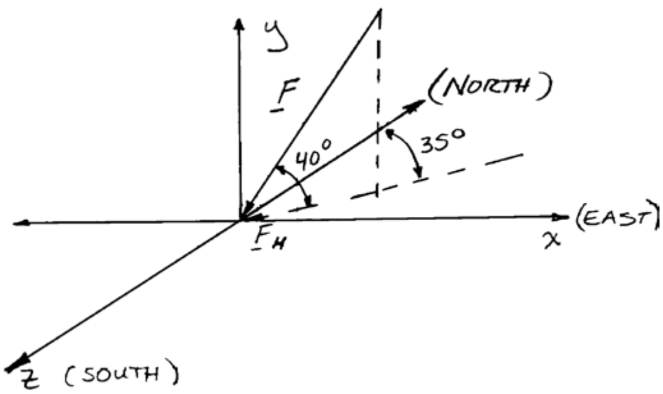
PROBLEM 2.60

A gun is aimed at a point *A* located 35° east of north. Knowing that the barrel of the gun forms an angle of 40° with the horizontal and that the maximum recoil force is 400 N, determine (*a*) the *x*, *y*, and *z* components of that force, (*b*) the values of the angles θ_x, θ_y, and θ_z defining the direction of the recoil force. (Assume that the *x*, *y*, and *z* axes are directed, respectively, east, up, and south.)

SOLUTION

Recoil force $F = 400 \text{ N}$

$$\therefore \quad F_H = (400 \text{ N})\cos 40°$$
$$= 306.42 \text{ N}$$



(*a*)

$$F_x = -F_H \sin 35°$$
$$= -(306.42 \text{ N})\sin 35°$$
$$= -175.755 \text{ N} \qquad F_x = -175.8 \text{ N} \blacktriangleleft$$

$$F_y = -F \sin 40°$$
$$= -(400 \text{ N})\sin 40°$$
$$= -257.12 \text{ N} \qquad F_y = -257 \text{ N} \blacktriangleleft$$

$$F_z = +F_H \cos 35°$$
$$= +(306.42 \text{ N})\cos 35°$$
$$= +251.00 \text{ N} \qquad F_z = +251 \text{ N} \blacktriangleleft$$

(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{-175.755 \text{ N}}{400 \text{ N}} \qquad \theta_x = 116.1° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{-257.12 \text{ N}}{400 \text{ N}} \qquad \theta_y = 130.0° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{251.00 \text{ N}}{400 \text{ N}} \qquad \theta_z = 51.1° \blacktriangleleft$$

PROBLEM 2.61

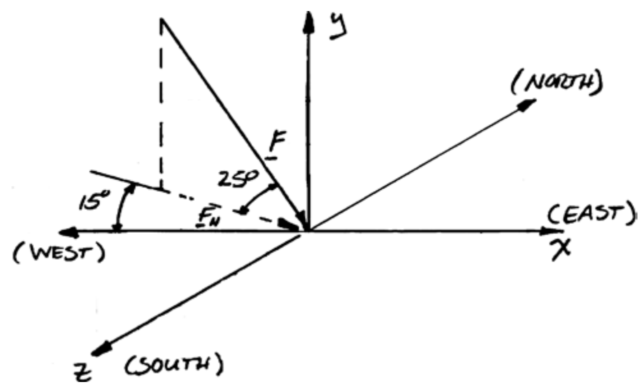
Solve Problem 2.60, assuming that point *A* is located 15° north of west and that the barrel of the gun forms an angle of 25° with the horizontal.

PROBLEM 2.60 A gun is aimed at a point *A* located 35° east of north. Knowing that the barrel of the gun forms an angle of 40° with the horizontal and that the maximum recoil force is 400 N, determine (*a*) the *x*, *y*, and *z* components of that force, (*b*) the values of the angles θ_x, θ_y, and θ_z defining the direction of the recoil force. (Assume that the *x*, *y*, and *z* axes are directed, respectively, east, up, and south.)

SOLUTION

Recoil force $F = 400 \text{ N}$

$$\therefore \quad F_H = (400 \text{ N})\cos 25° = 362.52 \text{ N}$$



(*a*)

$$F_x = +F_H \cos 15° = +(362.52 \text{ N})\cos 15° = +350.17 \text{ N}$$

$F_x = +350 \text{ N}$ ◀

$$F_y = -F\sin 25° = -(400 \text{ N})\sin 25° = -169.047 \text{ N}$$

$F_y = -169.0 \text{ N}$ ◀

$$F_z = +F_H \sin 15° = +(362.52 \text{ N})\sin 15° = +93.827 \text{ N}$$

$F_z = +93.8 \text{ N}$ ◀

(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{+350.17 \text{ N}}{400 \text{ N}}$$

$\theta_x = 28.9°$ ◀

$$\cos\theta_y = \frac{F_y}{F} = \frac{-169.047 \text{ N}}{400 \text{ N}}$$

$\theta_y = 115.0°$ ◀

$$\cos\theta_z = \frac{F_z}{F} = \frac{+93.827 \text{ N}}{400 \text{ N}}$$

$\theta_z = 76.4°$ ◀

PROBLEM 2.62

Determine the magnitude and direction of the force **F** = (690 lb)**i** + (300 lb)**j** – (580 lb)**k**.

SOLUTION

$$\mathbf{F} = (690\text{ lb})\mathbf{i} + (300\text{ lb})\mathbf{j} - (580\text{ lb})\mathbf{k}$$

$$F = \sqrt{F_x^2 + F_y^2 + F_z^2}$$

$$= \sqrt{(690\text{ lb})^2 + (300\text{ lb})^2 + (-580\text{ lb})^2}$$

$$= 950\text{ lb} \qquad F = 950\text{ lb} \blacktriangleleft$$

$$\cos\theta_x = \frac{F_x}{F} = \frac{690\text{ lb}}{950\text{ lb}} \qquad \theta_x = 43.4° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{300\text{ lb}}{950\text{ lb}} \qquad \theta_y = 71.6° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{-580\text{ lb}}{950\text{ lb}} \qquad \theta_z = 127.6° \blacktriangleleft$$

PROBLEM 2.63

Determine the magnitude and direction of the force **F** = (650 N)**i** − (320 N)**j** + (760 N)**k**.

SOLUTION

$$\mathbf{F} = (650\text{ N})\mathbf{i} - (320\text{ N})\mathbf{j} + (760\text{ N})\mathbf{k}$$

$$F = \sqrt{F_x^2 + F_y^2 + F_z^2}$$

$$= \sqrt{(650\text{ N})^2 + (-320\text{ N})^2 + (760\text{ N})^2} \qquad F = 1050\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{F_x}{F} = \frac{650\text{ N}}{1050\text{ N}} \qquad \theta_x = 51.8° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{-320\text{ N}}{1050\text{ N}} \qquad \theta_y = 107.7° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{760\text{ N}}{1050\text{ N}} \qquad \theta_z = 43.6° \blacktriangleleft$$

PROBLEM 2.64

A force acts at the origin of a coordinate system in a direction defined by the angles θ_x = 69.3° and θ_z = 57.9°. Knowing that the *y* component of the force is –174.0 lb, determine (*a*) the angle θ_y, (*b*) the other components and the magnitude of the force.

SOLUTION

$$\cos^2\theta_x + \cos^2\theta_y + \cos^2\theta_z = 1$$

$$\cos^2(69.3°) + \cos^2\theta_y + \cos^2(57.9°) = 1$$

$$\cos\theta_y = \pm 0.7699$$

(*a*) Since $F_y < 0$, we choose $\cos\theta_y = -0.7699$ $\quad\therefore\quad \theta_y = 140.3° \blacktriangleleft$

(*b*)

$$F_y = F\cos\theta_y$$

$$-174.0\text{ lb} = F(-0.7699)$$

$$F = 226.0\text{ lb} \qquad F = 226\text{ lb} \blacktriangleleft$$

$$F_x = F\cos\theta_x = (226.0\text{ lb})\cos 69.3° \qquad F_x = 79.9\text{ lb} \blacktriangleleft$$

$$F_z = F\cos\theta_z = (226.0\text{ lb})\cos 57.9° \qquad F_z = 120.1\text{ lb} \blacktriangleleft$$

PROBLEM 2.65

A force acts at the origin of a coordinate system in a direction defined by the angles θ_x = 70.9° and θ_y = 144.9°. Knowing that the z component of the force is –52.0 lb, determine (a) the angle θ_z, (b) the other components and the magnitude of the force.

SOLUTION

$$\cos^2\theta_x + \cos^2\theta_y + \cos^2\theta_z = 1$$

$$\cos^2 70.9^\circ + \cos^2 144.9^\circ + \cos^2\theta_z^\circ = 1$$

$$\cos\theta_z = \pm 0.47282$$

(a) Since $F_z < 0$, we choose $\cos\theta_z = -0.47282$ $\therefore \quad \theta_z = 118.2^\circ$ ◀

(b)

$$F_z = F\cos\theta_z$$

$$-52.0\ lb = F(-0.47282)$$

$$F = 110.0 \text{ lb}$$ $F = 110.0$ lb ◀

$$F_x = F\cos\theta_x = (110.0 \text{ lb})\cos 70.9^\circ$$ $F_x = 36.0$ lb ◀

$$F_y = F\cos\theta_y = (110.0 \text{ lb})\cos 144.9^\circ$$ $F_y = -90.0$ lb ◀

PROBLEM 2.66

A force acts at the origin of a coordinate system in a direction defined by the angles $\theta_y = 55°$ and $\theta_z = 45°$. Knowing that the x component of the force is – 500 lb, determine (*a*) the angle θ_x, (*b*) the other components and the magnitude of the force.

SOLUTION

(*a*) We have

$$(\cos\theta_x)^2 + (\cos\theta_y)^2 + (\cos\theta_z)^2 = 1 \Rightarrow (\cos\theta_y)^2 = 1 - (\cos\theta_y)^2 - (\cos\theta_z)^2$$

Since $F_x < 0$ we must have $\cos\theta_x$, 0

Thus, taking the negative square root, from above, we have:

$$\cos\theta_x = -\sqrt{1 - (\cos 55)^2 - (\cos 45)^2} = 0.41353 \qquad \theta_x = 114.4° \blacktriangleleft$$

(*b*) Then:

$$F = \frac{F_x}{\cos\theta_x} = \frac{500 \text{ lb}}{0.41353} = 1209.10 \text{ lb} \qquad F = 1209 \text{ lb} \blacktriangleleft$$

and

$$F_y = F\cos\theta_y = (1209.10 \text{ lb})\cos 55° \qquad F_y = 694 \text{ lb} \blacktriangleleft$$

$$F_z = F\cos\theta_z = (1209.10 \text{ lb})\cos 45° \qquad F_z = 855 \text{ lb} \blacktriangleleft$$

PROBLEM 2.67

A force **F** of magnitude 1200 N acts at the origin of a coordinate system. Knowing that $\theta_x = 65°$, $\theta_y = 40°$, and $F_z > 0$, determine (*a*) the components of the force, (*b*) the angle θ_z.

SOLUTION

$$\cos^2\theta_x + \cos^2\theta_y + \cos^2\theta_z = 1$$

$$\cos^2 65^\circ + \cos^2 40° + \cos^2\theta_z° = 1$$

$$\cos\theta_z = \pm 0.48432$$

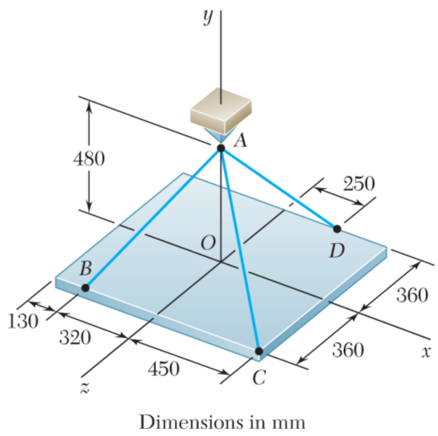
(*b*) Since $F_z > 0$, we choose $\cos\theta_z = 0.48432$, or $\theta_z = 61.032^\circ$ $\quad\therefore\quad \theta_z = 61.0°$ ◀

(*a*) $F = 1200\text{ N}$

$$F_x = F\cos\theta_x = (1200\text{ N})\cos 65^\circ \qquad F_x = 507\text{ N} ◀$$

$$F_y = F\cos\theta_y = (1200\text{ N})\cos 40° \qquad F_y = 919\text{ N} ◀$$

$$F_z = F\cos\theta_z = (1200\text{ N})\cos 61.032° \qquad F_z = 582\text{ N} ◀$$



PROBLEM 2.68

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable *AB* is 408 N, determine the components of the force exerted on the plate at *B*.

SOLUTION

We have:

$$\overrightarrow{BA} = +(320\text{ mm})\mathbf{i} + (480\text{ mm})\mathbf{j} - (360\text{ mm})\mathbf{k} \qquad BA = 680\text{ mm}$$

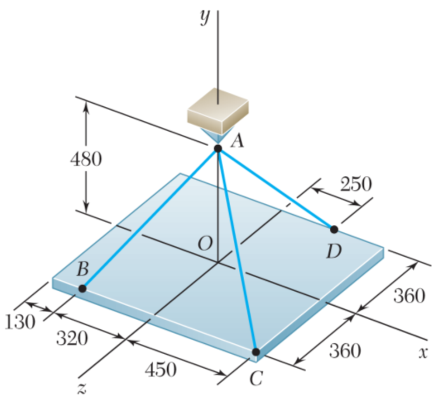
Thus:

$$\mathrm{F}_B = T_{BA}\boldsymbol{\lambda}_{BA} = T_{BA}\frac{\overrightarrow{BA}}{BA} = T_{BA}\left(\frac{8}{17}\mathbf{i} + \frac{12}{17}\mathbf{j} - \frac{9}{17}\mathbf{k}\right)$$

$$\left(\frac{8}{17}T_{BA}\right)\mathbf{i} + \left(\frac{12}{17}T_{BA}\right)\mathbf{j} - \left(\frac{9}{17}T_{BA}\right)\mathbf{k} = 0$$

Setting $T_{BA} = 408\text{ N}$ yields,

$$F_x = +192.0\text{ N}, \quad F_y = +288\text{ N}, \quad F_z = -216\text{ N} \blacktriangleleft$$



Dimensions in mm

PROBLEM 2.69

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable *AD* is 429 N, determine the components of the force exerted on the plate at *D*.

SOLUTION

We have:

$$\overrightarrow{DA} = -(250 \text{ mm})\mathbf{i} + (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \qquad DA = 650 \text{ mm}$$

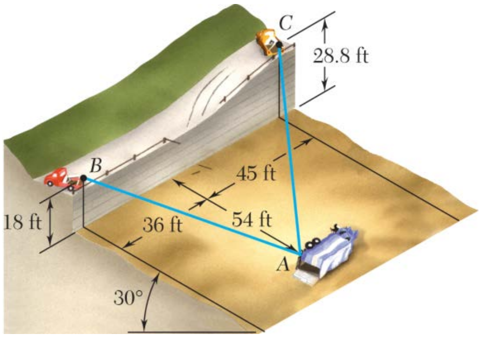
Thus:

$$\mathrm{F}_D = T_{DA}\boldsymbol{\lambda}_{DA} = T_{DA}\frac{\overrightarrow{DA}}{DA} = T_{DA}\left(-\frac{5}{13}\mathbf{i} + \frac{48}{65}\mathbf{j} + \frac{36}{65}\mathbf{k}\right)$$

$$-\left(\frac{5}{13}T_{DA}\right)\mathbf{i} + \left(\frac{48}{65}T_{DA}\right)\mathbf{j} + \left(\frac{36}{65}T_{DA}\right)\mathbf{k} = 0$$

Setting $T_{DA} = 429$ N yields,

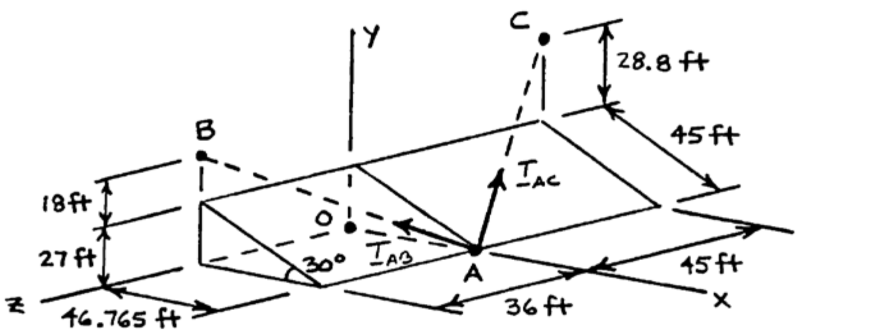
$$F_x = -165.0 \text{ N}, \quad F_y = +317 \text{ N}, \quad F_z = +238 \text{ N} \blacktriangleleft$$



PROBLEM 2.70

In order to move a wrecked truck, two cables are attached at *A* and pulled by winches *B* and *C* as shown. Knowing that the tension in cable *AB* is 2 kips, determine the components of the force exerted at *A* by the cable.

SOLUTION



$\underline{AB} = 74.216$ ft $\qquad \underline{AC} = 85.590$ ft

Cable *AB*:

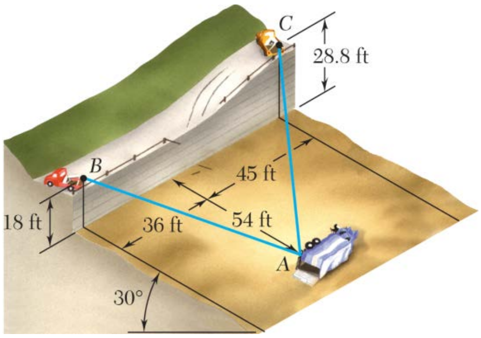
$$\boldsymbol{\lambda}_{AB} = \frac{\overline{AB}}{AB} = \frac{(-46.765\text{ ft})\mathbf{i} + (45\text{ ft})\mathbf{j} + (36\text{ ft})\mathbf{k}}{74.216\text{ ft}}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = \frac{-46.765\mathbf{i} + 45\mathbf{j} + 36\mathbf{k}}{74.216}$$

$(T_{AB})_x = -1.260$ kips ◀

$(T_{AB})_y = +1.213$ kips ◀

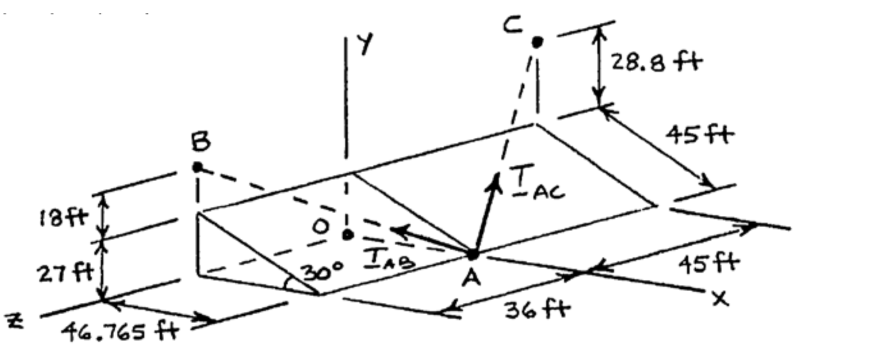
$(T_{AB})_z = +0.970$ kips ◀



PROBLEM 2.71

In order to move a wrecked truck, two cables are attached at A and pulled by winches B and C as shown. Knowing that the tension in cable AC is 1.5 kips, determine the components of the force exerted at A by the cable.

SOLUTION



AB = 74.216 ft   AC = 85.590 ft

Cable AB:

$$\boldsymbol{\lambda}_{AC} = \frac{\overrightarrow{AC}}{AC} = \frac{(-46.765 \text{ ft})\mathbf{i} + (55.8 \text{ ft})\mathbf{j} + (-45 \text{ ft})\mathbf{k}}{85.590 \text{ ft}}$$

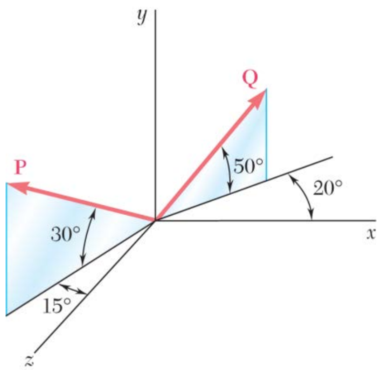
$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = (1.5 \text{ kips})\frac{-46.765\mathbf{i} + 55.8\mathbf{j} - 45\mathbf{k}}{85.590}$$

$(T_{AC})_x = -0.820$ kips ◀

$(T_{AC})_y = +0.978$ kips ◀

$(T_{AC})_z = -0.789$ kips ◀

PROBLEM 2.72



Find the magnitude and direction of the resultant of the two forces shown knowing that $P = 300$ N and $Q = 400$ N.

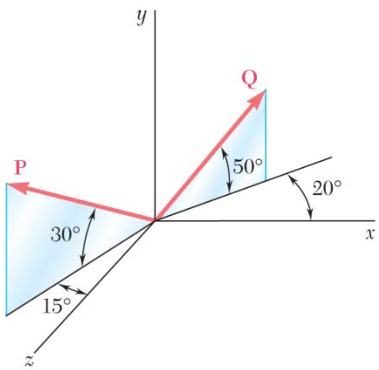
SOLUTION

$$\mathbf{P} = (300\text{ N})[-\cos 30°\sin 15°\mathbf{i} + \sin 30°\mathbf{j} + \cos 30°\cos 15°\mathbf{k}]$$
$$= -(67.243\text{ N})\mathbf{i} + (150\text{ N})\mathbf{j} + (250.95\text{ N})\mathbf{k}$$
$$\mathbf{Q} = (400\text{ N})[\cos 50°\cos 20°\mathbf{i} + \sin 50°\mathbf{j} - \cos 50°\sin 20°\mathbf{k}]$$
$$= (400\text{ N})[0.60402\mathbf{i} + 0.76604\mathbf{j} - 0.21985]$$
$$= (241.61\text{ N})\mathbf{i} + (306.42\text{ N})\mathbf{j} - (87.939\text{ N})\mathbf{k}$$
$$\mathbf{R} = \mathbf{P} + \mathbf{Q}$$
$$= (174.367\text{ N})\mathbf{i} + (456.42\text{ N})\mathbf{j} + (163.011\text{ N})\mathbf{k}$$
$$R = \sqrt{(174.367\text{ N})^2 + (456.42\text{ N})^2 + (163.011\text{ N})^2}$$
$$= 515.07\text{ N} \qquad R = 515\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{R_x}{R} = \frac{174.367\text{ N}}{515.07\text{ N}} = 0.33853 \qquad \theta_x = 70.2° \blacktriangleleft$$

$$\cos\theta_y = \frac{R_y}{R} = \frac{456.42\text{ N}}{515.07\text{ N}} = 0.88613 \qquad \theta_y = 27.6° \blacktriangleleft$$

$$\cos\theta_z = \frac{R_z}{R} = \frac{163.011\text{ N}}{515.07\text{ N}} = 0.31648 \qquad \theta_z = 71.5° \blacktriangleleft$$



PROBLEM 2.73

Find the magnitude and direction of the resultant of the two forces shown knowing that $P = 400$ N and $Q = 300$ N.

SOLUTION

$$\mathbf{P} = (400 \text{ N})[-\cos 30° \sin 15° \mathbf{i} + \sin 30° \mathbf{j} + \cos 30° \cos 15° \mathbf{k}]$$

$$= -(89.678 \text{ N})\mathbf{i} + (200 \text{ N})\mathbf{j} + (334.61 \text{ N})\mathbf{k}$$

$$\mathbf{Q} = (300 \text{ N})[\cos 50° \cos 20° \mathbf{i} + \sin 50° \mathbf{j} - \cos 50° \sin 20° \mathbf{k}]$$

$$= (181.21 \text{ N})\mathbf{i} + (229.81 \text{ N})\mathbf{j} - (65.954 \text{ N})\mathbf{k}$$

$$\mathbf{R} = \mathbf{P} + \mathbf{Q}$$

$$= (91.532 \text{ N})\mathbf{i} + (429.81 \text{ N})\mathbf{j} + (268.66 \text{ N})\mathbf{k}$$

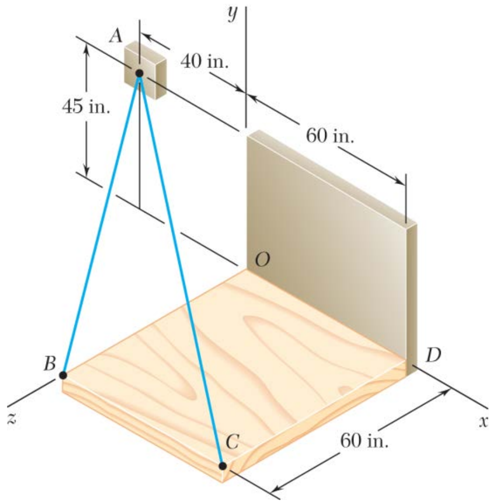
$$R = \sqrt{(91.532 \text{ N})^2 + (429.81 \text{ N})^2 + (268.66 \text{ N})^2}$$

$$= 515.07 \text{ N} \qquad R = 515 \text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{R_x}{R} = \frac{91.532 \text{ N}}{515.07 \text{ N}} = 0.177708 \qquad \theta_x = 79.8° \blacktriangleleft$$

$$\cos\theta_y = \frac{R_y}{R} = \frac{429.81 \text{ N}}{515.07 \text{ N}} = 0.83447 \qquad \theta_y = 33.4° \blacktriangleleft$$

$$\cos\theta_z = \frac{R_z}{R} = \frac{268.66 \text{ N}}{515.07 \text{ N}} = 0.52160 \qquad \theta_z = 58.6° \blacktriangleleft$$



PROBLEM 2.74

Knowing that the tension is 425 lb in cable AB and 510 lb in cable AC, determine the magnitude and direction of the resultant of the forces exerted at A by the two cables.

SOLUTION

$$\overrightarrow{AB} = (40\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}$$

$$AB = \sqrt{(40\text{ in.})^2 + (45\text{ in.})^2 + (60\text{ in.})^2} = 85\text{ in.}$$

$$\overrightarrow{AC} = (100\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}$$

$$AC = \sqrt{(100\text{ in.})^2 + (45\text{ in.})^2 + (60\text{ in.})^2} = 125\text{ in.}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (425\text{ lb})\left[\frac{(40\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}}{85\text{ in.}}\right]$$

$$\mathbf{T}_{AB} = (200\text{ lb})\mathbf{i} - (225\text{ lb})\mathbf{j} + (300\text{ lb})\mathbf{k}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (510\text{ lb})\left[\frac{(100\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}}{125\text{ in.}}\right]$$

$$\mathbf{T}_{AC} = (408\text{ lb})\mathbf{i} - (183.6\text{ lb})\mathbf{j} + (244.8\text{ lb})\mathbf{k}$$

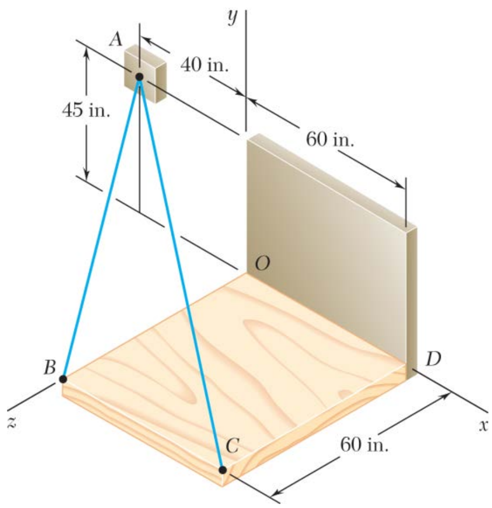
$$\mathbf{R} = \mathbf{T}_{AB} + \mathbf{T}_{AC} = (608)\mathbf{i} - (408.6\text{ lb})\mathbf{j} + (544.8\text{ lb})\mathbf{k}$$

Then: $R = 912.92\text{ lb}$ $\qquad R = 913\text{ lb}$ ◀

and $\cos\theta_x = \dfrac{608\text{ lb}}{912.92\text{ lb}} = 0.66599$ $\qquad \theta_x = 48.2°$ ◀

$\cos\theta_y = \dfrac{408.6\text{ lb}}{912.92\text{ lb}} = -0.44757$ $\qquad \theta_y = 116.6°$ ◀

$\cos\theta_z = \dfrac{544.8\text{ lb}}{912.92\text{ lb}} = 0.59677$ $\qquad \theta_z = 53.4°$ ◀



PROBLEM 2.75

Knowing that the tension is 510 lb in cable AB and 425 lb in cable AC, determine the magnitude and direction of the resultant of the forces exerted at A by the two cables.

SOLUTION

$$\overrightarrow{AB} = (40\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}$$

$$AB = \sqrt{(40\text{ in.})^2 + (45\text{ in.})^2 + (60\text{ in.})^2} = 85\text{ in.}$$

$$\overrightarrow{AC} = (100\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}$$

$$AC = \sqrt{(100\text{ in.})^2 + (45\text{ in.})^2 + (60\text{ in.})^2} = 125\text{ in.}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (510\text{ lb})\left[\frac{(40\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}}{85\text{ in.}}\right]$$

$$\mathbf{T}_{AB} = (240\text{ lb})\mathbf{i} - (270\text{ lb})\mathbf{j} + (360\text{ lb})\mathbf{k}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (425\text{ lb})\left[\frac{(100\text{ in.})\mathbf{i} - (45\text{ in.})\mathbf{j} + (60\text{ in.})\mathbf{k}}{125\text{ in.}}\right]$$

$$\mathbf{T}_{AC} = (340\text{ lb})\mathbf{i} - (153\text{ lb})\mathbf{j} + (204\text{ lb})\mathbf{k}$$

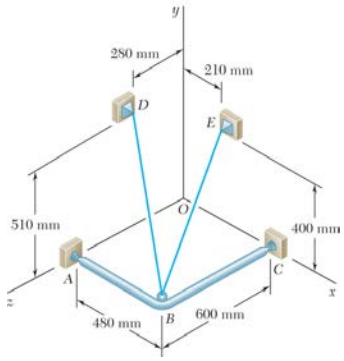
$$\mathbf{R} = \mathbf{T}_{AB} + \mathbf{T}_{AC} = (580\text{ lb})\mathbf{i} - (423\text{ lb})\mathbf{j} + (564\text{ lb})\mathbf{k}$$

Then: $R = 912.92\text{ lb}$ $\qquad R = 913\text{ lb}$ ◀

and $\cos\theta_x = \dfrac{580\text{ lb}}{912.92\text{ lb}} = 0.63532$ $\qquad \theta_x = 50.6°$ ◀

$\cos\theta_y = \dfrac{-423\text{ lb}}{912.92\text{ lb}} = -0.46335$ $\qquad \theta_y = 117.6°$ ◀

$\cos\theta_z = \dfrac{564\text{ lb}}{912.92\text{ lb}} = 0.61780$ $\qquad \theta_z = 51.8°$ ◀



PROBLEM 2.76

A frame *ABC* is supported in part by cable *DBE* that passes through a frictionless ring at *B*. Knowing that the tension in the cable is 385 N, determine the components of the force exerted by the cable on the support at *D*.

SOLUTION

$$\overrightarrow{BD} = -(480\text{ mm})\mathbf{i} + (510\text{ mm})\mathbf{j} - (320\text{ mm})\mathbf{k}$$

$$BD = \sqrt{(480\text{ mm})^2 + (510\text{ mm})^2 + (320\text{ mm})^2} = 770\text{ mm}$$

$$\mathbf{F}_{BD} = T_{BD}\boldsymbol{\lambda}_{BD} = T_{BD}\frac{\overrightarrow{BD}}{BD}$$

$$= \frac{(385\text{ N})}{(770\text{ mm})}[-(480\text{ mm})\mathbf{i} + (510\text{ mm})\mathbf{j} - (320\text{ mm})\mathbf{k}]$$

$$= -(240\text{ N})\mathbf{i} + (255\text{ N})\mathbf{j} - (160\text{ N})\mathbf{k}$$

$$\overrightarrow{BE} = -(270\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} - (600\text{ mm})\mathbf{k}$$

$$BE = \sqrt{(270\text{ mm})^2 + (400\text{ mm})^2 + (600\text{ mm})^2} = 770\text{ mm}$$

$$\mathbf{F}_{BE} = T_{BE}\boldsymbol{\lambda}_{BE} = T_{BE}\frac{\overrightarrow{BE}}{BE}$$

$$= \frac{(385\text{ N})}{(770\text{ mm})}[-(270\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} - (600\text{ mm})\mathbf{k}]$$

$$= -(135\text{ N})\mathbf{i} + (200\text{ N})\mathbf{j} - (300\text{ N})\mathbf{k}$$

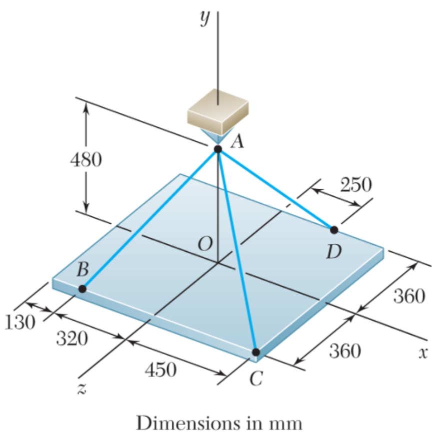
$$\mathbf{R} = \mathbf{F}_{BD} + \mathbf{F}_{BE} = -(375\text{ N})\mathbf{i} + (455\text{ N})\mathbf{j} - (460\text{ N})\mathbf{k}$$

$$R = \sqrt{(375\text{ N})^2 + (455\text{ N})^2 + (460\text{ N})^2} = 747.83\text{ N} \qquad R = 748\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{-375\text{ N}}{747.83\text{ N}} \qquad \theta_x = 120.1° \blacktriangleleft$$

$$\cos\theta_y = \frac{455\text{ N}}{747.83\text{ N}} \qquad \theta_y = 52.5° \blacktriangleleft$$

$$\cos\theta_z = \frac{-460\text{ N}}{747.83\text{ N}} \qquad \theta_z = 128.0° \blacktriangleleft$$



PROBLEM 2.77

For the plate of Prob. 2.68, determine the tensions in cables *AB* and *AD* knowing that the tension in cable *AC* is 54 N and that the resultant of the forces exerted by the three cables at *A* must be vertical.

SOLUTION

We have:

$$\overrightarrow{AB} = -(320 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \qquad AB = 680 \text{ mm}$$

$$\overrightarrow{AC} = (450 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \qquad AC = 750 \text{ mm}$$

$$\overrightarrow{AD} = (250 \text{ mm})\mathbf{i} - (480 \text{ mm})\mathbf{j} - (360 \text{ mm})\mathbf{k} \qquad AD = 650 \text{ mm}$$

Thus:

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = \frac{T_{AB}}{680}(-320\mathbf{i} - 480\mathbf{j} + 360\mathbf{k})$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = \frac{54}{750}(450\mathbf{i} - 480\mathbf{j} + 360\mathbf{k})$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = \frac{T_{AD}}{650}(250\mathbf{i} - 480\mathbf{j} - 360\mathbf{k})$$

Substituting into the Eq. $\mathbf{R} = \Sigma\mathbf{F}$ and factoring $\mathbf{i}, \mathbf{j}, \mathbf{k}$:

$$\mathbf{R} = \left(-\frac{320}{680}T_{AB} + 32.40 + \frac{250}{650}T_{AD}\right)\mathbf{i}$$

$$+\left(-\frac{480}{680}T_{AB} - 34.560 - \frac{480}{650}T_{AD}\right)\mathbf{j}$$

$$+\left(\frac{360}{680}T_{AB} + 25.920 - \frac{360}{650}T_{AD}\right)\mathbf{k}$$

SOLUTION (Continued)

Since **R** is vertical, the coefficients of **i** and **k** are zero:

$$\mathbf{i}: \qquad -\frac{320}{680}T_{AB} + 32.40 + \frac{250}{650}T_{AD} = 0 \qquad (1)$$

$$\mathbf{k}: \qquad \frac{360}{680}T_{AB} + 25.920 - \frac{360}{650}T_{AD} = 0 \qquad (2)$$

Multiply (1) by 3.6 and (2) by 2.5 then add:

$$-\frac{252}{680}T_{AB} + 181.440 = 0$$

$$T_{AB} = 489.60 \text{ N}$$

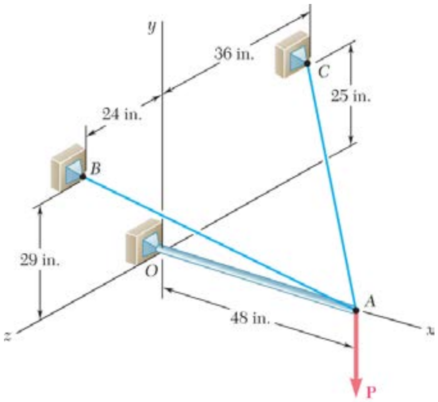
$$T_{AB} = 490 \text{ N} \blacktriangleleft$$

Substitute into (2) and solve for T_{AD}:

$$\frac{360}{680}(489.60 \text{ N}) + 25.920 - \frac{360}{650}T_{AD} = 0$$

$$T_{AD} = 514.80 \text{ N}$$

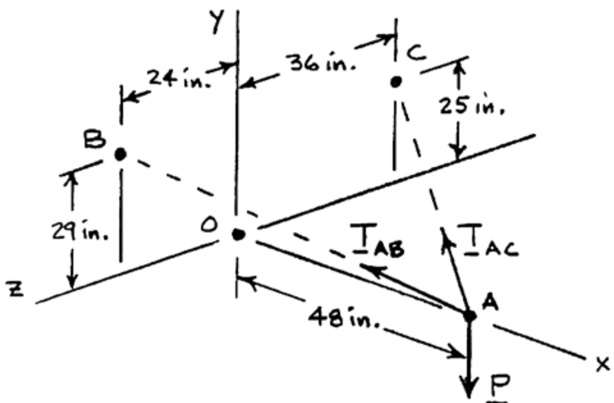
$$T_{AD} = 515 \text{ N} \blacktriangleleft$$



PROBLEM 2.78

The boom *OA* carries a load **P** and is supported by two cables as shown. Knowing that the tension in cable *AB* is 183 lb and that the resultant of the load **P** and of the forces exerted at *A* by the two cables must be directed along *OA*, determine the tension in cable *AC*.

SOLUTION



Cable *AB*: $T_{AB} = 183\text{ lb}$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (183\text{ lb})\frac{(-48\text{ in.})\mathbf{i} + (29\text{ in.})\mathbf{j} + (24\text{ in.})\mathbf{k}}{61\text{ in.}}$$

$$\mathbf{T}_{AB} = -(144\text{ lb})\mathbf{i} + (87\text{ lb})\mathbf{j} + (72\text{ lb})\mathbf{k}$$

Cable *AC*: $$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\frac{(-48\text{ in.})\mathbf{i} + (25\text{ in.})\mathbf{j} + (-36\text{ in.})\mathbf{k}}{65\text{ in.}}$$

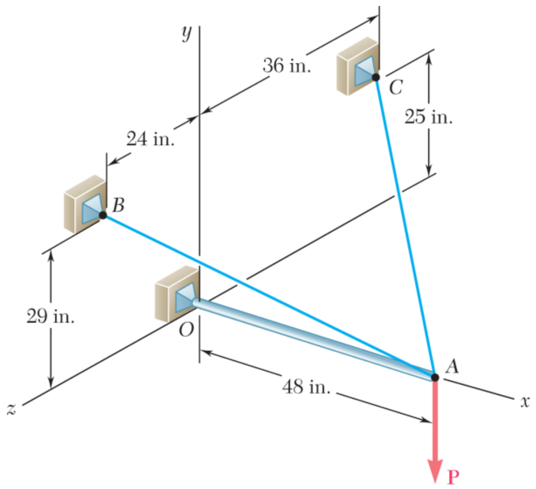
$$\mathbf{T}_{AC} = -\frac{48}{65}T_{AC}\mathbf{i} + \frac{25}{65}T_{AC}\mathbf{j} - \frac{36}{65}T_{AC}\mathbf{k}$$

Load *P*: $\mathbf{P} = P\,\mathbf{j}$

For resultant to be directed along *OA*, i.e., *x*-axis

$$R_z = 0: \quad \Sigma F_z = (72\text{ lb}) - \frac{36}{65}T'_{AC} = 0$$

$T_{AC} = 130.0\text{ lb}$ ◀



PROBLEM 2.79

For the boom and loading of Problem. 2.78, determine the magnitude of the load **P**.

PROBLEM 2.78 The boom *OA* carries a load **P** and is supported by two cables as shown. Knowing that the tension in cable *AB* is 183 lb and that the resultant of the load **P** and of the forces exerted at *A* by the two cables must be directed along *OA*, determine the tension in cable *AC*.

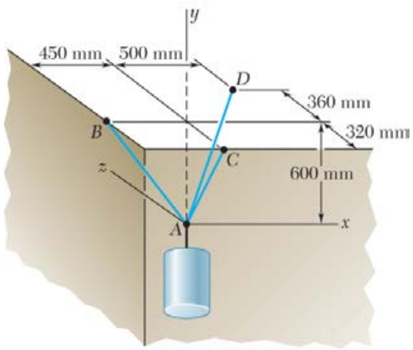
SOLUTION

See Problem 2.78. Since resultant must be directed along *OA*, i.e., the *x*-axis, we write

$$R_y = 0: \quad \Sigma F_y = (87\text{ lb}) + \frac{25}{65}T_{AC} - P = 0$$

$T_{AC} = 130.0\text{ lb}$ from Problem 2.97.

Then $$(87\text{ lb}) + \frac{25}{65}(130.0\text{ lb}) - P = 0$$ $P = 137.0\text{ lb}$ ◀

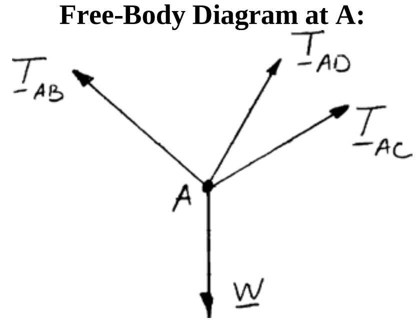


PROBLEM 2.80

A container is supported by three cables that are attached to a ceiling as shown. Determine the weight W of the container, knowing that the tension in cable AB is 6 kN.

SOLUTION

Free-Body Diagram at A:



The forces applied at A are: $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD},$ and $\mathbf{W}$

where $\mathbf{W} = W\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{AB} = -(450\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} \qquad AB = 750\text{ mm}$$

$$\overrightarrow{AC} = +(600\text{ mm})\mathbf{j} - (320\text{ mm})\mathbf{k} \qquad AC = 680\text{ mm}$$

$$\overrightarrow{AD} = +(500\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AD = 860\text{ mm}$$

and

$$\mathbf{T}_{AB} = \boldsymbol{\lambda}_{AB}T_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = T_{AB}\frac{(-450\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j}}{750\text{ mm}}$$

$$= \left(-\frac{45}{75}\mathbf{i} + \frac{60}{75}\mathbf{j}\right)T_{AB}$$

$$\mathbf{T}_{AC} = \boldsymbol{\lambda}_{AC}T_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\frac{(600\text{ mm})\mathbf{i} - (320\text{ mm})\mathbf{j}}{680\text{ mm}}$$

$$= \left(\frac{60}{68}\mathbf{j} - \frac{32}{68}\mathbf{k}\right)T_{AC}$$

$$\mathbf{T}_{AD} = \boldsymbol{\lambda}_{AD}T_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = T_{AD}\frac{(500\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k}}{860\text{ mm}}$$

$$= \left(\frac{50}{86}\mathbf{i} + \frac{60}{86}\mathbf{j} + \frac{36}{86}\mathbf{k}\right)T_{AD}$$

SOLUTION (Continued)

Equilibrium condition: $\Sigma F = 0$: $\therefore$ $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{W} = 0$

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$; factoring **i**, **j**, and **k**; and equating each of the coefficients to zero gives the following equations:

From **i**:
$$-\frac{45}{75}T_{AB} + \frac{50}{86}T_{AD} = 0 \tag{1}$$

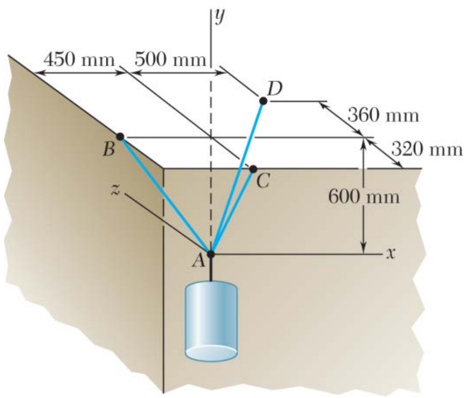
From **j**:
$$\frac{60}{75}T_{AB} + \frac{60}{68}T_{AC} + \frac{60}{86}T_{AD} - W = 0 \tag{2}$$

From **k**:
$$-\frac{32}{68}T_{AC} + \frac{36}{86}T_{AD} = 0 \tag{3}$$

Setting $T_{AB} = 6$ kN in (1) and (2), and solving the resulting set of equations gives

$$T_{AC} = 6.1920 \text{ kN}$$
$$T_{AC} = 5.5080 \text{ kN}$$

$W = 13.98$ kN ◀

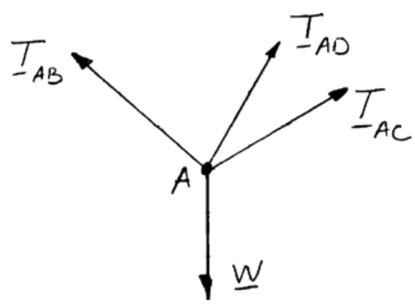


PROBLEM 2.81

A container is supported by three cables that are attached to a ceiling as shown. Determine the weight W of the container, knowing that the tension in cable AD is 4.3 kN.

SOLUTION

Free-Body Diagram at A:



The forces applied at A are: $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD},$ and $\mathbf{W}$

where $\mathbf{W} = W\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{AB} = -(450\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} \qquad AB = 750\text{ mm}$$

$$\overrightarrow{AC} = +(600\text{ mm})\mathbf{j} - (320\text{ mm})\mathbf{k} \qquad AC = 680\text{ mm}$$

$$\overrightarrow{AD} = +(500\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AD = 860\text{ mm}$$

and

$$\mathbf{T}_{AB} = \boldsymbol{\lambda}_{AB}T_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = T_{AB}\frac{(-450\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j}}{750\text{ mm}}$$

$$= \left(-\frac{45}{75}\mathbf{i} + \frac{60}{75}\mathbf{j}\right)T_{AB}$$

$$\mathbf{T}_{AC} = \boldsymbol{\lambda}_{AC}T_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\frac{(600\text{ mm})\mathbf{i} - (320\text{ mm})\mathbf{j}}{680\text{ mm}}$$

$$= \left(\frac{60}{68}\mathbf{j} - \frac{32}{68}\mathbf{k}\right)T_{AC}$$

$$\mathbf{T}_{AD} = \boldsymbol{\lambda}_{AD}T_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = T_{AD}\frac{(500\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k}}{860\text{ mm}}$$

$$= \left(\frac{50}{86}\mathbf{i} + \frac{60}{86}\mathbf{j} + \frac{36}{86}\mathbf{k}\right)T_{AD}$$

PROBLEM 2.81 (Continued)

Equilibrium condition: $\Sigma F = 0$: $\therefore$ $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{W} = 0$

Substituting the expressions obtained for $\mathbf{T}_{AB}, \mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$; factoring **i**, **j**, and **k**; and equating each of the coefficients to zero gives the following equations:

From **i**: $$-\frac{45}{75}T_{AB} + \frac{50}{86}T_{AD} = 0$$

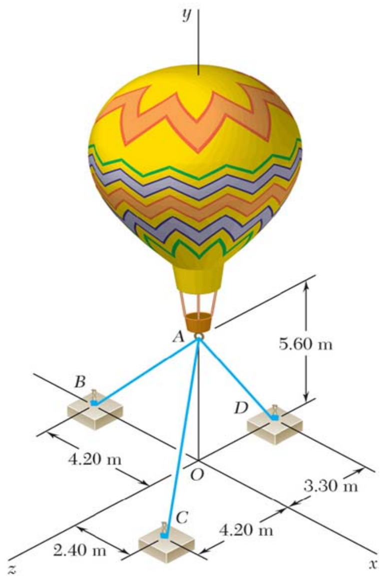
From **j**: $$\frac{60}{75}T_{AB} + \frac{60}{68}T_{AC} + \frac{60}{86}T_{AD} - W = 0$$

From **k**: $$-\frac{32}{68}T_{AC} + \frac{36}{86}T_{AD} = 0$$

Setting $T_{AD} = 4.3\text{ kN}$ into the above equations gives

$T_{AB} = 4.1667\text{ kN}$

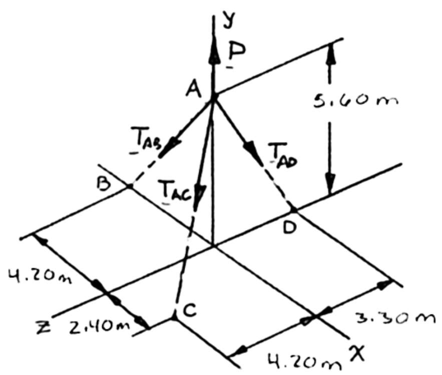
$T_{AC} = 3.8250\text{ kN}$ $\qquad W = 9.71\text{ kN}$ ◀



PROBLEM 2.82

Three cables are used to tether a balloon as shown. Knowing that the balloon exerts an 800-N vertical force at *A*, determine the tension in each cable.

SOLUTION



The forces applied at *A* are: $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD}$, and $\mathbf{P}$

where $\mathbf{P} = P\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{AB} = -(4.20\text{ m})\mathbf{i} - (5.60\text{ m})\mathbf{j} \qquad AB = 7.00\text{ m}$$

$$\overrightarrow{AC} = (2.40\text{ m})\mathbf{i} - (5.60\text{ m})\mathbf{j} + (4.20\text{ m})\mathbf{k} \qquad AC = 7.40\text{ m}$$

$$\overrightarrow{AD} = -(5.60\text{ m})\mathbf{j} - (3.30\text{ m})\mathbf{k} \qquad AD = 6.50\text{ m}$$

and

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (-0.6\mathbf{i} - 0.8\mathbf{j})T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (0.32432 - 0.75676\mathbf{j} + 0.56757\mathbf{k})T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = (-0.86154\mathbf{j} - 0.50769\mathbf{k})T_{AD}$$

PROBLEM 2.82 (Continued)

Equilibrium condition $\Sigma F = 0$: $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$ and factoring **i**, **j**, and **k**:

$$(-0.6T_{AB} + 0.32432T_{AC})\mathbf{i} + (-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P)\mathbf{j}$$
$$+(0.56757T_{AC} - 0.50769T_{AD})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$-0.6T_{AB} + 0.32432T_{AC} = 0 \tag{1}$$

$$-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0 \tag{2}$$

$$0.56757T_{AC} - 0.50769T_{AD} = 0 \tag{3}$$

From Eq. (1) $T_{AB} = 0.54053T_{AC}$

From Eq. (3) $T_{AD} = 1.11795T_{AC}$

Substituting for T_{AB} and T_{AD} in terms of T_{AC} into Eq. (2) gives:

$$-0.8(0.54053T_{AC}) - 0.75676T_{AC} - 0.86154(1.11795T_{AC}) + P = 0$$

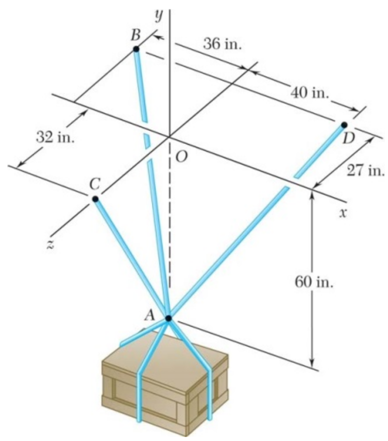
$$2.1523T_{AC} = P; \quad P = 800 \text{ N}$$

$$T_{AC} = \frac{800 \text{ N}}{2.1523}$$
$$= 371.69 \text{ N}$$

Substituting into expressions for T_{AB} and T_{AD} gives:

$$T_{AB} = 0.54053(371.69 \text{ N})$$
$$T_{AD} = 1.11795(371.69 \text{ N})$$

$$T_{AB} = 201 \text{ N}, \quad T_{AC} = 372 \text{ N}, \quad T_{AD} = 416 \text{ N} \blacktriangleleft$$



PROBLEM 2.83

A crate is supported by three cables as shown. Determine the weight of the crate knowing that the tension in cable AD is 616 lb.

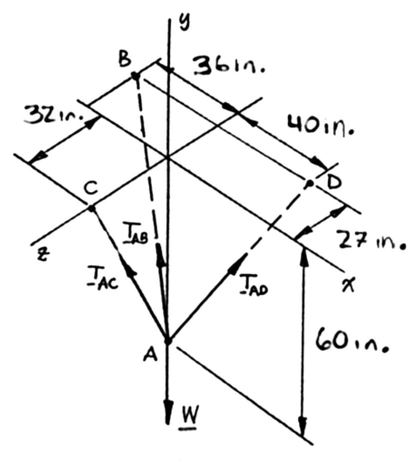
SOLUTION

The forces applied at A are:

$$\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD} \text{ and } \mathbf{W}$$

where $\mathbf{P} = P\mathbf{j}$. To express the other forces in terms of the unit vectors $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$, we write

$$\overrightarrow{AB} = -(36\text{ in.})\mathbf{i} + (60\text{ in.})\mathbf{j} - (27\text{ in.})\mathbf{k}$$
$$AB = 75\text{ in.}$$
$$\overrightarrow{AC} = (60\text{ in.})\mathbf{j} + (32\text{ in.})\mathbf{k}$$
$$AC = 68\text{ in.}$$
$$\overrightarrow{AD} = (40\text{ in.})\mathbf{i} + (60\text{ in.})\mathbf{j} - (27\text{ in.})\mathbf{k}$$
$$AD = 77\text{ in.}$$



and

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$
$$= (-0.48\mathbf{i} + 0.8\mathbf{j} - 0.36\mathbf{k})T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC}$$
$$= (0.88235\mathbf{j} + 0.47059\mathbf{k})T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD}$$
$$= (0.51948\mathbf{i} + 0.77922\mathbf{j} - 0.35065\mathbf{k})T_{AD}$$

Equilibrium Condition with $\mathbf{W} = -W\mathbf{j}$

$$\Sigma F = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} - W\mathbf{j} = 0$$

PROBLEM 2.83 (Continued)

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$ and factoring **i**, **j**, and **k**:

$$(-0.48T_{AB} + 0.51948T_{AD})\mathbf{i} + (0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W)\mathbf{j}$$
$$+(-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD})\mathbf{k} = 0$$

$$-0.48T_{AB} + 0.51948T_{AD} = 0$$

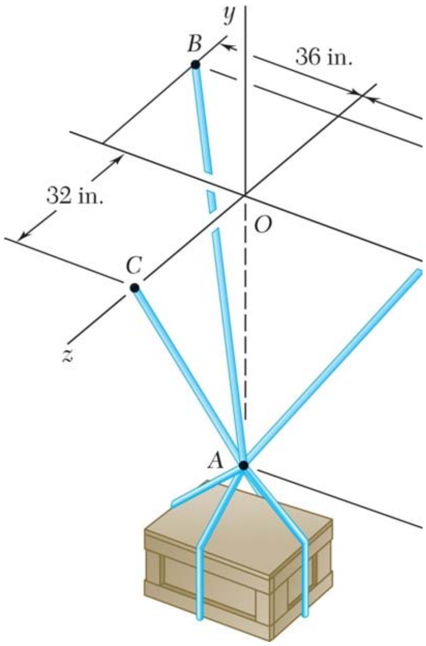
$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0$$

$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0$$

Substituting $T_{AD} = 616\text{ lb}$ in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms, gives:

$T_{AB} = 667.67\text{ lb}$

$T_{AC} = 969.00\text{ lb}$ $W = 1868\text{ lb}$ ◀



PROBLEM 2.84

A crate is supported by three cables as shown. Determine the weight of the crate knowing that the tension in cable AC is 544 lb.

SOLUTION

See Problem 2.83 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-0.48T_{AB} + 0.51948T_{AD} = 0 \quad (1)$$

$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0 \quad (2)$$

$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0 \quad (3)$$

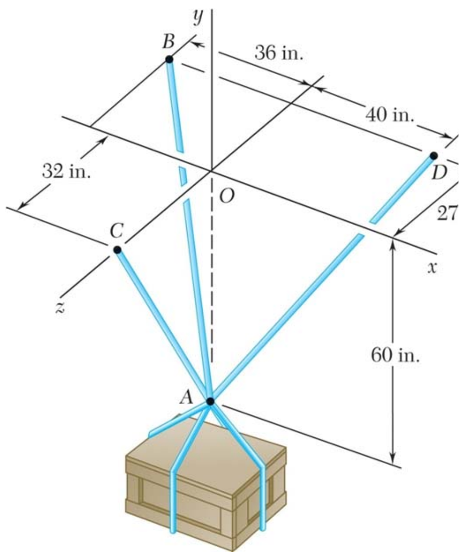
Substituting $T_{AC} = 544\text{ lb}$ in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms, gives:

$$T_{AB} = 374.27\text{ lb}$$

$$T_{AD} = 345.82\text{ lb}$$

$W = 1049\text{ lb}$ ◀

PROBLEM 2.85



A 1600-lb crate is supported by three cables as shown. Determine the tension in each cable.

SOLUTION

See Problem 2.83 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-0.48T_{AB} + 0.51948T_{AD} = 0 \tag{1}$$

$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0 \tag{2}$$

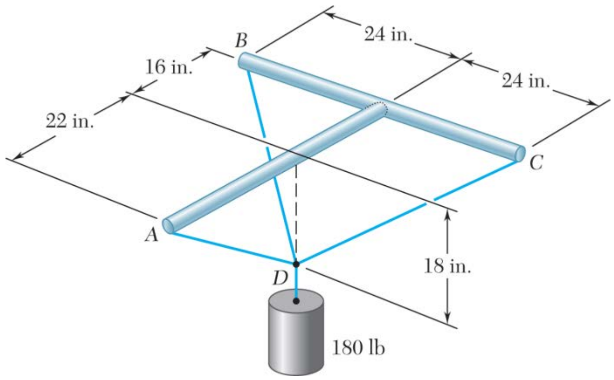
$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0 \tag{3}$$

Substituting $W = 1600$ lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms, gives

$T_{AB} = 571$ lb ◀

$T_{AC} = 830$ lb ◀

$T_{AD} = 528$ lb ◀

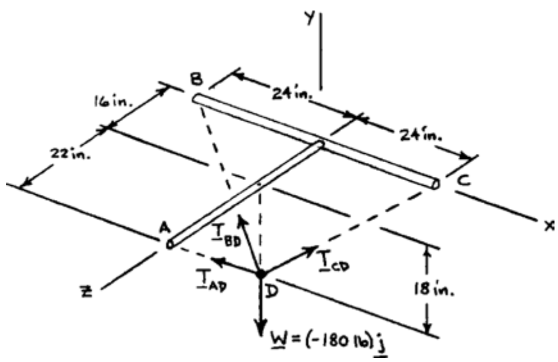


PROBLEM 2.86

Three wires are connected at point D, which is located 18 in. below the T-shaped pipe support ABC. Determine the tension in each wire when a 180-lb cylinder is suspended from point D as shown.

SOLUTION

Free-Body Diagram of Point *D*:



The forces applied at D are:

$$\mathbf{T}_{DA}, \mathbf{T}_{DB}, \mathbf{T}_{DC} \text{ and } \mathbf{W}$$

where $\mathbf{W} = -180.0 \text{ lb}\mathbf{j}$. To express the other forces in terms of the unit vectors $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$, we write

$$\overrightarrow{DA} = (18 \text{ in.})\mathbf{j} + (22 \text{ in.})\mathbf{k}$$
$$DA = 28.425 \text{ in.}$$
$$\overrightarrow{DB} = -(24 \text{ in.})\mathbf{i} + (18 \text{ in.})\mathbf{j} - (16 \text{ in.})\mathbf{k}$$
$$DB = 34.0 \text{ in.}$$
$$\overrightarrow{DC} = (24 \text{ in.})\mathbf{i} + (18 \text{ in.})\mathbf{j} - (16 \text{ in.})\mathbf{k}$$
$$DC = 34.0 \text{ in.}$$

SOLUTION (Continued)

and
$$\mathbf{T}_{DA} = T_{Da}\boldsymbol{\lambda}_{DA} = T_{Da}\frac{\overrightarrow{DA}}{DA}$$
$$= (0.63324\mathbf{j} + 0.77397\mathbf{k})T_{DA}$$
$$\mathbf{T}_{DB} = T_{DB}\boldsymbol{\lambda}_{DB} = T_{DB}\frac{\overrightarrow{DB}}{DB}$$
$$= (-0.70588\mathbf{i} + 0.52941\mathbf{j} - 0.47059\mathbf{k})T_{DB}$$
$$\mathbf{T}_{DC} = T_{DC}\boldsymbol{\lambda}_{DC} = T_{DC}\frac{\overrightarrow{DC}}{DC}$$
$$= (0.70588\mathbf{i} + 0.52941\mathbf{j} - 0.47059\mathbf{k})T_{DC}$$

Equilibrium Condition with $\mathbf{W} = -W\mathbf{j}$

$$\Sigma F = 0: \quad \mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} - W\mathbf{j} = 0$$

Substituting the expressions obtained for $\mathbf{T}_{DA}$, $\mathbf{T}_{DB}$, and $\mathbf{T}_{DC}$ and factoring **i**, **j**, and **k**:

$$(-0.70588T_{DB} + 0.70588T_{DC})\mathbf{i}$$
$$(0.63324T_{DA} + 0.52941T_{DB} + 0.52941T_{DC} - W)\mathbf{j}$$
$$(0.77397T_{DA} - 0.47059T_{DB} - 0.47059T_{DC})\mathbf{k}$$

Equating to zero the coefficients of **i**, **j**, **k**:

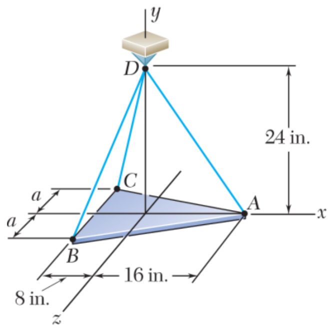
$$-0.70588T_{DB} + 0.70588T_{DC} = 0 \tag{1}$$
$$0.63324T_{DA} + 0.52941T_{DB} + 0.52941T_{DC} - W = 0 \tag{2}$$
$$0.77397T_{DA} - 0.47059T_{DB} - 0.47059T_{DC} = 0 \tag{3}$$

Substituting $W = 180$ lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms gives,

$T_{DA} = 119.7$ lb ◀

$T_{DB} = 98.4$ lb ◀

$T_{DC} = 98.4$ lb ◀



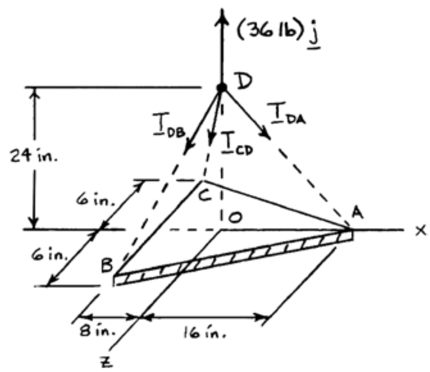
PROBLEM 2.87

A 36-lb triangular plate is supported by three wires as shown. Determine the tension in each wire, knowing that a = 6 in.

SOLUTION

By Symmetry $T_{DB} = T_{DC}$

Free-Body Diagram of Point *D*:



The forces applied at D are: $\mathbf{T}_{DB}, \mathbf{T}_{DC}, \mathbf{T}_{DA}$, and $\mathbf{P}$

where $\mathbf{P} = P\mathbf{j} = (36 \text{ lb})\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{DA} = (16 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} \qquad DA = 28.844 \text{ in.}$$

$$\overrightarrow{DB} = -(8 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} + (6 \text{ in.})\mathbf{k} \qquad DB = 26.0 \text{ in.}$$

$$\overrightarrow{DC} = -(8 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} - (6 \text{ in.})\mathbf{k} \qquad DC = 26.0 \text{ in.}$$

and

$$\mathbf{T}_{DA} = T_{DA}\boldsymbol{\lambda}_{DA} = T_{DA}\frac{\overrightarrow{DA}}{DA} = (0.55471\mathbf{i} - 0.83206\mathbf{j})T_{DA}$$

$$\mathbf{T}_{DB} = T_{DB}\boldsymbol{\lambda}_{DB} = T_{DB}\frac{\overrightarrow{DB}}{DB} = (-0.30769\mathbf{i} - 0.92308\mathbf{j} + 0.23077\mathbf{k})T_{DB}$$

$$\mathbf{T}_{DC} = T_{DC}\boldsymbol{\lambda}_{DC} = T_{DC}\frac{\overrightarrow{DC}}{DC} = (-0.30769\mathbf{i} - 0.92308\mathbf{j} - 0.23077\mathbf{k})T_{DC}$$

SOLUTION (Continued)

Equilibrium condition: $\Sigma F = 0$: $\mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} + (36 \text{ lb})\mathbf{j} = 0$

Substituting the expressions obtained for $\mathbf{T}_{DA}$, $\mathbf{T}_{DB}$, and $\mathbf{T}_{DC}$ and factoring **i**, **j**, and **k**:

$$(0.55471T_{DA} - 0.30769T_{DB} - 0.30769T_{DC})\mathbf{i} + (-0.83206T_{DA} - 0.92308T_{DB} - 0.92308T_{DC} + 36 \text{ lb})\mathbf{j}$$
$$+ (0.23077T_{DB} - 0.23077T_{DC})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

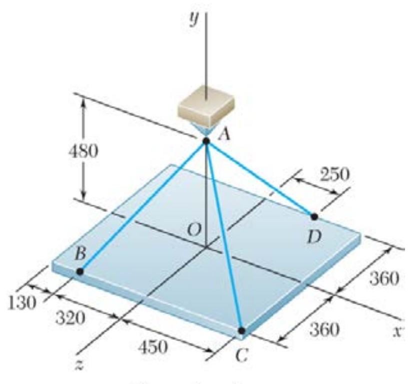
$$0.55471T_{DA} - 0.30769T_{DB} - 0.30769T_{DC} = 0 \qquad (1)$$

$$-0.83206T_{DA} - 0.92308T_{DB} - 0.92308T_{DC} + 36 \text{ lb} = 0 \qquad (2)$$

$$0.23077T_{DB} - 0.23077T_{DC} = 0 \qquad (3)$$

Equation (3) confirms that $T_{DB} = T_{DC}$. Solving simultaneously gives,

$$T_{DA} = 14.42 \text{ lb}; \qquad T_{DB} = T_{DC} = 13.00 \text{ lb} \blacktriangleleft$$



Dimensions in mm

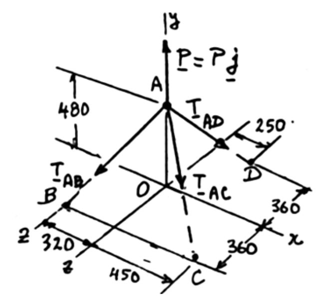
PROBLEM 2.88

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AC is 60 N, determine the weight of the plate.

SOLUTION

We note that the weight of the plate is equal in magnitude to the force $\mathbf{P}$ exerted by the support on Point A.

Free Body A:



Dimensions in mm

$$\Sigma F = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$$

We have:

$$\overrightarrow{AB} = -(320\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AB = 680\text{ mm}$$

$$\overrightarrow{AC} = (450\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AC = 750\text{ mm}$$

$$\overrightarrow{AD} = (250\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} - (360\text{ mm})\mathbf{k} \qquad AD = 650\text{ mm}$$

Thus:

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = \left(-\frac{8}{17}\mathbf{i} - \frac{12}{17}\mathbf{j} + \frac{9}{17}\mathbf{k}\right)T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (0.6\mathbf{i} - 0.64\mathbf{j} + 0.48\mathbf{k})T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = \left(\frac{5}{13}\mathbf{i} - \frac{9.6}{13}\mathbf{j} - \frac{7.2}{13}\mathbf{k}\right)T_{AD}$$

Substituting into the Eq. $\Sigma F = 0$ and factoring $\mathbf{i}, \mathbf{j}, \mathbf{k}$:

$$\left(-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD}\right)\mathbf{i}$$

$$+\left(-\frac{12}{17}T_{AB} - 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P\right)\mathbf{j}$$

$$+\left(\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD}\right)\mathbf{k} = 0$$

SOLUTION (Continued)

Setting the coefficient of **i**, **j**, **k** equal to zero:

$$\mathbf{i}: \qquad -\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0 \tag{1}$$

$$\mathbf{j}: \qquad -\frac{12}{7}T_{AB} - 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P = 0 \tag{2}$$

$$\mathbf{k}: \qquad \frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0 \tag{3}$$

Making $T_{AC} = 60 \text{ N}$ in (1) and (3):

$$-\frac{8}{17}T_{AB} + 36 \text{ N} + \frac{5}{13}T_{AD} = 0 \tag{1′}$$

$$\frac{9}{17}T_{AB} + 28.8 \text{ N} - \frac{7.2}{13}T_{AD} = 0 \tag{3′}$$

Multiply (1′) by 9, (3′) by 8, and add:

$$554.4 \text{ N} - \frac{12.6}{13}T_{AD} = 0 \quad T_{AD} = 572.0 \text{ N}$$

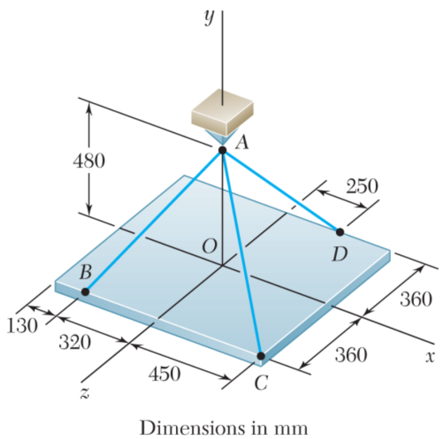
Substitute into (1′) and solve for T_{AB}:

$$T_{AB} = \frac{17}{8}\left(36 + \frac{5}{13} \times 572\right) \qquad T_{AB} = 544.0 \text{ N}$$

Substitute for the tensions in Eq. (2) and solve for P:

$$P = \frac{12}{17}(544 \text{ N}) + 0.64(60 \text{ N}) + \frac{9.6}{13}(572 \text{ N})$$
$$= 844.8 \text{ N}$$

Weight of plate $= P = 845 \text{ N}$ ◀



PROBLEM 2.89

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable *AD* is 520 N, determine the weight of the plate.

SOLUTION

See Problem 2.88 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0 \qquad (1)$$

$$-\frac{12}{17}T_{AB} + 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P = 0 \qquad (2)$$

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0 \qquad (3)$$

Making $T_{AD} = 520$ N in Eqs. (1) and (3):

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + 200 \text{ N} = 0 \qquad (1')$$

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - 288 \text{ N} = 0 \qquad (3')$$

Multiply (1′) by 9, (3′) by 8, and add:

$$9.24T_{AC} - 504 \text{ N} = 0 \quad T_{AC} = 54.5455 \text{ N}$$

Substitute into (1′) and solve for T_{AB}:

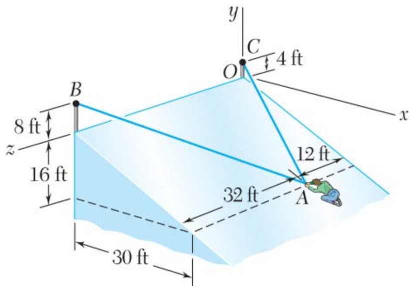
$$T_{AB} = \frac{17}{8}(0.6 \times 54.5455 + 200) \quad T_{AB} = 494.545 \text{ N}$$

Substitute for the tensions in Eq. (2) and solve for *P*:

$$P = \frac{12}{17}(494.545 \text{ N}) + 0.64(54.5455 \text{ N}) + \frac{9.6}{13}(520 \text{ N})$$

$$= 768.00 \text{ N}$$

Weight of plate $= P = 768$ N ◀

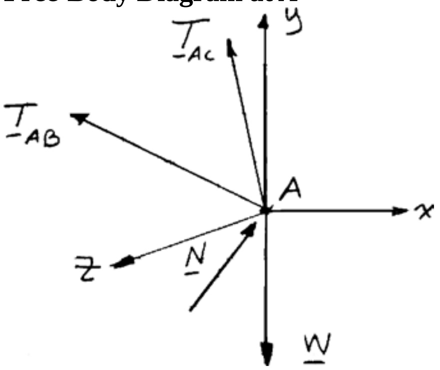


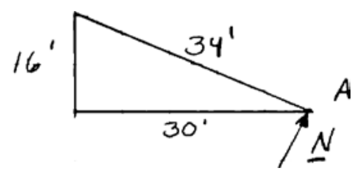
PROBLEM 2.90

In trying to move across a slippery icy surface, a 175-lb man uses two ropes *AB* and *AC*. Knowing that the force exerted on the man by the icy surface is perpendicular to that surface, determine the tension in each rope.

SOLUTION

Free-Body Diagram at *A*





$$\mathbf{N} = N\left(\frac{16}{34}\mathbf{i} + \frac{30}{34}\mathbf{j}\right)$$

and $\mathbf{W} = W\,\mathbf{j} = -(175\text{ lb})\mathbf{j}$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\frac{(-30\text{ ft})\mathbf{i} + (20\text{ ft})\mathbf{j} - (12\text{ ft})\mathbf{k}}{38\text{ ft}}$$

$$= T_{AC}\left(-\frac{15}{19}\mathbf{i} + \frac{10}{19}\mathbf{j} - \frac{6}{19}\mathbf{k}\right)$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = T_{AB}\frac{(-30\text{ ft})\mathbf{i} + (24\text{ ft})\mathbf{j} + (32\text{ ft})\mathbf{k}}{50\text{ ft}}$$

$$= T_{AB}\left(-\frac{15}{25}\mathbf{i} + \frac{12}{25}\mathbf{j} + \frac{16}{25}\mathbf{k}\right)$$

Equilibrium condition: $\Sigma\mathbf{F} = 0$

$$\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{N} + \mathbf{W} = 0$$

SOLUTION (Continued)

Substituting the expressions obtained for $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{N},$ and **W**; factoring **i**, **j**, and **k**; and equating each of the coefficients to zero gives the following equations:

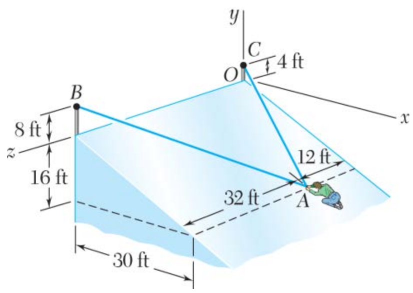
From **i**:
$$-\frac{15}{25}T_{AB} - \frac{15}{19}T_{AC} + \frac{16}{34}N = 0 \tag{1}$$

From **j**:
$$\frac{12}{25}T_{AB} + \frac{10}{19}T_{AC} + \frac{30}{34}N - (175\text{ lb}) = 0 \tag{2}$$

From **k**:
$$\frac{16}{25}T_{AB} - \frac{6}{19}T_{AC} = 0 \tag{3}$$

Solving the resulting set of equations gives:

$$T_{AB} = 30.8\text{ lb}; \;\; T_{AC} = 62.5\text{ lb} \;\blacktriangleleft$$



PROBLEM 2.91

Solve Problem 2.90, assuming that a friend is helping the man at A by pulling on him with a force $\mathbf{P} = -(45\text{ lb})\mathbf{k}$.

PROBLEM 2.90 In trying to move across a slippery icy surface, a 175-lb man uses two ropes AB and AC. Knowing that the force exerted on the man by the icy surface is perpendicular to that surface, determine the tension in each rope.

SOLUTION

Refer to Problem 2.90 for the figure and analysis leading to the following set of equations, Equation (3) being modified to include the additional force $\mathbf{P} = (-45\text{ lb})\mathbf{k}$.

$$-\frac{15}{25}T_{AB} - \frac{15}{19}T_{AC} + \frac{16}{34}N = 0 \tag{1}$$

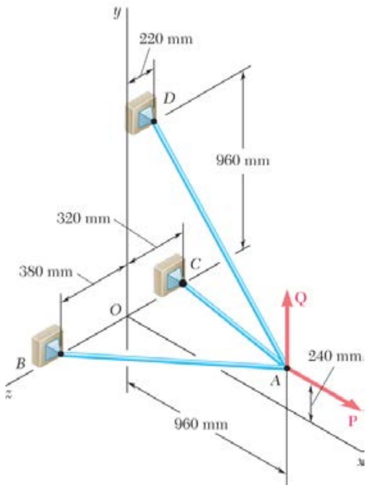
$$\frac{12}{25}T_{AB} + \frac{10}{19}T_{AC} + \frac{30}{34}N - (175\text{ lb}) = 0 \tag{2}$$

$$\frac{16}{25}T_{AB} - \frac{6}{19}T_{AC} - (45\text{ lb}) = 0 \tag{3}$$

Solving the resulting set of equations simultaneously gives:

$$T_{AB} = 81.3\text{ lb} \blacktriangleleft$$

$$T_{AC} = 22.2\text{ lb} \blacktriangleleft$$



PROBLEM 2.92

Three cables are connected at A, where the forces **P** and **Q** are applied as shown. Knowing that $Q = 0$, find the value of P for which the tension in cable AD is 305 N.

SOLUTION

$$\Sigma \mathbf{F}_A = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{P} = 0 \quad \text{where} \quad \mathbf{P} = P\mathbf{i}$$

$$\overrightarrow{AB} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} + (380 \text{ mm})\mathbf{k} \qquad AB = 1060 \text{ mm}$$

$$\overrightarrow{AC} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k} \qquad AC = 1040 \text{ mm}$$

$$\overrightarrow{AD} = -(960 \text{ mm})\mathbf{i} + (720 \text{ mm})\mathbf{j} - (220 \text{ mm})\mathbf{k} \qquad AD = 1220 \text{ mm}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = T_{AB}\left(-\frac{48}{53}\mathbf{i} - \frac{12}{53}\mathbf{j} + \frac{19}{53}\mathbf{k}\right)$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\left(-\frac{12}{13}\mathbf{i} - \frac{3}{13}\mathbf{j} - \frac{4}{13}\mathbf{k}\right)$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = \frac{305 \text{ N}}{1220 \text{ mm}}[(-960 \text{ mm})\mathbf{i} + (720 \text{ mm})\mathbf{j} - (220 \text{ mm})\mathbf{k}]$$

$$= -(240 \text{ N})\mathbf{i} + (180 \text{ N})\mathbf{j} - (55 \text{ N})\mathbf{k}$$

Substituting into $\Sigma \mathbf{F}_A = 0$, factoring $\mathbf{i}, \mathbf{j}, \mathbf{k}$, and setting each coefficient equal to ϕ gives:

$$\mathbf{i}: \quad P = \frac{48}{53}T_{AB} + \frac{12}{13}T_{AC} + 240 \text{ N} \tag{1}$$

$$\mathbf{j}: \quad \frac{12}{53}T_{AB} + \frac{3}{13}T_{AC} = 180 \text{ N} \tag{2}$$

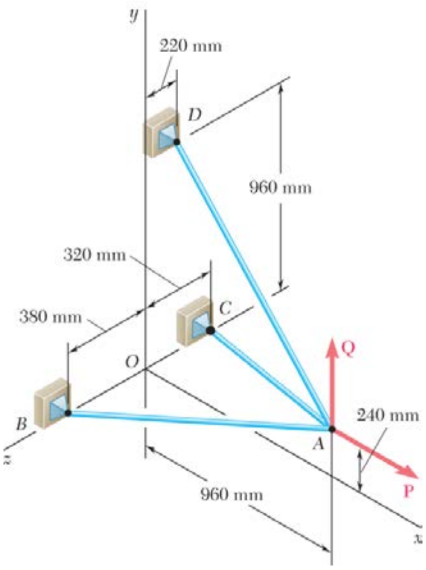
$$\mathbf{k}: \quad \frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} = 55 \text{ N} \tag{3}$$

Solving the system of linear equations using conventional algorithms gives:

$$T_{AB} = 446.71 \text{ N}$$

$$T_{AC} = 341.71 \text{ N}$$

$$P = 960 \text{ N} \blacktriangleleft$$



PROBLEM 2.93

Three cables are connected at A, where the forces $\mathbf{P}$ and $\mathbf{Q}$ are applied as shown. Knowing that $P = 1200$ N, determine the values of Q for which cable AD is taut.

SOLUTION

We assume that $T_{AD} = 0$ and write $\quad \Sigma\mathbf{F}_A = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + Q\mathbf{j} + (1200 \text{ N})\mathbf{i} = 0$

$$\overrightarrow{AB} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} + (380 \text{ mm})\mathbf{k} \quad AB = 1060 \text{ mm}$$

$$\overrightarrow{AC} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k} \quad AC = 1040 \text{ mm}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = \left(-\frac{48}{53}\mathbf{i} - \frac{12}{53}\mathbf{j} + \frac{19}{53}\mathbf{k}\right)T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = \left(-\frac{12}{13}\mathbf{i} - \frac{3}{13}\mathbf{j} - \frac{4}{13}\mathbf{k}\right)T_{AC}$$

Substituting into $\Sigma\mathbf{F}_A = 0$, factoring $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$, and setting each coefficient equal to ϕ gives:

$$\mathbf{i}: \quad -\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} + 1200 \text{ N} = 0 \qquad (1)$$

$$\mathbf{j}: \quad -\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + Q = 0 \qquad (2)$$

$$\mathbf{k}: \quad \frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} = 0 \qquad (3)$$

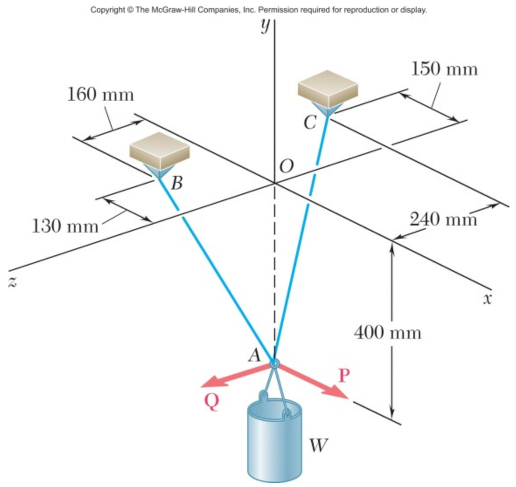
Solving the resulting system of linear equations using conventional algorithms gives:

$$T_{AB} = 605.71 \text{ N}$$

$$T_{AC} = 705.71 \text{ N}$$

$$Q = 300.00 \text{ N} \qquad 0 \le Q < 300 \text{ N} \blacktriangleleft$$

Note: This solution assumes that Q is directed upward as shown $(Q \ge 0)$, if negative values of Q are considered, cable AD remains taut, but AC becomes slack for $Q = -460$ N.

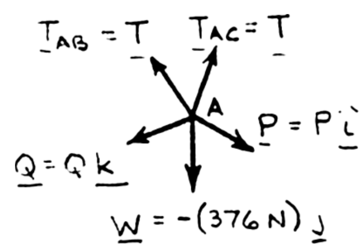


PROBLEM 2.94

A container of weight W is suspended from ring A. Cable BAC passes through the ring and is attached to fixed supports at B and C. Two forces $\mathbf{P} = P\mathbf{i}$ and $\mathbf{Q} = Q\mathbf{k}$ are applied to the ring to maintain the container in the position shown. Knowing that $W = 376$ N, determine P and Q. (*Hint:* The tension is the same in both portions of cable BAC.)

SOLUTION

Free-Body A:



$$\mathbf{T}_{AB} = T\boldsymbol{\lambda}_{AB}$$
$$= T\frac{\overrightarrow{AB}}{AB}$$
$$= T\frac{(-130\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} + (160\text{ mm})\mathbf{k}}{450\text{ mm}}$$
$$= T\left(-\frac{13}{45}\mathbf{i} + \frac{40}{45}\mathbf{j} + \frac{16}{45}\mathbf{k}\right)$$

$$\mathbf{T}_{AC} = T\boldsymbol{\lambda}_{AC}$$
$$= T\frac{\overrightarrow{AC}}{AC}$$
$$= T\frac{(-150\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} + (-240\text{ mm})\mathbf{k}}{490\text{ mm}}$$
$$= T\left(-\frac{15}{49}\mathbf{i} + \frac{40}{49}\mathbf{j} - \frac{24}{49}\mathbf{k}\right)$$

$$\Sigma F = 0{:}\quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{Q} + \mathbf{P} + \mathbf{W} = 0$$

Setting coefficients of **i**, **j**, **k** equal to zero:

$$\mathbf{i}{:}\quad -\frac{13}{45}T - \frac{15}{49}T + P = 0 \qquad 0.59501T = P \qquad (1)$$

$$\mathbf{j}{:}\quad +\frac{40}{45}T + \frac{40}{49}T - W = 0 \qquad 1.70521T = W \qquad (2)$$

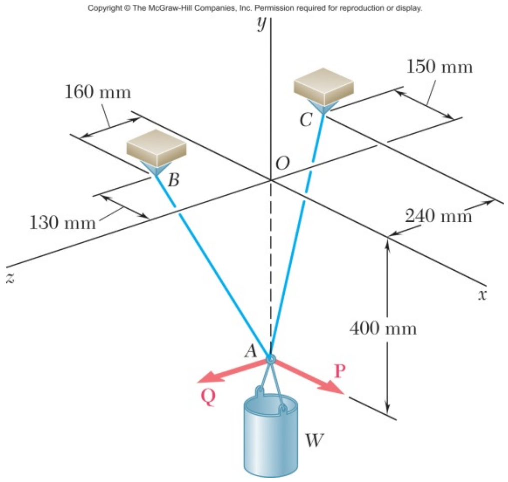
$$\mathbf{k}{:}\quad +\frac{16}{45}T - \frac{24}{49}T + Q = 0 \qquad 0.134240T = Q \qquad (3)$$

PROBLEM 2.94 (Continued)

Data: $W = 376\text{ N} \quad 1.70521T = 376\text{ N} \quad T = 220.50\text{ N}$

$$0.59501(220.50\text{ N}) = P \qquad P = 131.2\text{ N} \blacktriangleleft$$

$$0.134240(220.50\text{ N}) = Q \qquad Q = 29.6\text{ N} \blacktriangleleft$$



PROBLEM 2.95

For the system of Problem 2.94, determine W and Q knowing that $P = 164$ N.

PROBLEM 2.94 A container of weight W is suspended from ring A. Cable BAC passes through the ring and is attached to fixed supports at B and C. Two forces $\mathbf{P} = P\mathbf{i}$ and $\mathbf{Q} = Q\mathbf{k}$ are applied to the ring to maintain the container in the position shown. Knowing that $W = 376$ N, determine P and Q. (*Hint:* The tension is the same in both portions of cable BAC.)

SOLUTION

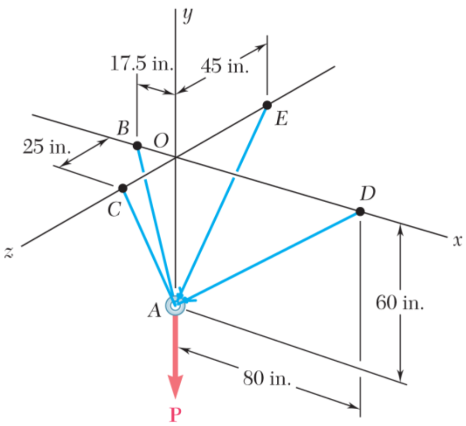
Refer to Problem 2.94 for the figure and analysis resulting in Equations (1), (2), and (3) for P, W, and Q in terms of T below. Setting $P = 164$ N we have:

Eq. (1): $0.59501T = 164$ N $\qquad T = 275.63$ N

Eq. (2): $1.70521(275.63\text{ N}) = W \qquad W = 470$ N ◀

Eq. (3): $0.134240(275.63\text{ N}) = Q \qquad Q = 37.0$ N ◀

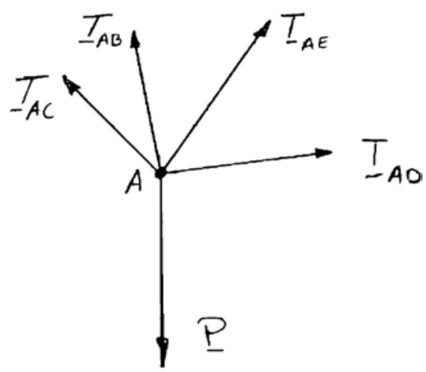
PROBLEM 2.96



Cable *BAC* passes through a frictionless ring *A* and is attached to fixed supports at *B* and *C*, while cables *AD* and *AE* are both tied to the ring and are attached, respectively, to supports at *D* and *E*. Knowing that a 200-lb vertical load **P** is applied to ring *A*, determine the tension in each of the three cables.

SOLUTION

Free Body Diagram at *A*:



Since T_{BAC} = tension in cable *BAC*, it follows that

$$T_{AB} = T_{AC} = T_{BAC}$$

$$\mathbf{T}_{AB} = T_{BAC}\boldsymbol{\lambda}_{AB} = T_{BAC}\frac{(-17.5\text{ in.})\mathbf{i} + (60\text{ in.})\mathbf{j}}{62.5\text{ in.}} = T_{BAC}\left(\frac{-17.5}{62.5}\mathbf{i} + \frac{60}{62.5}\mathbf{j}\right)$$

$$\mathbf{T}_{AC} = T_{BAC}\boldsymbol{\lambda}_{AC} = T_{BAC}\frac{(60\text{ in.})\mathbf{i} + (25\text{ in.})\mathbf{k}}{65\text{ in.}} = T_{BAC}\left(\frac{60}{65}\mathbf{j} + \frac{25}{65}\mathbf{k}\right)$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{(80\text{ in.})\mathbf{i} + (60\text{ in.})\mathbf{j}}{100\text{ in.}} = T_{AD}\left(\frac{4}{5}\mathbf{i} + \frac{3}{5}\mathbf{j}\right)$$

$$\mathbf{T}_{AE} = T_{AE}\boldsymbol{\lambda}_{AE} = T_{AE}\frac{(60\text{ in.})\mathbf{j} - (45\text{ in.})\mathbf{k}}{75\text{ in.}} = T_{AE}\left(\frac{4}{5}\mathbf{j} - \frac{3}{5}\mathbf{k}\right)$$

SOLUTION Continued

Substituting into $\Sigma \mathbf{F}_A = 0$, setting $\mathbf{P} = (-200 \text{ lb})\mathbf{j}$, and setting the coefficients of $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$ equal to ϕ, we obtain the following three equilibrium equations:

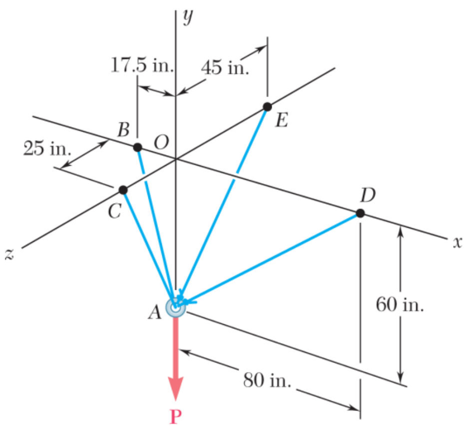
From $\mathbf{i}$: $$-\frac{17.5}{62.5}T_{BAC} + \frac{4}{5}T_{AD} = 0 \qquad (1)$$

From $\mathbf{j}$: $$\left(\frac{60}{62.5} + \frac{60}{65}\right)T_{BAC} + \frac{3}{5}T_{AD} + \frac{4}{5}T_{AE} - 200 \text{ lb} = 0 \qquad (2)$$

From $\mathbf{k}$: $$\frac{25}{65}T_{BAC} - \frac{3}{5}T_{AE} = 0 \qquad (3)$$

Solving the system of linear equations using conventional algorithms gives:

$T_{BAC} = 76.7 \text{ lb}$; $T_{AD} = 26.9 \text{ lb}$; $T_{AE} = 49.2 \text{ lb}$ ◀



PROBLEM 2.97

Knowing that the tension in cable *AE* of Prob. 2.96 is 75 lb, determine (*a*) the magnitude of the load **P**, (*b*) the tension in cables *BAC* and *AD*.

PROBLEM 2.96 Cable *BAC* passes through a frictionless ring *A* and is attached to fixed supports at *B* and *C*, while cables *AD* and *AE* are both tied to the ring and are attached, respectively, to supports at *D* and *E*. Knowing that a 200-lb vertical load **P** is applied to ring *A*, determine the tension in each of the three cables.

SOLUTION

Refer to the solution to Problem 2.96 for the figure and analysis leading to the following set of equilibrium equations, Equation (2) being modified to include $P\mathbf{j}$ as an unknown quantity:

$$-\frac{17.5}{62.5}T_{BAC} + \frac{4}{5}T_{AD} = 0 \tag{1}$$

$$\left(\frac{60}{62.5} + \frac{60}{65}\right)T_{BAC} + \frac{3}{5}T_{AD} + \frac{4}{5}T_{AE} - P = 0 \tag{2}$$

$$\frac{25}{65}T_{BAC} - \frac{3}{5}T_{AE} = 0 \quad (3)$$

Substituting for $T_{AE} = 75 \text{ lb}$ and solving simultaneously gives:

(*a*) $P = 305 \text{ lb}$ ◀

(*b*) $T_{BAC} = 117.0 \text{ lb}; \; T_{AD} = 40.9 \text{ lb}$ ◀

SOLUTION Continued

Then from the specifications of the problem, $y = 155\text{ mm} = 0.155\text{ m}$

$$z^2 = 0.23563\text{ m}^2 - (0.155\text{ m})^2$$
$$z = 0.46\text{ m}$$

and

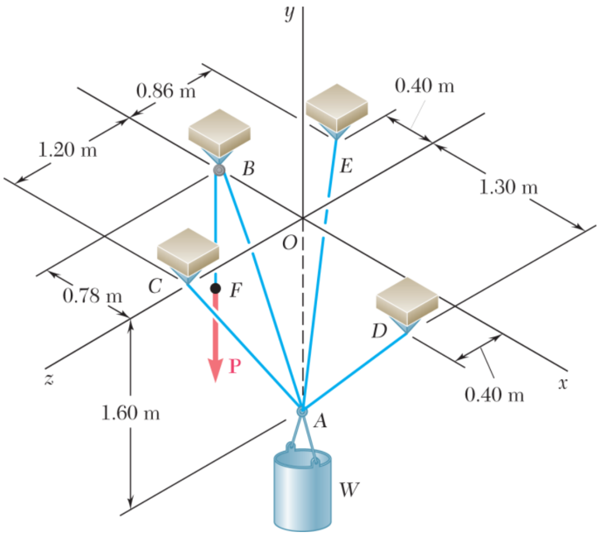
(*a*)
$$T_{AB} = \frac{341\text{ N}}{0.155(1.90476)}$$
$$= 1155.00\text{ N}$$

or $T_{AB} = 1155\text{ N}$ ◀

and

(*b*)
$$Q = \frac{341\text{ N}(0.46\text{ m})(0.866)}{(0.155\text{ m})}$$
$$= (1012.00\text{ N})$$

or $Q = 1012\text{ N}$ ◀



PROBLEM 2.98

A container of weight W is suspended from ring A, to which cables AC and AE are attached. A force $\mathbf{P}$ is applied to the end F of a third cable that passes over a pulley at B and through ring A and that is attached to a support at D. Knowing that $W = 1000$ N, determine the magnitude of P. (*Hint:* The tension is the same in all portions of cable $FBAD$.)

SOLUTION

The (vector) force in each cable can be written as the product of the (scalar) force and the unit vector along the cable. That is, with

$$\overrightarrow{AB} = -(0.78\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0\text{ m})\mathbf{k}$$

$$AB = \sqrt{(-0.78\text{ m})^2 + (1.6\text{ m})^2 + (0)^2}$$

$$= 1.78\text{ m}$$

$$\mathbf{T}_{AB} = T\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$

$$= \frac{T_{AB}}{1.78\text{ m}}[-(0.78\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0\text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AB} = T_{AB}(-0.4382\mathbf{i} + 0.8989\mathbf{j} + 0\mathbf{k})$$

and

$$\overrightarrow{AC} = (0)\mathbf{i} + (1.6\text{ m})\mathbf{j} + (1.2\text{ m})\mathbf{k}$$

$$AC = \sqrt{(0\text{ m})^2 + (1.6\text{ m})^2 + (1.2\text{ m})^2} = 2\text{ m}$$

$$\mathbf{T}_{AC} = T\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = \frac{T_{AC}}{2\text{ m}}[(0)\mathbf{i} + (1.6\text{ m})\mathbf{j} + (1.2\text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AC} = T_{AC}(0.8\mathbf{j} + 0.6\mathbf{k})$$

and

$$\overrightarrow{AD} = (1.3\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0.4\text{ m})\mathbf{k}$$

$$AD = \sqrt{(1.3\text{ m})^2 + (1.6\text{ m})^2 + (0.4\text{ m})^2} = 2.1\text{ m}$$

$$\mathbf{T}_{AD} = T\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = \frac{T_{AD}}{2.1\text{ m}}[(1.3\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0.4\text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AD} = T_{AD}(0.6190\mathbf{i} + 0.7619\mathbf{j} + 0.1905\mathbf{k})$$

SOLUTION Continued

Finally,
$$\overrightarrow{AE} = -(0.4\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} - (0.86\text{ m})\mathbf{k}$$
$$AE = \sqrt{(-0.4\text{ m})^2 + (1.6\text{ m})^2 + (-0.86\text{ m})^2} = 1.86\text{ m}$$
$$\mathbf{T}_{AE} = T\boldsymbol{\lambda}_{AE} = T_{AE}\frac{\overrightarrow{AE}}{AE}$$
$$= \frac{T_{AE}}{1.86\text{ m}}[-(0.4\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} - (0.86\text{ m})\mathbf{k}]$$
$$\mathbf{T}_{AE} = T_{AE}(-0.2151\mathbf{i} + 0.8602\mathbf{j} - 0.4624\mathbf{k})$$

With the weight of the container $\mathbf{W} = -W\mathbf{j}$, at A we have:

$$\Sigma\mathbf{F} = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} - W\mathbf{j} = 0$$

Equating the factors of **i**, **j**, and **k** to zero, we obtain the following linear algebraic equations:

$$-0.4382T_{AB} + 0.6190T_{AD} - 0.2151T_{AE} = 0 \tag{1}$$

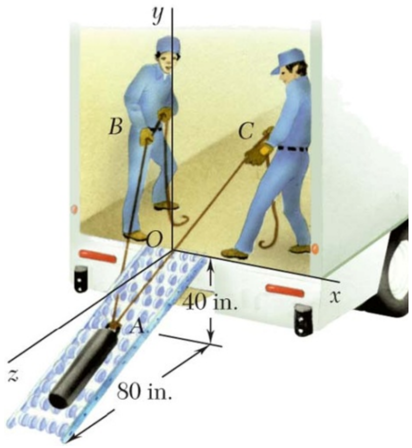
$$0.8989T_{AB} + 0.8T_{AC} + 0.7619T_{AD} + 0.8602T_{AE} - W = 0 \tag{2}$$

$$0.6T_{AC} + 0.1905T_{AD} - 0.4624T_{AE} = 0 \tag{3}$$

Knowing that $W = 1000\text{ N}$ and that because of the pulley system at $B\,T_{AB} = T_{AD} = P$, where P is the externally applied (unknown) force, we can solve the system of linear Equations (1), (2) and (3) uniquely for P.

$P = 378\text{ N}$ ◀

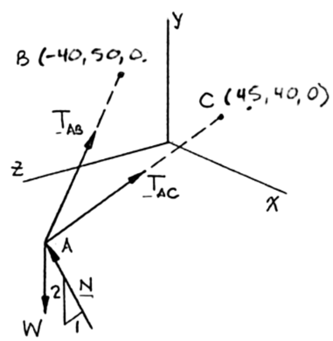
PROBLEM 2.99



Using two ropes and a roller chute, two workers are unloading a 200-lb cast-iron counterweight from a truck. Knowing that at the instant shown the counterweight is kept from moving and that the positions of Points *A*, *B*, and *C* are, respectively, *A*(0, –20 in., 40 in.), *B*(–40 in., 50 in., 0), and *C*(45 in., 40 in., 0), and assuming that no friction exists between the counterweight and the chute, determine the tension in each rope. (*Hint*: Since there is no friction, the force exerted by the chute on the counterweight must be perpendicular to the chute.)

SOLUTION

From the geometry of the chute:



$$\mathbf{N} = \frac{N}{\sqrt{5}}(2\mathbf{j} + \mathbf{k})$$
$$= N(0.8944\mathbf{j} + 0.4472\mathbf{k})$$

The force in each rope can be written as the product of the magnitude of the force and the unit vector along the cable. Thus, with

$$\overrightarrow{AB} = (40 \text{ in.})\mathbf{i} + (70 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}$$
$$AB = \sqrt{(40 \text{ in.})^2 + (70 \text{ in.})^2 + (40 \text{ in.})^2}$$
$$= 90 \text{ in.}$$
$$\mathbf{T}_{AB} = T\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$
$$= \frac{T_{AB}}{90 \text{ in.}}[(-40 \text{ in.})\mathbf{i} + (70 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}]$$
$$\mathbf{T}_{AB} = T_{AB}\left(-\frac{4}{9}\mathbf{i} + \frac{7}{9}\mathbf{j} - \frac{4}{9}\mathbf{k}\right)$$

and

$$\overrightarrow{AC} = (45 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}$$
$$AC = \sqrt{(45 \text{ in.})^2 + (60 \text{ in.})^2 + (40 \text{ in.})^2} = 85 \text{ in.}$$
$$\mathbf{T}_{AC} = T\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC}$$
$$= \frac{T_{AC}}{85 \text{ in.}}[(45 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (40 \text{ in.})\mathbf{k}]$$
$$\mathbf{T}_{AC} = T_{AC}\left(\frac{9}{17}\mathbf{i} + \frac{12}{17}\mathbf{j} - \frac{8}{17}\mathbf{k}\right)$$

Then: $\Sigma\mathbf{F} = 0: \quad \mathbf{N} + \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{W} = 0$

SOLUTION Continued

With $W = 200$ lb, and equating the factors of **i**, **j**, and **k** to zero, we obtain the linear algebraic equations:

$$\mathbf{i}: \quad -\frac{4}{9}T_{AB} + \frac{9}{17}T_{AC} = 0 \tag{1}$$

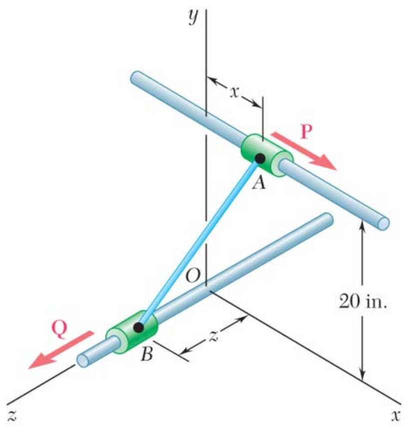
$$\mathbf{j}: \quad \frac{7}{9}T_{AB} + \frac{12}{17}T_{AC} + \frac{2}{\sqrt{5}} - 200 \text{ lb} = 0 \tag{2}$$

$$\mathbf{k}: \quad -\frac{4}{9}T_{AB} - \frac{8}{17}T_{AC} + \frac{1}{\sqrt{5}}N = 0 \tag{3}$$

Using conventional methods for solving linear algebraic equations we obtain:

$T_{AB} = 65.6$ lb ◀

$T_{AC} = 55.1$ lb ◀



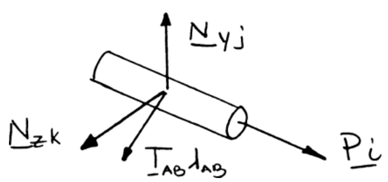
PROBLEM 2.100

Collars A and B are connected by a 25-in.-long wire and can slide freely on frictionless rods. If a 60-lb force $\mathbf{Q}$ is applied to collar B as shown, determine (*a*) the tension in the wire when $x = 9$ in., (*b*) the corresponding magnitude of the force $\mathbf{P}$ required to maintain the equilibrium of the system.

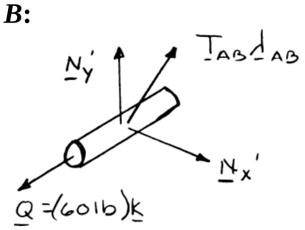
SOLUTION

Free-Body Diagrams of Collars:

***A*:**



***B*:**



$$\boldsymbol{\lambda}_{AB} = \frac{\overrightarrow{AB}}{AB} = \frac{-x\mathbf{i} - (20\text{ in.})\mathbf{j} + z\mathbf{k}}{25\text{ in.}}$$

Collar A: $\Sigma\mathbf{F} = 0$: $\quad P\mathbf{i} + N_y\mathbf{j} + N_z\mathbf{k} + T_{AB}\boldsymbol{\lambda}_{AB} = 0$

Substitute for $\boldsymbol{\lambda}_{AB}$ and set coefficient of $\mathbf{i}$ equal to zero:

$$P - \frac{T_{AB}x}{25\text{ in.}} = 0 \qquad (1)$$

Collar B: $\Sigma\mathbf{F} = 0$: $\quad (60\text{ lb})\mathbf{k} + N'_x\mathbf{i} + N'_y\mathbf{j} - T_{AB}\boldsymbol{\lambda}_{AB} = 0$

Substitute for $\boldsymbol{\lambda}_{AB}$ and set coefficient of $\mathbf{k}$ equal to zero:

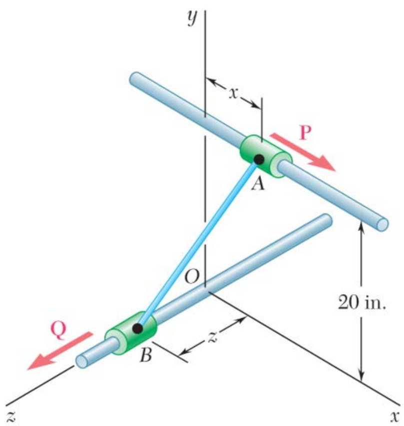
$$60\text{ lb} - \frac{T_{AB}z}{25\text{ in.}} = 0 \qquad (2)$$

(*a*) $\quad x = 9$ in. $\quad (9\text{ in.})^2 + (20\text{ in.})^2 + z^2 = (25\text{ in.})^2$

$$z = 12\text{ in.}$$

From Eq. (2): $\quad \dfrac{60\text{ lb} - T_{AB}(12\text{ in.})}{25\text{ in.}} \qquad T_{AB} = 125.0\text{ lb}$ ◀

(*b*) From Eq. (1): $\quad P = \dfrac{(125.0\text{ lb})(9\text{ in.})}{25\text{ in.}} \qquad P = 45.0\text{ lb}$ ◀



PROBLEM 2.101

Collars A and B are connected by a 25-in.-long wire and can slide freely on frictionless rods. Determine the distances x and z for which the equilibrium of the system is maintained when $P = 120$ lb and $Q = 60$ lb.

SOLUTION

See Problem 2.100 for the diagrams and analysis leading to Equations (1) and (2) below:

$$P = \frac{T_{AB}x}{25 \text{ in.}} = 0 \tag{1}$$

$$60 \text{ lb} - \frac{T_{AB}z}{25 \text{ in.}} = 0 \tag{2}$$

For $P = 120$ lb, Eq. (1) yields $\quad T_{AB}x = (25 \text{ in.})(20 \text{ lb}) \quad (1')$

From Eq. (2): $\quad T_{AB}z = (25 \text{ in.})(60 \text{ lb}) \quad (2')$

Dividing Eq. (1′) by (2′), $\quad \frac{x}{z} = 2 \quad (3)$

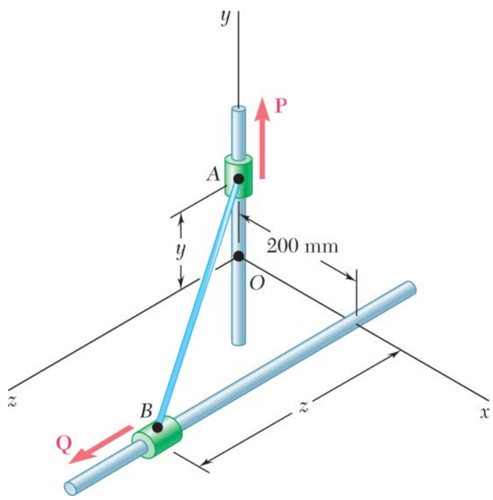
Now write $\quad x^2 + z^2 + (20 \text{ in.})^2 = (25 \text{ in.})^2 \quad (4)$

Solving (3) and (4) simultaneously,

$$4z^2 + z^2 + 400 = 625$$
$$z^2 = 45$$
$$z = 6.7082 \text{ in.}$$

From Eq. (3): $\quad x = 2z = 2(6.7082 \text{ in.})$
$$= 13.4164 \text{ in.}$$

$x = 13.42$ in., $\quad z = 6.71$ in. ◀



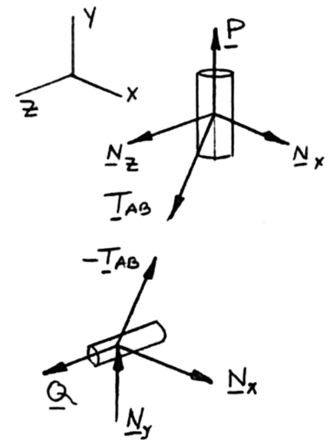
PROBLEM 2.102

Collars A and B are connected by a 525-mm-long wire and can slide freely on frictionless rods. If a force $\mathbf{P} = (341\text{ N})\mathbf{j}$ is applied to collar A, determine (a) the tension in the wire when $y = 155$ mm, (b) the magnitude of the force $\mathbf{Q}$ required to maintain the equilibrium of the system.

SOLUTION

For both Problems 2.102 and 2.103:

Free-Body Diagrams of Collars:



$$(AB)^2 = x^2 + y^2 + z^2$$

Here $$(0.525\text{ m})^2 = (0.20\text{ m})^2 + y^2 + z^2$$

or $$y^2 + z^2 = 0.23563\text{ m}^2$$

Thus, when y given, z is determined,

Now
$$\boldsymbol{\lambda}_{AB} = \frac{\overrightarrow{AB}}{AB}$$
$$= \frac{1}{0.525\text{ m}}(0.20\mathbf{i} - y\mathbf{j} + z\mathbf{k})\text{m}$$
$$= 0.38095\mathbf{i} - 1.90476y\mathbf{j} + 1.90476z\mathbf{k}$$

Where y and z are in units of meters, m.

From the F.B. Diagram of collar A: $\Sigma\mathbf{F} = 0$: $N_x\mathbf{i} + N_z\mathbf{k} + P\mathbf{j} + T_{AB}\lambda_{AB} = 0$

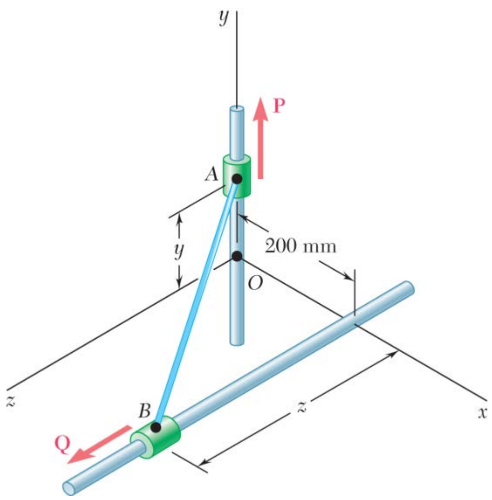
Setting the **j** coefficient to zero gives $P - (1.90476y)T_{AB} = 0$

With $$P = 341\text{ N}$$
$$T_{AB} = \frac{341\text{ N}}{1.90476y}$$

Now, from the free body diagram of collar B: $\Sigma\mathbf{F} = 0$: $N_x\mathbf{i} + N_y\mathbf{j} + Q\mathbf{k} - T_{AB}\boldsymbol{\lambda}_{AB} = 0$

Setting the **k** coefficient to zero gives $Q - T_{AB}(1.90476z) = 0$

And using the above result for T_{AB}, we have $Q = T_{AB}z = \dfrac{341\text{ N}}{(1.90476)y}(1.90476z) = \dfrac{(341\text{ N})(z)}{y}$



PROBLEM 2.103

Solve Problem 2.102 assuming that $y = 275$ mm.

PROBLEM 2.102 Collars *A* and *B* are connected by a 525-mm-long wire and can slide freely on frictionless rods. If a force $\mathbf{P} = (341 \text{ N})\mathbf{j}$ is applied to collar *A*, determine (*a*) the tension in the wire when $y = 155$ mm, (*b*) the magnitude of the force **Q** required to maintain the equilibrium of the system.

SOLUTION

From the analysis of Problem 2.102, particularly the results:

$$y^2 + z^2 = 0.23563 \text{ m}^2$$

$$T_{AB} = \frac{341 \text{ N}}{1.90476 y}$$

$$Q = \frac{341 \text{ N}}{y} z$$

With $y = 275 \text{ mm} = 0.275 \text{ m}$, we obtain:

$$z^2 = 0.23563 \text{ m}^2 - (0.275 \text{ m})^2$$

$$z = 0.40 \text{ m}$$

and

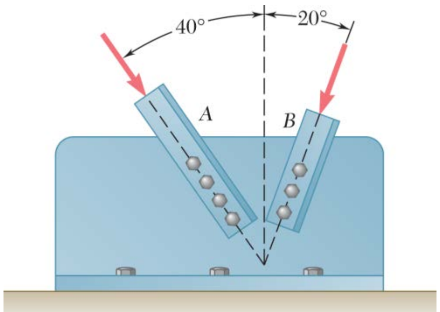
(*a*) $$T_{AB} = \frac{341 \text{ N}}{(1.90476)(0.275 \text{ m})} = 651.00$$

or $$T_{AB} = 651 \text{ N} \blacktriangleleft$$

and

(*b*) $$Q = \frac{341 \text{ N}(0.40 \text{ m})}{(0.275 \text{ m})}$$

or $$Q = 496 \text{ N} \blacktriangleleft$$

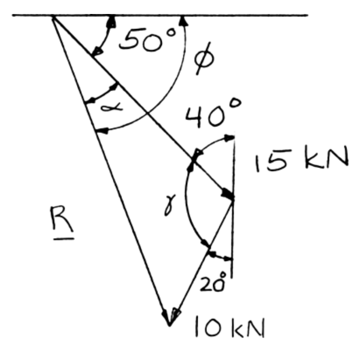


PROBLEM 2.104

Two structural members *A* and *B* are bolted to a bracket as shown. Knowing that both members are in compression and that the force is 15 kN in member *A* and 10 kN in member *B*, determine by trigonometry the magnitude and direction of the resultant of the forces applied to the bracket by members *A* and *B*.

SOLUTION

Using the force triangle and the laws of cosines and sines,



we have

$$\gamma = 180° - (40° + 20°)$$
$$= 120°$$

Then

$$R^2 = (15\text{ kN})^2 + (10\text{ kN})^2 - 2(15\text{ kN})(10\text{ kN})\cos 120°$$
$$= 475\text{ kN}^2$$
$$R = 21.794\text{ kN}$$

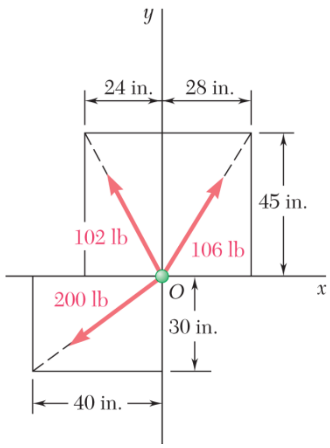
and

$$\frac{10\text{ kN}}{\sin\alpha} = \frac{21.794\text{ kN}}{\sin 120°}$$
$$\sin\alpha = \left(\frac{10\text{ kN}}{21.794\text{ kN}}\right)\sin 120°$$
$$= 0.39737$$
$$\alpha = 23.414$$

Hence:

$$\phi = \alpha + 50° = 73.414$$

R = 21.8 kN ◥ 73.4° ◀

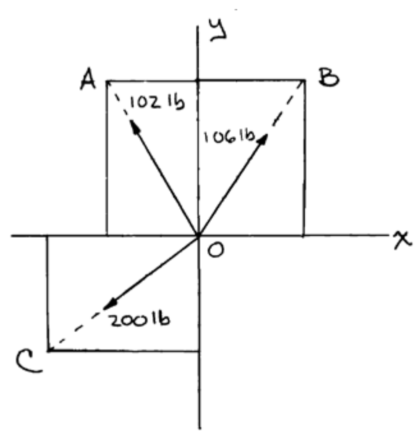


PROBLEM 2.105

Determine the x and y components of each of the forces shown.

SOLUTION

Compute the following distances:



$$OA = \sqrt{(24\text{ in.})^2 + (45\text{ in.})^2}$$
$$= 51.0\text{ in.}$$
$$OB = \sqrt{(28\text{ in.})^2 + (45\text{ in.})^2}$$
$$= 53.0\text{ in.}$$
$$OC = \sqrt{(40\text{ in.})^2 + (30\text{ in.})^2}$$
$$= 50.0\text{ in.}$$

102-lb Force:

$$F_x = -102\text{ lb}\frac{24\text{ in.}}{51.0\text{ in.}} \qquad F_x = -48.0\text{ lb} \blacktriangleleft$$

$$F_y = +102\text{ lb}\frac{45\text{ in.}}{51.0\text{ in.}} \qquad F_y = +90.0\text{ lb} \blacktriangleleft$$

106-lb Force:

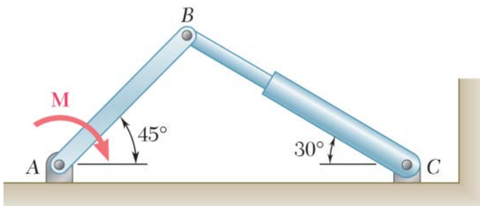
$$F_x = +106\text{ lb}\frac{28\text{ in.}}{53.0\text{ in.}} \qquad F_x = +56.0\text{ lb} \blacktriangleleft$$

$$F_y = +106\text{ lb}\frac{45\text{ in.}}{53.0\text{ in.}} \qquad F_y = +90.0\text{ lb} \blacktriangleleft$$

200-lb Force:

$$F_x = -200\text{ lb}\frac{40\text{ in.}}{50.0\text{ in.}} \qquad F_x = -160.0\text{ lb} \blacktriangleleft$$

$$F_y = -200\text{ lb}\frac{30\text{ in.}}{50.0\text{ in.}} \qquad F_y = -120.0\text{ lb} \blacktriangleleft$$



PROBLEM 2.106

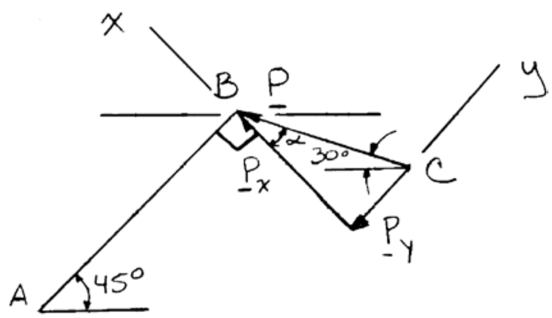
The hydraulic cylinder *BC* exerts on member *AB* a force **P** directed along line *BC*. Knowing that **P** must have a 600-N component perpendicular to member *AB*, determine (*a*) the magnitude of the force **P**, (*b*) its component along line *AB*.

SOLUTION

$$180° = 45° + \alpha + 90° + 30°$$

$$\alpha = 180° - 45° - 90° - 30°$$

$$= 15°$$



(*a*)

$$\cos\alpha = \frac{P_x}{P}$$

$$P = \frac{P_x}{\cos\alpha}$$

$$= \frac{600\text{ N}}{\cos 15°}$$

$$= 621.17\text{ N}$$

$P = 621$ N ◀

(*b*)

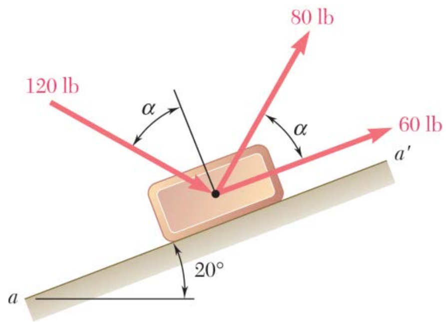
$$\tan\alpha = \frac{P_y}{P_x}$$

$$P_y = P_x \tan\alpha$$

$$= (600\text{ N})\tan 15°$$

$$= 160.770\text{ N}$$

$P_y = 160.8$ N ◀



PROBLEM 2.107

Knowing that $\alpha = 40°$, determine the resultant of the three forces shown.

SOLUTION

60-lb Force:

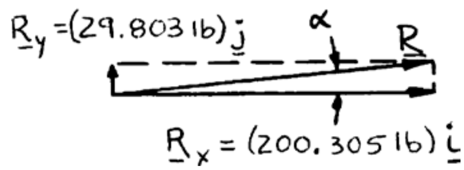
$$F_x = (60 \text{ lb})\cos 20° = 56.382 \text{ lb}$$
$$F_y = (60 \text{ lb})\sin 20° = 20.521 \text{ lb}$$

80-lb Force:

$$F_x = (80 \text{ lb})\cos 60° = 40.000 \text{ lb}$$
$$F_y = (80 \text{ lb})\sin 60° = 69.282 \text{ lb}$$

120-lb Force:

$$F_x = (120 \text{ lb})\cos 30° = 103.923 \text{ lb}$$
$$F_y = -(120 \text{ lb})\sin 30° = -60.000 \text{ lb}$$



and

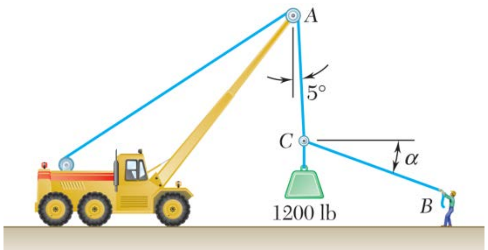
$$R_x = \Sigma F_x = 200.305 \text{ lb}$$
$$R_y = \Sigma F_y = 29.803 \text{ lb}$$
$$R = \sqrt{(200.305 \text{ lb})^2 + (29.803 \text{ lb})^2}$$
$$= 202.510 \text{ lb}$$

Further:

$$\tan\alpha = \frac{29.803}{200.305}$$

$$\alpha = \tan^{-1}\frac{29.803}{200.305}$$
$$= 8.46°$$

$\mathbf{R} = 203 \text{ lb} \measuredangle\ 8.46°$ ◀

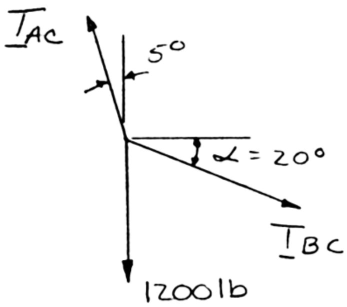


PROBLEM 2.108

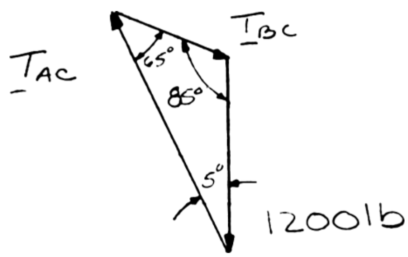
Knowing that $\alpha = 20°$, determine the tension (*a*) in cable *AC*, (*b*) in rope *BC*.

SOLUTION

Free-Body Diagram



Force Triangle



Law of sines:

$$\frac{T_{AC}}{\sin 110°} = \frac{T_{BC}}{\sin 5°} = \frac{1200\text{ lb}}{\sin 65°}$$

(*a*)

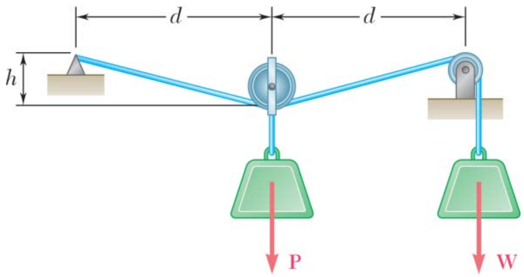
$$T_{AC} = \frac{1200\text{ lb}}{\sin 65°}\sin 110°$$

$T_{AC} = 1244$ lb ◀

(*b*)

$$T_{BC} = \frac{1200\text{ lb}}{\sin 65°}\sin 5°$$

$T_{BC} = 115.4$ lb ◀

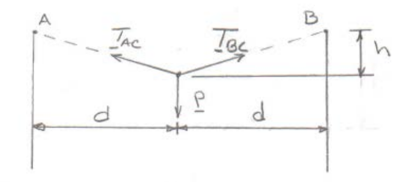


PROBLEM 2.109

For $W = 800$ N, $P = 200$ N, and $d = 600$ mm, determine the value of h consistent with equilibrium.

SOLUTION

Free-Body Diagram



$$T_{AC} = T_{BC} = 800 \text{ N}$$

$$AC = BC = \sqrt{\left(h^2 + d^2\right)}$$

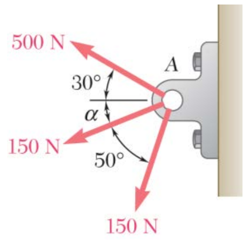
$$\Sigma F_y = 0: \quad 2(800 \text{ N})\frac{h}{\sqrt{h^2 + d^2}} - P = 0$$

$$800 = \frac{P}{2}\sqrt{1 + \left(\frac{d}{h}\right)^2}$$

Data: $P = 200$ N, $d = 600$ mm and solving for h

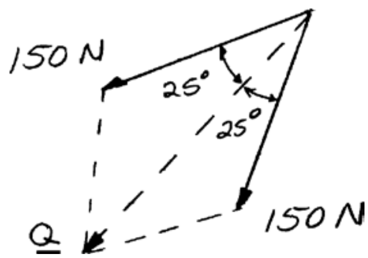
$$800 \text{ N} = \frac{200 \text{ N}}{2}\sqrt{1 + \left(\frac{600 \text{ mm}}{h}\right)^2}$$

$$h = 75.6 \text{ mm} \blacktriangleleft$$

	**PROBLEM 2.110** Three forces are applied to a bracket as shown. The directions of the two 150-N forces may vary, but the angle between these forces is always 50°. Determine the range of values of α for which the magnitude of the resultant of the forces acting at A is less than 600 N.

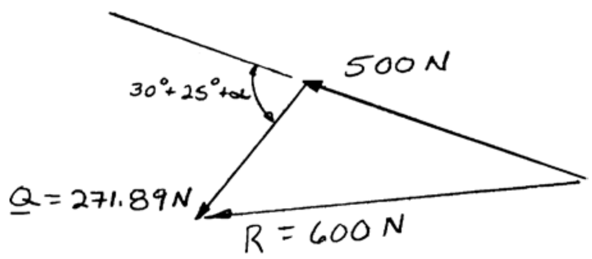
SOLUTION

Combine the two 150-N forces into a resultant force Q:



$$Q = 2(150 \text{ N})\cos 25°$$
$$= 271.89 \text{ N}$$

Equivalent loading at A:



Using the law of cosines:

$$(600 \text{ N})^2 = (500 \text{ N})^2 + (271.89 \text{ N})^2 + 2(500 \text{ N})(271.89 \text{ N})\cos(55° + \alpha)$$
$$\cos(55° + \alpha) = 0.132685$$

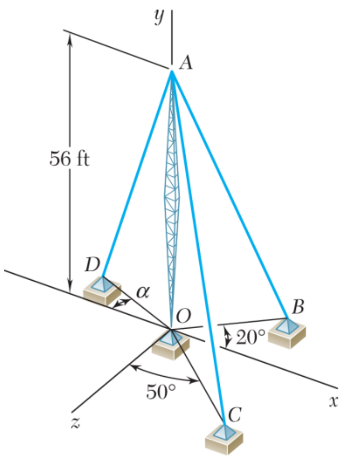
Two values for α: $\quad 55° + \alpha = 82.375$

$$\alpha = 27.4°$$

or

$$55° + \alpha = -82.375°$$
$$55° + \alpha = 360° - 82.375°$$
$$\alpha = 222.6°$$

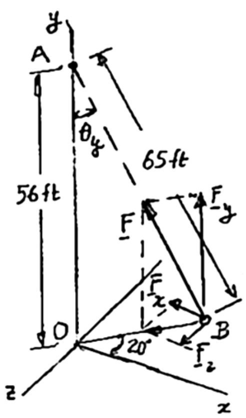
For $R < 600$ lb: $\quad 27.4° < \alpha < 222.6°$ ◀



PROBLEM 2.111

Cable *AB* is 65 ft long, and the tension in that cable is 3900 lb. Determine (*a*) the *x*, *y*, and *z* components of the force exerted by the cable on the anchor *B*, (*b*) the angles θ_x, θ_y, and θ_z defining the direction of that force.

SOLUTION



From triangle *AOB*:

$$\cos\theta_y = \frac{56 \text{ ft}}{65 \text{ ft}} = 0.86154$$

$$\theta_y = 30.51°$$

(*a*)

$$F_x = -F \sin\theta_y \cos 20° = -(3900 \text{ lb}) \sin 30.51° \cos 20°$$

$$F_x = -1861 \text{ lb} \blacktriangleleft$$

$$F_y = +F\cos\theta_y = (3900 \text{ lb})(0.86154) \qquad F_y = +3360 \text{ lb} \blacktriangleleft$$

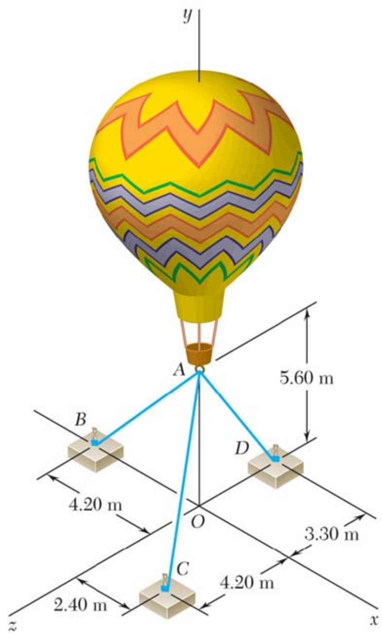
$$F_z = +(3900 \text{ lb}) \sin 30.51° \sin 20° \qquad F_z = +677 \text{ lb} \blacktriangleleft$$

(*b*)

$$\cos\theta_x = \frac{F_x}{F} = -\frac{1861 \text{ lb}}{3900 \text{ lb}} = -0.4771 \qquad \theta_x = 118.5° \blacktriangleleft$$

From above: $\theta_y = 30.51°$ $\qquad \theta_y = 30.5° \blacktriangleleft$

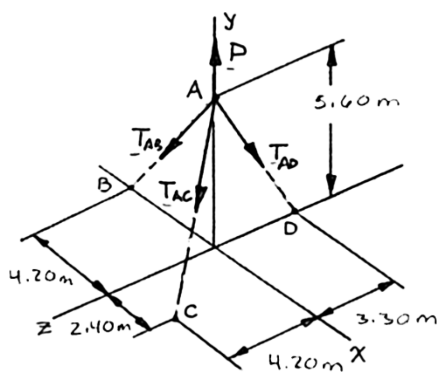
$$\cos\theta_z = \frac{F_z}{F} = +\frac{677 \text{ lb}}{3900 \text{ lb}} = +0.1736 \qquad \theta_z = 80.0° \blacktriangleleft$$



PROBLEM 2.112

Three cables are used to tether a balloon as shown. Determine the vertical force **P** exerted by the balloon at *A* knowing that the tension in cable *AB* is 259 N.

SOLUTION



The forces applied at *A* are: $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD}$, and $\mathbf{P}$

where $\mathbf{P} = P\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{AB} = -(4.20\text{ m})\mathbf{i} - (5.60\text{ m})\mathbf{j} \qquad AB = 7.00\text{ m}$$
$$\overrightarrow{AC} = (2.40\text{ m})\mathbf{i} - (5.60\text{ m})\mathbf{j} + (4.20\text{ m})\mathbf{k} \qquad AC = 7.40\text{ m}$$
$$\overrightarrow{AD} = -(5.60\text{ m})\mathbf{j} - (3.30\text{ m})\mathbf{k} \qquad AD = 6.50\text{ m}$$

and

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (-0.6\mathbf{i} - 0.8\mathbf{j})T_{AB}$$
$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (0.32432 - 0.75676\mathbf{j} + 0.56757\mathbf{k})T_{AC}$$
$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = (-0.86154\mathbf{j} - 0.50769\mathbf{k})T_{AD}$$

SOLUTION Continued

Equilibrium condition $\Sigma F = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$ and factoring **i**, **j**, and **k**:

$$(-0.6T_{AB} + 0.32432T_{AC})\mathbf{i} + (-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P)\mathbf{j}$$
$$+ (0.56757T_{AC} - 0.50769T_{AD})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$-0.6T_{AB} + 0.32432T_{AC} = 0 \quad (1)$$

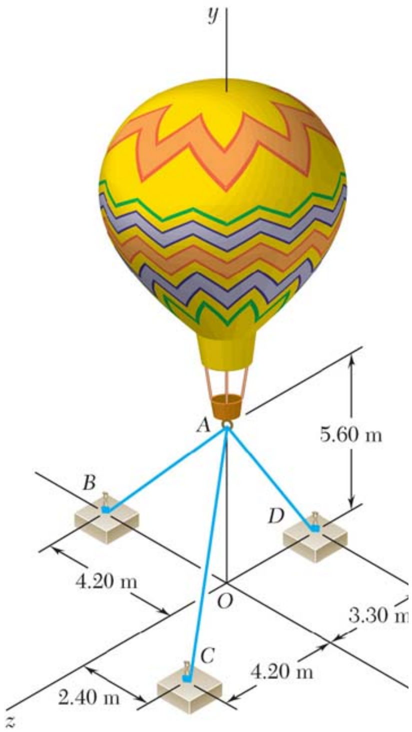
$$-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0 \quad (2)$$

$$0.56757T_{AC} - 0.50769T_{AD} = 0 \quad (3)$$

Setting $T_{AB} = 259\text{ N}$ in (1) and (2), and solving the resulting set of equations gives

$$T_{AC} = 479.15\text{ N}$$
$$T_{AD} = 535.66\text{ N}$$

$\mathbf{P} = 1031\text{ N} \uparrow$ ◀



PROBLEM 2.113

Three cables are used to tether a balloon as shown. Determine the vertical force **P** exerted by the balloon at *A* knowing that the tension in cable *AC* is 444 N.

SOLUTION

See Problem 2.112 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-0.6T_{AB} + 0.32432T_{AC} = 0 \quad (1)$$

$$-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0 \quad (2)$$

$$0.56757T_{AC} - 0.50769T_{AD} = 0 \quad (3)$$

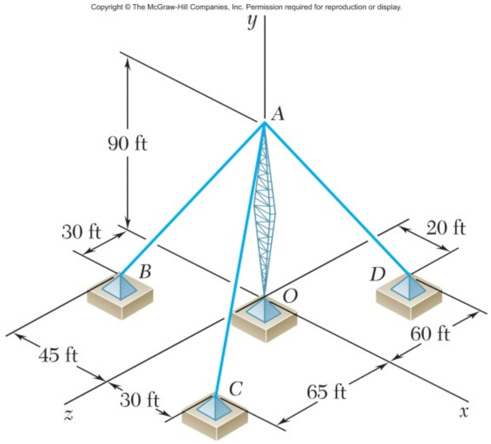
Substituting $T_{AC} = 444\text{ N}$ in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms gives

$$T_{AB} = 240\text{ N}$$

$$T_{AD} = 496.36\text{ N}$$

$\mathbf{P} = 956\text{ N}\uparrow$ ◀

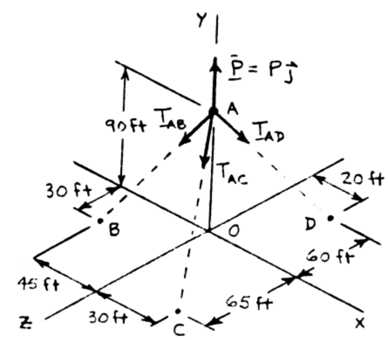
PROBLEM 2.114



A transmission tower is held by three guy wires attached to a pin at A and anchored by bolts at B, C, and D. If the tension in wire AB is 630 lb, determine the vertical force $\mathbf{P}$ exerted by the tower on the pin at A.

SOLUTION

Free Body A:



$$\Sigma \mathbf{F} = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$$

$$\overrightarrow{AB} = -45\mathbf{i} - 90\mathbf{j} + 30\mathbf{k} \qquad AB = 105 \text{ ft}$$

$$\overrightarrow{AC} = 30\mathbf{i} - 90\mathbf{j} + 65\mathbf{k} \qquad AC = 115 \text{ ft}$$

$$\overrightarrow{AD} = 20\mathbf{i} - 90\mathbf{j} - 60\mathbf{k} \qquad AD = 110 \text{ ft}$$

We write

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$

$$= \left(-\frac{3}{7}\mathbf{i} - \frac{6}{7}\mathbf{j} + \frac{2}{7}\mathbf{k}\right)T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC}$$

$$= \left(\frac{6}{23}\mathbf{i} - \frac{18}{23}\mathbf{j} + \frac{13}{23}\mathbf{k}\right)T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD}$$

$$= \left(\frac{2}{11}\mathbf{i} - \frac{9}{11}\mathbf{j} - \frac{6}{11}\mathbf{k}\right)T_{AD}$$

Substituting into the Eq. $\Sigma \mathbf{F} = 0$ and factoring $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$:

$$\left(-\frac{3}{7}T_{AB} + \frac{6}{23}T_{AC} + \frac{2}{11}T_{AD}\right)\mathbf{i}$$

$$+\left(-\frac{6}{7}T_{AB} - \frac{18}{23}T_{AC} - \frac{9}{11}T_{AD} + P\right)\mathbf{j}$$

$$+\left(\frac{2}{7}T_{AB} + \frac{13}{23}T_{AC} - \frac{6}{11}T_{AD}\right)\mathbf{k} = 0$$

PROBLEM 2.114 (Continued)

Setting the coefficients of $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$, equal to zero:

$$\mathbf{i}: \quad -\frac{3}{7}T_{AB} + \frac{6}{23}T_{AC} + \frac{2}{11}T_{AD} = 0 \tag{1}$$

$$\mathbf{j}: \quad -\frac{6}{7}T_{AB} - \frac{18}{23}T_{AC} - \frac{9}{11}T_{AD} + P = 0 \tag{2}$$

$$\mathbf{k}: \quad \frac{2}{7}T_{AB} + \frac{13}{23}T_{AC} - \frac{6}{11}T_{AD} = 0 \tag{3}$$

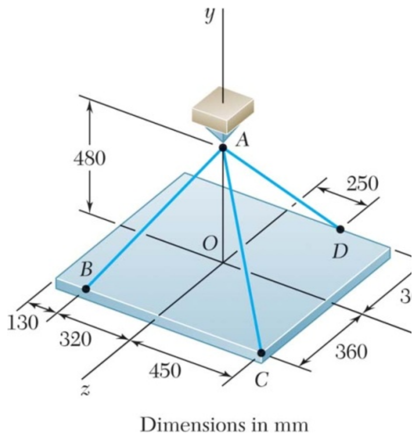
Set $T_{AB} = 630$ lb in Eqs. (1) – (3):

$$-270 \text{ lb} + \frac{6}{23}T_{AC} + \frac{2}{11}T_{AD} = 0 \tag{1$'$}$$

$$-540 \text{ lb} - \frac{18}{23}T_{AC} - \frac{9}{11}T_{AD} + P = 0 \tag{2$'$}$$

$$180 \text{ lb} + \frac{13}{23}T_{AC} - \frac{6}{11}T_{AD} = 0 \tag{3$'$}$$

Solving, $T_{AC} = 467.42$ lb $\quad T_{AD} = 814.35$ lb $\quad P = 1572.10$ lb $\qquad P = 1572$ lb ◀



PROBLEM 2.115

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable *AD* is 520 N, determine the weight of the plate.

SOLUTION

See Problem 2.114 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0 \tag{1}$$

$$-\frac{12}{17}T_{AB} + 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P = 0 \tag{2}$$

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0 \tag{3}$$

Making $T_{AD} = 520 \text{ N}$ in Eqs. (1) and (3):

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + 200 \text{ N} = 0 \tag{1$'$}$$

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - 288 \text{ N} = 0 \tag{3$'$}$$

Multiply (1′) by 9, (3′) by 8, and add:

$$9.24T_{AC} - 504 \text{ N} = 0 \quad T_{AC} = 54.5455 \text{ N}$$

Substitute into (1′) and solve for T_{AB}:

$$T_{AB} = \frac{17}{8}(0.6 \times 54.5455 + 200) \quad T_{AB} = 494.545 \text{ N}$$

Substitute for the tensions in Eq. (2) and solve for *P*:

$$P = \frac{12}{17}(494.545 \text{ N}) + 0.64(54.5455 \text{ N}) + \frac{9.6}{13}(520 \text{ N})$$

$$= 768.00 \text{ N}$$

Weight of plate $= P = 768 \text{ N}$ ◀