## Chapter 2

2.1 Nominal: Occupation, undergraduate major. Ordinal: Rating of university professor, Taste test ratings. Interval:age, income
2.2 a Interval
b Interval
c Nominal
d Ordinal
2.3 a Interval
b Nominal
c Ordinal
d Interval
e Interval
2.4 a Nominal
b Interval
c Nominal
d Interval
e Ordinal
2.5 a Interval
b Interval
c Nominal
d Interval
e Nominal
2.6 a Interval
b Interval
c Nominal
d Ordinal
e Interval
2.7 a Interval
b Nominal
c. Nominal
d Interval
e Interval
f Ordinal
2.8 a Interval
b Ordinal
c Nominal
d Ordinal
2.9 a Interval
b Nominal
c Nominal
2.10 a Ordinal
b Ordinal
c Ordinal
2.11 a Nominal
b Interval
c Ordinal
2.12a Nominal
b Interval
c Interval
d Interval
2.13

2.14

2.15

2.16


2.18

2.19

2.20


2.22

2.23


2.25



2.27



The basement is the top choice followed by kitchen, bathroom, bedroom, and living/dining room.

| 2.29 a | Newspaper | Frequency | Relative Frequency |
| ---: | :--- | :---: | :---: |
|  | Daily News | 141 | $39.2 \%$ |
|  | Post | 128 | $35.6 \%$ |
|  | Times | 32 | $8.9 \%$ |
|  | WSJ | 59 | $16.4 \%$ |

b


The Daily News and the Post dominate the market

2.30a

Degree Frequency

| BA | 88 |
| :--- | :--- |
| BBA | 37 |

B Eng 51

B Sc 24

Other 30
b.

c

d. About 4 applicants in 10 have the BA degree, about one-fifth have a BEng. and one-sixth have a BBA.

b

c Dell is most popular with $40 \%$ proportion, followed by other, $26 \%, \mathrm{HP}, 21 \%$ and Lenovo, $13 \%$.
2.32 a Software Frequency

Excel 34
Minitab 17
SAS 3
SPSS 4
Other 12
b

c Excel is the choice of about half the sample, one-quarter have opted for Minitab, and a small fraction chose SAS and SPSS.
2.33

2.34

2.35

2.36 a

b


According to the survey Republicans favor the rich and Democrats are split among the middle class, poor, and rich.
2.37 a

| Category | Frequency | Relative Frequency |
| :--- | :--- | :--- |
| Mom: Full time, Dad: Full time | 403 | $46.0 \%$ |
| Mom: Part time, Dad: Full time | 149 | $17.0 \%$ |
| Mom: Not employed, Dad: Full time | 228 | $26.0 \%$ |
| Mom: Full time, Dad: Part time or not employed | 53 | $6.0 \%$ |
| Mom: Not employed, Dad: Not employed | 18 | $2.1 \%$ |
| Other | 26 | $3.0 \%$ |

b

c

d In most households Dad is working full time. There are very few households where neither Mom nor Dad are working.
2.38


A small majority oppose the Affordable Care Act.
2.39a

| Views on social issues | Frequency | Relative Frequency |
| :--- | :--- | :--- |
| Liberal | 322 | $31.4 \%$ |
| Moderate | 328 | $32.0 \%$ |
| Conservative | 375 | $36.6 \%$ |

b


The country is split among the three views on social issues with a small plurality of conservatives.
2.40 a

| Views on economic issues | Frequency | Relative Frequency |
| :--- | :--- | :--- |
| Liberal | 208 | $20.3 \%$ |
| Moderate | 354 | $34.5 \%$ |
| Conservative | 463 | $45.2 \%$ |

b


Economically the country is conservative.
2.41


There is decreasing numbers of Americans who did not finish high school and increasing numbers of those that go to college.
2.42


Spending is increasing in all seven areas.

### 2.43



In general crime was decreasing until 2014 when it started increasing.


Universities 1 and 2 are similar and quite dissimilar from universities 3 and 4, which also differ. The two nominal variables appear to be related.
2.45

| 3 | Count of Owner | Last [ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | Second-last - | Exxon | Amoco | Texaco | Other | Grand Total |
| 5 | Exxon | 39 | 36 | 51 | 23 | 149 |
| 6 | Amoco | 36 | 32 | 46 | 20 | 134 |
| 7 | Texaco | 54 | 46 | 65 | 29 | 194 |
| 8 | Other | 24 | 20 | 28 | 10 | 82 |
| 9 | Grand Total | 153 | 134 | 190 | 82 | 559 |


| 3 | Count of Owner | Last |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | ---: | ---: |
| 4 | Second-last | Exxon | Amoco | Texaco | Other | Grand Total |
| 5 | Exxon | $25 \%$ | $27 \%$ | $27 \%$ | $28 \%$ | $27 \%$ |
| 6 | Amoco | $24 \%$ | $24 \%$ | $24 \%$ | $24 \%$ | $24 \%$ |
| 7 | Texaco | $35 \%$ | $34 \%$ | $34 \%$ | $35 \%$ | $35 \%$ |
| 8 | Other | $16 \%$ | $15 \%$ | $15 \%$ | $12 \%$ | $15 \%$ |
| 9 | Grand Total | $100 \%$ | $100 \%$ | $100 \%$ | $100 \%$ | $100 \%$ |

The column proportions are similar; the two nominal variables appear to be unrelated. There does not appear to be any brand loyalty.

| 3 | Count of Respondent | Smoke? |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 4 | Parent | Smoke? | Do not smo | Grand Total |
| 5 | Neither | 73 | 14 | 87 |
| 6 | Father | 26 | 12 | 38 |
| 7 | Mother | 31 | 18 | 49 |
| 8 | Both | 10 | 41 | 51 |
| 9 | Grand Total | 140 | 85 | 225 |


| 3 | Count of Respondent | Smoke? | $\mid$ |  |  |
| ---: | :--- | :--- | :--- | :--- | :--- |
| 4 | Parent | Smoke? | Do not smoke | Grand Total |  |
| 5 | Neither | $52 \%$ | $16 \%$ | $39 \%$ |  |
| 6 | Father | $19 \%$ | $14 \%$ | $17 \%$ |  |
| 7 | Mother | $22 \%$ | $21 \%$ | $22 \%$ |  |
| 8 | Both | $7 \%$ | $48 \%$ | $23 \%$ |  |
| 9 | Grand Total | $100 \%$ | $100 \%$ | $100 \%$ |  |

The two variables are related.
2.47


There are large differences between men and women in terms of the reason for unemployment.


The number of prescriptions filled by all stores except independent drug stores has increased substantially.
2.49


There appears to be differences between female and male students in their choice of light beer.


There are differences among the five groups.
2.51


All three groups say that upper-income people pay too little. However Conservatives are more likely to say fair share than Moderates or Liberals
2.52


Democrats support and Republicans oppose the Affordable Care Act.
2.53


No surprise-on social issues Democrats are liberal and Republicans are conservative.


On economic issues Republicans are very conservative whereas Democrats and Moderates are mixed.

### 2.55



2.57

2.58


The pattern is about the same for the three households.
2.59



There are decreases in almost every state. However, there are many Americans without health insurance.
2.61


More students disagree than agree.


More than $40 \%$ rate the food as less than good.
2.63



Customers with children rated the restaurant more highly than did customers with no children.
2.65


Males and females differ in their areas of employment. Females tend to choose accounting marketing/sales and males opt for finance.
b


Area and job satisfaction are related. Graduates who work in finance and general management appear to be more satisfied than those in accounting, marketing/sales, and others.
2.66


The survey oversampled women slightly.

2.68a

| Married | 1158 |
| :--- | ---: |
| Widowed | 209 |
| Divorced | 411 |
| Separated | 81 |
| Never married | 675 |

b. Pie chart
c.

2.69

2.70


The patterns are similar.

2.72


The patterns are similar.


Males are slightly more likely to be self-employed than females.
2.74


The "married" categories (4 and 5) make up more than $60 \%$ of the households.
2.75


There are large differences between male and female heads of households.
2.76


Whites make up three quarters of the survey.


There are large differences between the four races in terms of family structure.
2.78


College degree holders are much more likely to own their homes.


## Chapter Two

## Graphical Descriptive Techniques 1

- Types of Data and Information
- Describing a Set of Nominal Data
- Describing the Relationship between Two Nominal Variables and Comparing Two or More Nominal Data Sets


## Types of Data \& Information

Definitions

A variable is some characteristic of a population or sample.
E.g. student grades.

Typically denoted with a capital letter: X, Y, Z...

The values of the variable are the range of possible values for a variable.
E.g. student marks (0..100)

Data are the observed values of a variable.
E.g. student marks: $\{67,74,71,83,93,55,48\}$

## Types of Data \& Information

Hierarchy of Data
Data (at least for purposes of Statistics) fall into three main groups:

Interval Data
Nominal Data
Ordinal Data
The data types can be placed in order of the permissible calculations. At the top of the list, we place the interval data type because virtually all computations are allowed. The nominal data type is at the bottom because no calculations other than determining frequencies are permitted.

## Types of Data \& Information

Interval data

- Real numbers, i.e. heights, weights, prices, etc.
- Also referred to as quantitative or numerical.

Arithmetic operations can be performed on Interval Data, thus its meaningful to talk about 2*Height, or Price + \$1, and so on.

## Types of Data \& Information

## Nominal Data

- The values of nominal data are categories.
E.g. responses to questions about marital status, coded as:

Single $=1$, Married $=2$, Divorced $=3$, Widowed $=4$

These data are categorical in nature; arithmetic operations don't make any sense (e.g. does Widowed $\div 2=$ Married?!)

Nominal data are also called qualitative or categorical.

## Types of Data \& Information

Ordinal Data appear to be categorical in nature, but their values have an order; a ranking to them:
E.g. College course rating system:
poor $=1$, fair $=2$, good $=3$, very good $=4$, excellent $=5$
While its still not meaningful to do arithmetic on this data (e.g. does $2^{*}$ fair $=$ very good?! $)$, we can say things like:

```
excellent > poor or fair < very good
```

That is, order is maintained no matter what numeric values are assigned to each category.

## Types of Data \& Information

As mentioned above,

- All calculations are permitted on interval data.
- Only calculations involving a ranking process are allowed for ordinal data.
- No calculations are allowed for nominal data, save counting the number of observations in each category.

This lends itself to the following "hierarchy of data"...

## Types of Data \& Information

## Interval

Values are real numbers.
All calculations are valid.
Data may be treated as ordinal or nominal.

## Ordinal

Values must represent the ranked order of the data.
Calculations based on an ordering process are valid.
Data may be treated as nominal but not as interval.

## Nominal

Values are the arbitrary numbers that represent categories.
Only calculations based on the frequencies of occurrence are valid.
Data may not be treated as ordinal or interval.

## Describing a Set of Nominal Data

Graphical \& Tabular Techniques for Nominal Data...
The only allowable calculation on nominal data is to count the frequency of each value of the variable.

We can summarize the data in a table that presents the categories and their counts called a frequency distribution.

A relative frequency distribution lists the categories and the proportion with which each occurs.

## Example 2.1 Work Status in the GSS 2012 Survey

### 1.11

[GSS2012*] In Chapter 1 we briefly introduced the General Social Survey.
In the 2012 survey respondents were asked the following question.
Last week were you working full time, part time, going to school, keeping house, or what? The responses were

1. Working full time
2. Working part time
3. Temporarily not working
4. Unemployed, Iaid off
5. Retired
6. School
7. Keeping house
8. Other

The responses were recorded using the codes $1,2,3,4,5,6,7$, and 8 , respectively.

## Describing a Set of Nominal Data

Frequency and Relative Frequency Distributions

| Work Status | Code | Frequency | Relative Frequency (\%) |
| :--- | :---: | :---: | :---: |
| Working full-time | 1 | 912 | 46.2 |
| Working part-time | 2 | 226 | 11.5 |
| Temporarily not working | 3 | 40 | 2.0 |
| Unemployed, laid off | 4 | 104 | 5.3 |
| Retired | 5 | 357 | 18.1 |
| School | 6 | 70 | 3.5 |
| Keeping house | 7 | 210 | 10.6 |
| Other | 8 | 54 | 2.7 |

## Describing a Set of Nominal Data

Nominal Data (Frequency)

Bar Chart



Bar Charts are often used to display frequencies...

## Describing a Set of Nominal Data

Nominal Data (Relative Frequency)

Pie Chart


Pie Charts show relative frequencies...

## Describing a Set of Nominal Data

## Bar Chart



It is all the same information, (based on the same data). Just different presentation.

Pie Chart


Describing the Relationship between
Two Nominal Variables

To describe the relationship between two nominal variables, we must remember that we are permitted only to determine the frequency of the values. As a first step we need to produce a cross-classification table, which lists the frequency of each combination of the values of the two variables

## Example 2.4 Newspaper Readership Survey

In a major North American city there are four competing newspapers: the Globe and Mail (G\&M), Post, Sun, and Star. To help design advertising campaigns, the advertising managers of the newspapers need to know which segments of the newspaper market are reading their papers. A survey was conducted to analyze the relationship between newspapers read and occupation. A sample of newspaper readers was asked to report which newspaper they read: Globe and Mail (1) Post (2), Star (3), Sun (4), and to indicate whether they were blue-collar worker (1), white-collar worker (2), or professional (3). The responses are stored in Xm02-04 using the codes. Some of the data are listed here.

## Example 2.4

Reader Occupation Newspaper

| 1 | 2 | 2 |
| :--- | :--- | :--- |
| 2 | 1 | 4 |
| 3 | 2 | 1 |
| $\cdot$ | $\cdot$ | $\cdot$ |
| $\cdots$ | $\cdot$ | $\cdot$ |
| 352 | 3 | 2 |
| 353 | 1 | 3 |
| 354 | 2 | 3 |

Determine whether the two nominal variables are related.

## Describing the Relationship between Two Nominal Variables

Cross-Classification Table of Frequencies

Newspaper
Occupation G\&M Post Star Sun Total $\begin{array}{llllll}\text { Blue collar } & 27 & 18 & 38 & 37 & 120\end{array}$
$\begin{array}{lllllll}\text { White collar } & 29 & 43 & 21 & 15 & 108\end{array}$

| Professional | 33 | 51 | 22 | 20 | 126 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Total | 89 | 112 | 81 | 72 | 354 |

## Describing the Relationship between Two Nominal Variables

Row Relative Frequencies

Newspaper

| Occupation | G\&M | Post | Star | Sun | Total |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Blue collar | .23 | .15 | .32 | .31 | 1.00 |
| White collar | .27 | .40 | .19 | .14 | 1.00 |
| Professional | .26 | .40 | .17 | .16 | 1.00 |
| Total | .25 | .32 | .23 | .20 | 1.00 |

## Graphing the Relationship between 2 Nominal Variables



The shapes of the bar charts for White-collar and Professional are very similar, but both differ considerably from
Blue collar.

## Graphing the Relationship between 2 Nominal Variables

## INTERPRET

If the two variables are unrelated, the patterns exhibited in the bar charts should be approximately the same. If some relationship exists, then some bar charts will differ from others.

The graphs tell us the same story as did the table. The shapes of the bar charts for occupations 2 and 3 (White-collar and Professional) are very similar. Both differ considerably from the bar chart for occupation 1 (Blue-collar).

