### **Multiple Choice**

Identify the choice that best completes the statement or answers the question.

1. Find the complement and supplement of the angle 55°.

a. Complement: 45° Supplement: 145°

b. Complement: 125° Supplement: 35°

c. Complement: 145° Supplement: 235°

d. Complement: 125° Supplement: 305°

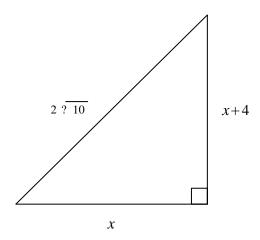
e. Complement: 35° Supplement: 125°

2. Let triangle ABC be a right triangle with  $C = 90^{\circ}$ . If c = 19 and a = 6, find b.

d.  $5\sqrt{13}$ 

e. None of the above.

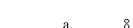
3. Solve for *x* in the following right triangle:



3

b. 2

d. 4



4. Find the lengths of the shortest two sides of a  $30^{\circ} - 60^{\circ} - 90^{\circ}$  triangle, if the length of the longest side is 16.

a. 
$$4, \frac{8}{\sqrt{3}}$$

d. 
$$4, \frac{4}{\sqrt{3}}$$

b. 
$$4, 4\sqrt{3}$$

e. 
$$8, \frac{\sqrt{3}}{\sqrt{3}}$$

c. 
$$8, 8\sqrt{3}$$

5. Find the length of the shorter sides of a  $45^{\circ} - 45^{\circ} - 90^{\circ}$  triangle if the length of the hypotenuse is 21.

a. 
$$\frac{21\sqrt{2}}{2}$$

d. 
$$\frac{21\sqrt{3}}{3}$$

b. 
$$\frac{21\sqrt{2}}{4}$$

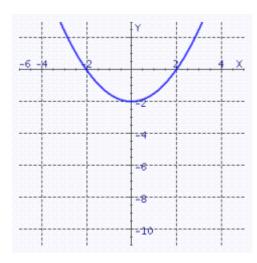
e. 
$$\frac{21\sqrt{3}}{2}$$

c. 
$$\frac{21}{2}$$

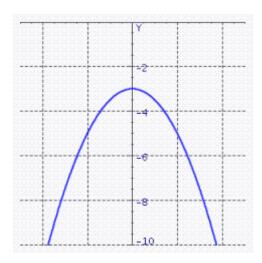
\_\_\_\_ 6. Graph the following parabola.

$$f(x) = -\frac{1}{2}x^2 - 2$$

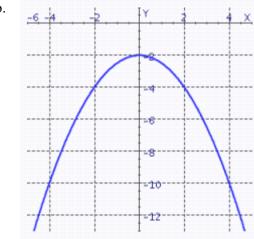
a.



d.

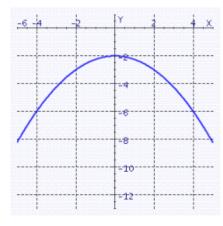


b.



e. None of the above.

c.



 7.	Find the distance between the two points $(-5, 8)$ and $(19, 53)$ .

- a. 102
  - b. 51
  - c. 48
  - d. 153
  - e. 99

- 8. Determine two coterminal angles (one positive and one negative) for  $\theta = -503^{\circ}$ .
  - a. 127°, 233°
  - b. 307°, -413°
  - c. 127°, 323°
  - d. 217°, 143°
  - e. 217°, 323°

- 9. Determine which of the following points is located in quadrant 4.
  - a. (-3, 7)

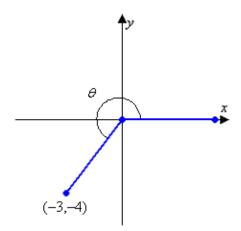
d. (-7, -3)

b. (3, -7)

e. (7, 3)

- c. (-7, 3)
- \_\_\_\_
  - 10. Which of the following points lies on the unit circle?
    - a.  $\left(\frac{-7}{11}, \frac{4\sqrt{2}}{11}\right)$
    - b.  $\left(\frac{5}{9}, \frac{-4\sqrt{2}}{9}\right)$
    - c.  $\left(\frac{-7}{9}, \frac{-4\sqrt{2}}{9}\right)$
    - d.  $\left(\frac{-5}{13}, \frac{-4\sqrt{2}}{13}\right)$
    - e. None of the above.

- \_\_\_\_ 11. Given  $\sin 30^\circ = \frac{1}{2}$  and  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ , determine the following:
  - csc 30°
  - a.  $\csc 30^{\circ} = \frac{\sqrt{3}}{3}$
  - b.  $\csc 30^{\circ} = \frac{\sqrt{2}}{2}$
  - c.  $csc 30^{\circ} = \sqrt{3}$
  - d.  $csc 30^{\circ} = 2$
  - e. undefined
  - 12. Given the figure below, determine the value of  $\sin \theta$ .



- a.  $\sin \theta = -\frac{3}{5}$
- b.  $\sin \theta = \frac{4}{3}$
- c.  $\sin \theta = -\frac{4}{5}$
- d.  $\sin \theta = -\frac{3}{4}$
- e.  $\sin \theta = \frac{3}{4}$

- 13. The point (3,4) is on the terminal side of an angle in standard position. Determine the exact value of
  - a.  $\cos \theta = -\frac{5}{3}$

  - b.  $\cos \theta = \frac{4}{3}$ c.  $\cos \theta = \frac{3}{4}$ d.  $\cos \theta = -\frac{4}{3}$
  - e.  $\cos \theta = \frac{3}{5}$
- 14. Indicate the two quadrants  $\theta$  could terminate in if  $\tan \theta = -\frac{13}{23}$ .
  - a. Quadrants II and III
  - b. Quadrants I and III
  - c. Quadrants I and IV

- d. Quadrants II and IV
- e. Quadrants III and IV

- \_\_\_\_ 15. Evaluate sin 300°.

- d.  $\frac{-\sqrt{2}}{2}$

- \_\_\_\_ 16. Find  $\sin \theta$  if  $\csc \theta = \frac{-23}{19}$ .

\_\_\_\_\_ 17. Find 
$$\tan \theta$$
 if  $\sec \theta = \frac{\sqrt{170}}{7}$  and  $\csc \theta = \frac{\sqrt{170}}{11}$ .

b.  $\frac{170}{77}$  c.  $\frac{7}{11}$ 

- \_\_\_\_ 18. If  $\sin \theta = \frac{-6}{\sqrt{85}}$  and  $\theta$  terminates in QIII, find  $\cos \theta$ .

d.  $\frac{-\sqrt{85}}{49}$  e.  $\frac{6}{7}$ 

b.  $\frac{-7}{\sqrt{85}}$  c.  $\frac{7}{\sqrt{85}}$ 

\_\_\_\_ 19. Suppose  $\csc \theta = 7$  and  $\theta$  terminates in QII. Find the remaining trigonometric ratios of  $\theta$ .

a. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{4\sqrt{3}}{7}$$

$$\tan\theta = \frac{1}{4\sqrt{3}}$$

$$\sec \theta = \frac{7}{4\sqrt{3}}$$

$$\cot \theta = 4\sqrt{3}$$

b. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{-4\sqrt{3}}{7}$$

$$\tan \theta = -4\sqrt{3}$$

$$\sec\theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = \frac{-1}{4\sqrt{3}}$$

$$\sin \theta = \frac{-4\sqrt{3}}{7}$$

$$\cos \theta = \frac{1}{7}$$

$$\tan \theta = \frac{-1}{4\sqrt{3}}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = -4\sqrt{3}$$

d. 
$$\sin \theta = \frac{-4\sqrt{3}}{7}$$

$$\cos \theta = \frac{1}{7}$$

$$\tan \theta = -4\sqrt{3}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = \frac{-1}{4\sqrt{3}}$$

e. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{-4\sqrt{3}}{7}$$

$$\tan \theta = \frac{-1}{4\sqrt{3}}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = -4\sqrt{3}$$

20. If  $\csc \theta = -11$ , find  $\csc^3 \theta$ .

e. -1,331

b. 
$$\frac{-1}{22}$$



21. Use fundamental identities to simplify the expression below and then determine which of the following is *not* equivalent.

$$\sin \alpha (\csc \alpha - \sin \alpha)$$

a. 
$$1 - \sin^2 \alpha$$

b. 
$$\frac{\csc^2 \alpha - 1}{\csc^2 \alpha}$$

c. 
$$\frac{\csc^2 \alpha - \sec^2 \alpha + \tan^2 \alpha}{\csc^2 \alpha}$$
d. 
$$1 - \cot^2 \alpha$$

d. 
$$1 - \cot^2 a$$

e. 
$$\cos^2 \alpha$$



22. Multiply; then use fundamental identities to simplify the expression below and determine which of the following is *not* equivalent.

$$(\sin x + \cos x)(\sin x - \cos x)$$

a. 
$$2\sin^2 x - \sec^2 x - \tan^2 x$$

b. 
$$\sin^2 x - \cos^2 x$$

c. 
$$1 - 2\cos^2 x$$

d. 
$$\csc^2 x - \cot^2 x - 2\cos^2 x$$

c. 
$$1 - 2\cos^2 x$$
d. 
$$\csc^2 x - \cot^2 x - 2\cos^2 x$$
e. 
$$1 - 2\sin\left(\frac{\pi}{2} - x\right)\cos x$$



23. Which of the following is equivalent to the given expression?

$$\frac{\sin^2 x}{1 - \cos x}$$

a. 
$$\tan x + \sin x$$

b. 
$$1 + \cos x$$

c. 
$$\csc x + \cot x$$

d. 
$$tan x cot x - cos x$$

e. 
$$\cot x \sin x + \tan x$$

24	Simplify the expression	$\sqrt{x^2+13}$	as much as possible after substituting	$\sqrt{13} \tan \theta$	for v
 <i>2</i> 4.	Simplify the expression	√1 × 1⊃	as much as possible after substituting	Δinamiα.	101 X.

a. 
$$\sqrt{13} |\csc \theta|$$
  
b.  $\sqrt{13} |\sin \theta|$   
c.  $\sqrt{13} |\sec \theta|$ 

b. 
$$\sqrt{13} |\sin \theta|$$

c. 
$$\sqrt{13}$$
 |sec  $\theta$ 

\_\_\_ 25. Simplify the expression  $\sqrt{30-6x^2}$  as much as possible after substituting  $\sqrt{5} \sin \theta$  for x.

b. 
$$\sqrt{30} |\csc \theta|$$
  
c.  $\sqrt{30} |\tan \theta|$ 

d. 
$$30 |\cos \theta|$$
  
e.  $\sqrt{30} |\cos \theta|$ 

c. 
$$\sqrt{30}$$
  $|tan \theta|$ 

### **Answer Section**

- 1. E
- 2. D
- 3. B
- 4. C
- 5. A
- 6. B
- 7. B
- 8. D
- 9. B
- 10. C
- 11. D
- 12. C
- 13. E
- 14. D
- 15. E
- 16. E
- 17. E
- 18. B
- 19. E
- 20. E
- 21. D
- 22. A
- 23. B
- 24. C
- 25. E

### **Multiple Choice**

Identify the choice that best completes the statement or answers the question.

1. Find the complement and supplement of the angle 59°.

a. Complement: 31° Supplement: 121°

b. Complement: 121°
Supplement: 31°

c. Complement: 41°
Supplement: 141°

d. Complement: 149° Supplement: 239°

e. Complement: 121° Supplement: 301°

2. Let triangle ABC be a right triangle with  $C = 90^{\circ}$ . If c = 19 and a = 10, find b.

a. 9

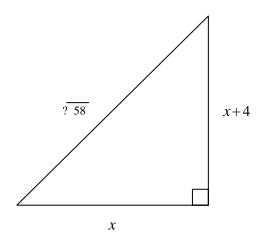
b. √9

c. <sub>3√√29</sub>

d.  $\sqrt{46}$ 

e. None of the above.

3. Solve for *x* in the following right triangle:



a. 6

b. 4

c. 2

d. 5

e. 3



a. 
$$6, 6\sqrt{3}$$

d. 
$$12, \frac{12}{\sqrt{3}}$$

b. 
$$6, \frac{6}{\sqrt{3}}$$

e. 
$$_{12}$$
,  $_{12}\sqrt{3}$ 

c. 
$$6, \frac{12}{\sqrt{3}}$$

5. Find the length of the shorter sides of a  $45^{\circ} - 45^{\circ} - 90^{\circ}$  triangle if the length of the hypotenuse is 17.

a. 
$$\frac{17\sqrt{2}}{4}$$

d. 
$$17\sqrt{3}$$

a. 
$$\frac{17\sqrt{2}}{4}$$
b.  $\frac{17\sqrt{2}}{2}$ 

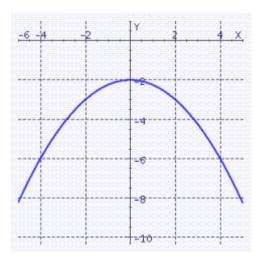
e. 
$$\frac{17}{2}$$

c. 
$$\frac{17\sqrt{3}}{2}$$

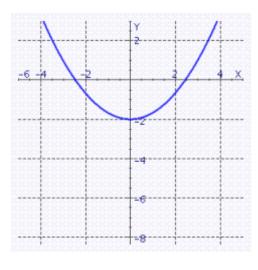
\_\_\_\_ 6. Graph the following parabola.

$$f(x) = -\frac{1}{3}x^2 - 2$$

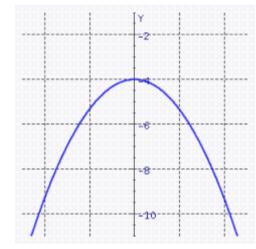
a.



d.

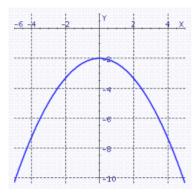


b.



e. None of the above.

c.



7
/.
 , .

- 7. Find the distance between the two points (-7, -5) and (5, 11).
  - a. 40
  - b. 20
  - c. 17
  - d. 60
  - e. 37



- 8. Determine two coterminal angles (one positive and one negative) for  $\theta = -506^{\circ}$ .
  - a. 124°, 236°
  - b. 304°, -416°
  - c. 124°, 326°
  - d. 214°, 146°
  - e. 214°, 326°



- 9. Determine which of the following points is located in quadrant 4.
  - a. (-6, -4)

d. (4, -6)

b. (-4, 6)

e. (-6, 4)

- c. (6, 4)
- - 10. Which of the following points lies on the unit circle?
    - a.  $\left(\frac{9}{13}, \frac{-2\sqrt{10}}{13}\right)$
    - b.  $\left(\frac{-7}{11}, \frac{2\sqrt{10}}{11}\right)$
    - c.  $\left(\frac{9}{11}, \frac{2\sqrt{10}}{11}\right)$
    - d.  $\left(\frac{7}{15}, \frac{2\sqrt{10}}{15}\right)$
    - e. None of the above.

\_\_\_\_ 11. Given  $\sin 30^\circ = \frac{1}{2}$  and  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ , determine the following:

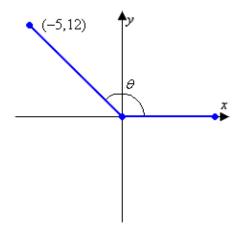
a. 
$$\tan 30^{\circ} = \sqrt{3}$$

b. 
$$\tan 30^{\circ} = 1$$

c. 
$$\tan 30^{\circ} = \frac{\sqrt{2}}{2}$$

d. 
$$\tan 30^{\circ} = \frac{\sqrt{3}}{3}$$

- e. undefined
- 12. Given the figure below, determine the value of  $\sin \theta$ .



a. 
$$\sin \theta = -\frac{5}{13}$$

b. 
$$\sin \theta = \frac{12}{5}$$

c. 
$$\sin \theta = \frac{12}{13}$$

a. 
$$\sin \theta = -\frac{5}{13}$$
  
b.  $\sin \theta = \frac{12}{5}$   
c.  $\sin \theta = \frac{12}{13}$   
d.  $\sin \theta = -\frac{5}{12}$ 

e. 
$$\sin \theta = \frac{5}{12}$$

- 13. The point (5, 12) is on the terminal side of an angle in standard position. Determine the exact value
  - a.  $\sec \theta = -\frac{5}{13}$

  - b.  $\sec \theta = \frac{5}{12}$ c.  $\sec \theta = \frac{12}{5}$ d.  $\sec \theta = -\frac{5}{12}$
  - e.  $\sec \theta = \frac{13}{5}$
- 14. Indicate the two quadrants  $\theta$  could terminate in if  $\tan \theta = -\frac{21}{31}$ .
  - a. Quadrants I and III
  - b. Quadrants II and III
  - c. Quadrants I and IV

- d. Quadrants II and IV
- e. Quadrants III and IV

- \_\_\_\_ 15. Evaluate sin 150°.

- \_\_\_\_ 16. Find  $\sin \theta$  if  $\csc \theta = \frac{-19}{17}$ .

\_\_\_\_ 17. Find 
$$\tan \theta$$
 if  $\sec \theta = \frac{\sqrt{218}}{7}$  and  $\csc \theta = \frac{\sqrt{218}}{13}$ .

a.  $\frac{218}{91}$ b.  $\frac{13}{7}$ c.  $\frac{7}{13}$ 

- \_\_\_\_ 18. If  $\sin \theta = \frac{-6}{\sqrt{85}}$  and  $\theta$  terminates in QIV, find  $\cos \theta$ .

\_\_\_\_ 19. Suppose  $\csc \theta = 15$  and  $\theta$  terminates in QII. Find the remaining trigonometric ratios of  $\theta$ .

a. 
$$\sin \theta = \frac{-4\sqrt{14}}{15}$$

$$\cos\theta = \frac{1}{15}$$

$$\tan \theta = \frac{-1}{4\sqrt{14}}$$

$$\sec \theta = \frac{-15}{4\sqrt{14}}$$

$$\cot \theta = -4\sqrt{14}$$

b. 
$$\sin \theta = \frac{1}{15}$$

$$\cos\theta = \frac{4\sqrt{14}}{15}$$

$$\tan\theta = \frac{1}{4\sqrt{14}}$$

$$\sec \theta = \frac{15}{4\sqrt{14}}$$

$$\cot \theta = 4\sqrt{14}$$

c. 
$$\sin \theta = \frac{1}{15}$$

$$\cos\theta = \frac{-4\sqrt{14}}{15}$$

$$\tan \theta = -4\sqrt{14}$$

$$\sec \theta = \frac{-15}{4\sqrt{14}}$$

$$\cot \theta = \frac{-1}{4\sqrt{14}}$$

d. 
$$\sin \theta = \frac{-4\sqrt{14}}{15}$$

$$\cos \theta = \frac{1}{15}$$

$$\tan \theta = -4\sqrt{14}$$

$$\sec \theta = \frac{-15}{4\sqrt{14}}$$

$$\cot \theta = \frac{-1}{4\sqrt{14}}$$

e. 
$$\sin \theta = \frac{1}{15}$$

$$\cos\theta = \frac{-4\sqrt{14}}{15}$$

$$\tan \theta = \frac{-1}{4\sqrt{14}}$$

$$\sec \theta = \frac{-15}{4\sqrt{14}}$$

$$\cot \theta = -4\sqrt{14}$$

\_\_\_\_ 20. If  $\csc \theta = -12$ , find  $\csc^3 \theta$ .

- a.  $\frac{-1}{36}$
- b.  $\frac{-1}{1,728}$
- c. -1.728

- d. -36
- e. 1,728

21. Use fundamental identities to simplify the expression below and then determine which of the following is *not* equivalent.

 $\sin \alpha (\csc \alpha - \sin \alpha)$ 

a. 
$$1 - \sin^2 \alpha$$

b. 
$$\frac{\csc^2 \alpha - 1}{\csc^2 \alpha}$$

c. 
$$\frac{\csc^2 \alpha - \sec^2 \alpha + \tan^2 \alpha}{\csc^2 \alpha}$$

d. 
$$1-\cot^2 \alpha$$

22. Multiply; then use fundamental identities to simplify the expression below and determine which of the following is *not* equivalent.

$$(\tan x + 1)^2$$

a. 
$$tan^2x + 1$$

b. 
$$\sec^2 x + 2\tan x$$

c. 
$$\frac{1 + 2\sin x \cos x}{\cos^2 x}$$

d. 
$$\tan^2 x + 2\tan x + 1$$

e. 
$$\sec^2 x (1 + 2\sin x \cos x)$$

23. Which of the following is equivalent to the given expression?

$$\frac{\sin^2 x}{1 - \cos x}$$

a. 
$$tan x + sin x$$

b. 
$$1 + \cos x$$

c. 
$$\csc x + \cot x$$

d. 
$$tan x cot x - cos x$$

e. 
$$\cot x \sin x + \tan x$$

24. Simplify the expression  $\sqrt{x^2 + 6}$  as much as possible after substituting  $\sqrt{6} \tan \theta$  for x.

b. 
$$\sqrt{6}$$
 |sec  $\theta$ 

a. 
$$6|\sec \theta|$$
  
b.  $\sqrt{6}|\sec \theta|$   
c.  $\sqrt{6}|\sin \theta|$ 

d. 
$$6|\csc\theta|$$
  
e.  $\sqrt{6}|\csc\theta|$ 

\_\_\_\_ 25. Simplify the expression  $\sqrt{70-7x^2}$  as much as possible after substituting  $\sqrt{10} \sin \theta$  for x.

a. 
$$\sqrt{70} |\tan \theta|$$

a. 
$$\sqrt{70} |\tan \theta|$$
  
b.  $\sqrt{70} |\cos \theta|$   
c.  $70 |\cos \theta|$ 

d. 
$$\sqrt{70} |\csc \theta|$$
  
e.  $70|\csc \theta|$ 

### **Answer Section**

- 1. A
- 2. C
- 3. E
- 4. E
- 5. B
- 6. C
- 7. B
- 8. D
- 9. D
- 10. C
- 11. D
- 12. C
- 13. E
- 14. D
- 15. D
- 16. A
- 17. B
- 18. C
- 19. E
- 20. C
- 21. D
- 22. A
- 23. B
- 24. B
- 25. B

### **Multiple Choice/Short Answer**

Identify the choice that best completes the statement or answers the question/Use the space provided to write your answer.

- \_\_\_ 1. Find the complement and supplement of the angle 54°.
  - a. Complement: 36°
     Supplement: 126°
  - b. Complement: 126°
     Supplement: 36°
     c. Complement: 46°

Supplement: 146°

- d. Complement: 144°

   Supplement: 234°

   e. Complement: 126°

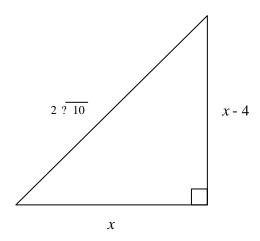
   Supplement: 306°
- 2. Determine two coterminal angles (one positive and one negative) for  $\theta = -457^{\circ}$ .

3. Let triangle ABC be a right triangle with  $C = 90^{\circ}$ . If c = 19 and a = 6, find b.

a. 
$$\sqrt{13}$$

b. 
$$\sqrt{397}$$

- d.  $5\sqrt{13}$
- e. None of the above.
- 4. Solve for *x* in the following right triangle:



- a. 9
- b. (
- c. 5

- d. 8
- e.

5. Find the lengths of the shortest two sides of a  $30^{\circ} - 60^{\circ} - 90^{\circ}$  triangle, if the length of the longest side is 16.

a. 4, 
$$\frac{8}{\sqrt{3}}$$

d. 4, 
$$\frac{4}{\sqrt{3}}$$

b. 
$$4, 4\sqrt{3}$$

d. 
$$4, \frac{4}{\sqrt{3}}$$
 e.  $8, \frac{8}{\sqrt{3}}$ 

c. 
$$8, 8\sqrt{3}$$

6. Find the length of the shorter sides of a  $45^{\circ} - 45^{\circ} - 90^{\circ}$  triangle if the length of the hypotenuse is 21.

a. 
$$\frac{21\sqrt{2}}{2}$$

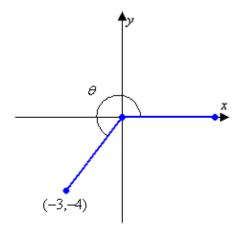
d. 
$$\frac{21\sqrt{3}}{3}$$

b. 
$$\frac{21\sqrt{2}}{4}$$

e. 
$$\frac{21\sqrt{3}}{2}$$

c. 
$$\frac{21}{2}$$

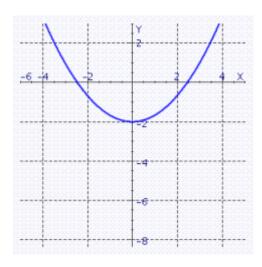
7. Given the figure below, determine the value of  $\sin \theta$ .



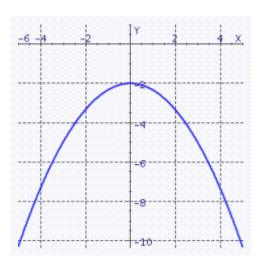
\_\_\_\_\_ 8. Graph the following parabola.

$$f(x) = -\frac{1}{3}x^2 - 2$$

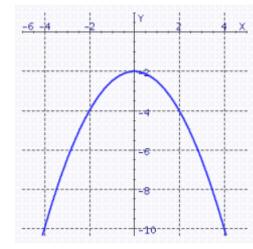
a.



d.

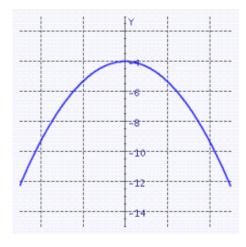


b.



e. None of the above.

c.



- 9. Find the distance between the two points (-5, 8) and (19, 53).

  - b. 51
  - c. 48
  - d. 153
  - e. 99

- 10. Determine which of the following points is located in quadrant 4.

 $\begin{array}{ll} d. & \left(-3, -6\right) \\ e. & \left(6, -3\right) \end{array}$ 

- c. (3, 6)
- 11. Which of the following points lies on the unit circle?

  - e. None of the above.
  - 12. Given  $\sin 30^\circ = \frac{1}{2}$  and  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ , determine the following: sec 30°

 13.	Indicate the two quadrants $\theta$	could terminate in if $\tan \theta = -$	$\frac{17}{25}$
			25

- a. Quadrants III and IV
- b. Quadrants I and III
- c. Quadrants I and IV

- d. Quadrants II and III
- e. Quadrants II and IV

\_\_\_\_ 15. Find 
$$\sin \theta$$
 if  $\csc \theta = \frac{-19}{17}$ .

- c.  $\frac{17}{19}$

- 16. Find  $\tan \theta$  if  $\sec \theta = \frac{\sqrt{290}}{11}$  and  $\csc \theta = \frac{\sqrt{290}}{13}$ .

- 17. Multiply; then use fundamental identities to simplify the expression below and determine which of the following is *not* equivalent.

$$(2-2\cos x)(2+2\cos x)$$

- a.  $4 \cos^2 x$ b.  $4 4\cos^2 x$ c.  $4\sin^2 x$ d.  $\frac{4}{\csc^2 x}$ e.  $\frac{4}{1 + \cot^2 x}$

\_\_\_\_ 18. If 
$$\sin \theta = \frac{-8}{\sqrt{89}}$$
 and  $\theta$  terminates in QIV, find  $\cos \theta$ .

a. 
$$\frac{5}{8}$$

a. 
$$\frac{5}{8}$$
b.  $\frac{-5}{8}$ 

d. 
$$\frac{5}{\sqrt{89}}$$

e. 
$$\frac{\sqrt{89}}{25}$$

19. The point (7,24) is on the terminal side of an angle in standard position. Determine the exact value of  $\sin \theta$ .

\_\_\_\_ 20. Suppose  $\csc \theta = 7$  and  $\theta$  terminates in QII. Find the remaining trigonometric ratios of  $\theta$ .

a. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{4\sqrt{3}}{7}$$

$$\tan \theta = \frac{1}{4\sqrt{3}}$$

$$\sec \theta = \frac{7}{4\sqrt{3}}$$

$$\cot \theta = 4\sqrt{3}$$

b. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{-4\sqrt{3}}{7}$$

$$\tan\theta = \frac{-1}{4\sqrt{3}}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = -4\sqrt{3}$$

c. 
$$\sin \theta = \frac{-4\sqrt{3}}{7}$$

$$\cos \theta = \frac{1}{7}$$

$$\tan \theta = -4\sqrt{3}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = \frac{-1}{4\sqrt{3}}$$

d. 
$$\sin \theta = \frac{-4\sqrt{3}}{7}$$

$$\cos \theta = \frac{1}{7}$$

$$\tan \theta = \frac{-1}{4\sqrt{3}}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = -4\sqrt{3}$$

e. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{-4\sqrt{3}}{7}$$

$$\tan \theta = -4\sqrt{3}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = \frac{-1}{4\sqrt{3}}$$

\_\_\_\_ 21. If  $\csc \theta = -14$ , find  $\csc^3 \theta$ .

- a.  $\frac{-1}{42}$
- b. <u>- 1</u> 2,744
- c. 2,744

- d. -2,744
- e. -42

22. Use fundamental identities to simplify the expression below and then determine which of the following is *not* equivalent.

$$\sec \phi \left( \frac{\sin \phi}{\tan \phi} \right)$$

- a.  $\sec^2 \phi \tan^2 \phi$
- b.  $\sin^2 \phi + \cos^2 \phi$ c.  $\csc^2 \phi \cot^2 \phi$
- d.  $\cos^2 \phi \sin^2 \phi$
- 23. Simplify the expression  $\sqrt{x^2 + 11}$  as much as possible after substituting  $\sqrt{11} \tan \theta$  for x.
  - a.  $\sqrt{11} |\sec \theta|$

d.  $\sqrt{11} |\sin \theta|$ e.  $11 |\csc \theta|$ 

b.  $11|\sec\theta|$ 

- c.  $\sqrt{11} |\csc \theta|$
- 24. Simplify the expression  $\sqrt{30-10x^2}$  as much as possible after substituting  $\sqrt{3} \sin \theta$  for x.
  - a. 30|cos *θ*|

d.  $\sqrt{30} |\tan \theta|$ e.  $30|\csc \theta|$ 

b.  $\sqrt{30} |\cos \theta|$ c.  $\sqrt{30} |\csc \theta|$ 

- 25. Which of the following is equivalent to the given expression?

$$\frac{\cot^2 x}{\csc x + 1}$$

### **Answer Section**

- 1. A
- 2. 263°, 97°
- 3. D
- 4. B
- 5. C
- 6. A
- 7.  $\sin \theta = -\frac{4}{5}$
- 8. D
- 9. B
- 10. E
- 11. D
- 12.  $\sec 30^{\circ} = \frac{2\sqrt{3}}{3}$
- 13. E
- 14. D
- 15. B
- 16. B
- 17. A
- 18. D
- 19.  $\sin \theta = \frac{24}{25}$
- 20. B
- 21. D
- 22. D
- 23. A
- 24. B
- 25.  $\csc x 1$

### **Multiple Choice/Short Answer**

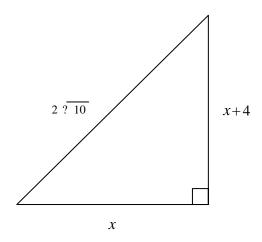
*Identify the choice that best completes the statement or answers the question/Use the space provided to write your answer.* 

1. Determine two coterminal angles (one positive and one negative) for  $\theta = -477^{\circ}$ .

- 2. Find the complement and supplement of the angle 59°.
  - a. Complement: 121° Supplement: 301°
  - b. Complement: 41° Supplement: 141°
  - c. Complement: 149° Supplement: 239°

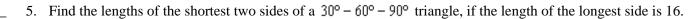
- d. Complement: 121° Supplement: 31°
- e. Complement: 31° Supplement: 121°
- 3. Let triangle ABC be a right triangle with  $C = 90^{\circ}$ . If c = 19 and a = 2, find b.
  - a. 17
  - b.  $\sqrt{365}$
  - c.  $\sqrt{357}$

- d.  $\sqrt{17}$
- e. None of the above.
- \_\_\_ 4. Solve for *x* in the following right triangle:



- a. 1
- b. 5
- c. 4

- d. 3
- e. 2



a. 4, 
$$\frac{4}{\sqrt{3}}$$

d. 
$$4, \frac{8}{\sqrt{3}}$$

b. 
$$4, 4\sqrt{3}$$

d. 4, 
$$\frac{8}{\sqrt{3}}$$
 e. 8,  $\frac{8}{\sqrt{3}}$ 

6. The point (8, 15) is on the terminal side of an angle in standard position. Determine the exact value of  $\cot \theta$ .

7. Find the length of the shorter sides of a  $45^{\circ} - 45^{\circ} - 90^{\circ}$  triangle if the length of the hypotenuse is 17.

a. 
$$\frac{17\sqrt{3}}{3}$$

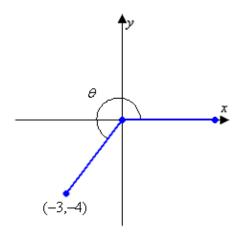
d. 
$$17\sqrt{2}$$

b. 
$$\frac{17\sqrt{3}}{2}$$

e. 
$$\frac{17\sqrt{2}}{2}$$

c. 
$$\frac{17}{2}$$

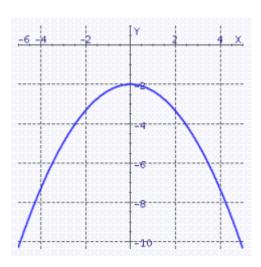
8. Given the figure below, determine the value of  $\sin \theta$ .



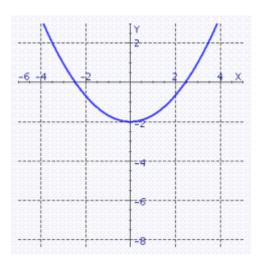
\_\_\_\_ 9. Graph the following parabola.

$$f(x) = -\frac{1}{3}x^2 - 2$$

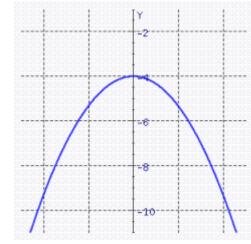
a.



d.

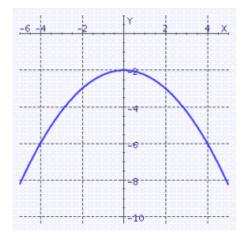


b.



e. None of the above.

c.



10. Determine which of the following points is located in quadrant 4.

a. 
$$(6, 4)$$
  
b.  $(-6, -4)$ 

\_\_\_\_ 11. Find  $\tan \theta$  if  $\sec \theta = \frac{\sqrt{530}}{13}$  and  $\csc \theta = \frac{\sqrt{530}}{19}$ .

d. 
$$-\frac{13}{10}$$

12. Which of the following points lies on the unit circle?

a. 
$$\left(\frac{-7}{11}, \frac{2\sqrt{10}}{11}\right)$$

b. 
$$\left(\frac{7}{15}, \frac{2\sqrt{10}}{15}\right)$$

a. 
$$\left(\frac{-7}{11}, \frac{2\sqrt{10}}{11}\right)$$
  
b.  $\left(\frac{7}{15}, \frac{2\sqrt{10}}{15}\right)$   
c.  $\left(\frac{9}{11}, \frac{2\sqrt{10}}{11}\right)$ 

d. 
$$\left(\frac{9}{13}, \frac{-2\sqrt{10}}{13}\right)$$

e. None of the above.

13. Given  $\sin 30^\circ = \frac{1}{2}$  and  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ , determine the following: csc 30°

14. Which of the following is equivalent to the given expression?

$$\frac{\cos^2 x}{1 + \sin x}$$

- a. tan x + cos x
- b.  $1 \sin x$
- c.  $\csc x + \cot x$
- d.  $tan x \cot x \sin x$
- e.  $\cot x \cos x + \tan x$

15. Evaluate sin 240°.

- 16. Indicate the two quadrants  $\theta$  could terminate in if  $\tan \theta = -\frac{21}{31}$ .
  - a. Quadrants I and III
  - b. Quadrants II and IV
  - c. Quadrants I and IV

- d. Quadrants II and III
- Quadrants III and IV

- \_\_\_\_ 17. Find  $\sin \theta$  if  $\csc \theta = \frac{-17}{13}$ .

- 18. Multiply; then use fundamental identities to simplify the expression below and determine which of the following is *not* equivalent.

$$(\tan x + 1)^2$$

- $\tan^2 x + 1$
- b.  $\sec^2 x + 2\tan x$
- c.  $\frac{1+2\sin x \cos x}{\cos^2 x}$ d.  $\tan^2 x + 2\tan x + 1$

\_\_\_\_ 19. If 
$$\sin \theta = \frac{-6}{\sqrt{85}}$$
 and  $\theta$  terminates in QIV, find  $\cos \theta$ .

a. 
$$\frac{7}{\sqrt{85}}$$

d. 
$$\frac{-7}{\sqrt{85}}$$

c. 
$$\frac{\sqrt{85}}{49}$$

20. Find the distance between the two points (-7, -4) and (41, 16).

- a. 104
- b. 52
- c. 49
- d. 156
- e. 101

21. Suppose  $\csc \theta = 9$  and  $\theta$  terminates in QII. Find the remaining trigonometric ratios of  $\theta$ .

a. 
$$\sin \theta = \frac{1}{9}$$

$$\cos\theta = \frac{4\sqrt{5}}{9}$$

$$\tan \theta = \frac{1}{4\sqrt{5}}$$

$$\sec \theta = \frac{9}{4\sqrt{5}}$$

$$\cot \theta = 4\sqrt{5}$$

b. 
$$\sin \theta = \frac{1}{9}$$

$$\cos\theta = \frac{-4\sqrt{5}}{9}$$

$$\tan\theta = \frac{-1}{4\sqrt{5}}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = -4\sqrt{5}$$

c. 
$$\sin \theta = \frac{-4\sqrt{5}}{9}$$

$$\cos\theta = \frac{1}{9}$$

$$\tan \theta = -4\sqrt{5}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = \frac{-1}{4\sqrt{5}}$$

d. 
$$\sin \theta = \frac{-4\sqrt{5}}{9}$$

$$\cos \theta = \frac{1}{9}$$

$$\tan \theta = \frac{-1}{4\sqrt{5}}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = -4\sqrt{5}$$

e. 
$$\sin \theta = \frac{1}{9}$$

$$\cos\theta = \frac{-4\sqrt{5}}{9}$$

$$\tan\theta = -4\sqrt{5}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = \frac{-1}{4\sqrt{5}}$$

\_\_\_\_ 22. If 
$$\csc \theta = -12$$
, find  $\csc^3 \theta$ .

c. 
$$\frac{-1}{1,728}$$

e. 
$$\frac{-1}{36}$$

23. Use fundamental identities to simplify the expression below and then determine which of the following is *not* equivalent.

$$\sin \alpha (\csc \alpha - \sin \alpha)$$

a. 
$$1 - \sin^2 \alpha$$

b. 
$$\frac{\csc^2 \alpha - 1}{\csc^2 \alpha}$$

csc 
$$\alpha$$

$$\frac{\csc^2 \alpha - \sec^2 \alpha + \tan^2 \alpha}{\csc^2 \alpha}$$
d.  $1 - \cot^2 \alpha$ 

d. 
$$1 - \cot^2 \alpha$$

e. 
$$\cos^2 \alpha$$

24. Simplify the expression  $\sqrt{x^2 + 10}$  as much as possible after substituting  $\sqrt{10} \tan \theta$  for x.

a. 
$$\sqrt{10} \left| \csc \theta \right|$$

b. 
$$\sqrt{10} |\sec \theta|$$

e. 
$$\sqrt{10} |\sin \theta|$$

25. Simplify the expression 
$$\sqrt{66-11x^2}$$
 as much as possible after substituting  $\sqrt{6} \sin \theta$  for x.

c. 
$$\sqrt{66} |\tan \theta|$$

d. 
$$\sqrt{66 \log 6}$$

d. 
$$\sqrt{66} |\csc \theta|$$
  
e.  $\sqrt{66} |\cos \theta|$ 

## **Answer Section**

- 1. 243°, 117°
- 2. E
- 3. C
- 4. E
- 5. C
- 6.  $\cot \theta = \frac{8}{15}$
- 7. E
- 8.  $\sin \theta = -\frac{4}{5}$
- 9. A
- 10. C
- 11. C
- 12. C
- 13.  $csc 30^{\circ} = 2$
- 14. B
- 15. D
- 16. B
- 17. C
- 18. A
- 19. A
- 20. B
- 21. B
- 22. D
- 23. D
- 24. B
- 25. E

#### **Multiple Choice/Short Answer**

*Identify the choice that best completes the statement or answers the question/Use the space provided to write your answer.* 

1. Use fundamental identities to simplify the expression below and then determine which of the following is *not* equivalent.

b. 
$$\frac{\csc\rho\sin\rho + \sec\rho\cos\rho}{\cos\rho}$$

c. 
$$\frac{\tan \rho \cos \rho + \sin \rho}{\sin \rho \cos \rho}$$

2. Find the complement and supplement of the angle 59°.

a. Complement: 121°

Supplement: 31°

b. Complement: 31° Supplement: 121°

c. Complement: 121° Supplement: 301°

d. Complement: 41°

Supplement: 141°

e. Complement: 149° Supplement: 239°

3. Determine which of the following points is located in quadrant 4.

a. 
$$(-3, -6)$$

d. 
$$(-3, 6)$$
  
e.  $(6, -3)$ 

- \_\_\_\_ 4. Wh
- 4. Which of the following points lies on the unit circle?

a. 
$$\left(\frac{-7}{11}, \frac{-4\sqrt{2}}{11}\right)$$

b. 
$$\left(\frac{-7}{9}, \frac{4\sqrt{2}}{9}\right)$$

c. 
$$\left(\frac{5}{9}, \frac{4\sqrt{2}}{9}\right)$$

d. 
$$\left(\frac{-5}{13}, \frac{4\sqrt{2}}{13}\right)$$

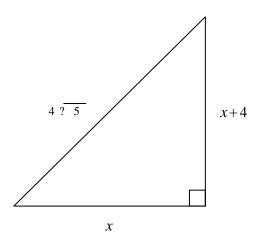
- e. None of the above.
- 5 T -440 1 4
  - 5. Let triangle ABC be a right triangle with  $C = 90^{\circ}$ . If c = 19 and a = 2, find b.

a. 
$$\sqrt{357}$$

b. 
$$\sqrt{365}$$

- c.  $\sqrt{17}$
- 6. Determine two coterminal angles (one positive and one negative) for  $\theta = -453^{\circ}$ .

7. Solve for *x* in the following right triangle:



- 6 a.
- b. 7
- c. 5

- d. 3
- e. 4
- 8. Find the lengths of the shortest two sides of a  $30^{\circ} 60^{\circ} 90^{\circ}$  triangle, if the length of the longest side is 20.
  - a.  $10, 10\sqrt{3}$
  - b.  $10, \frac{10}{\sqrt{3}}$

- d. 5,  $5\sqrt{3}$  e. 5,  $\frac{5}{\sqrt{3}}$
- 9. Given the figure below, determine the value of  $\sin \theta$ .

10. Indicate the two quadrants $\theta$ could terminate in if $\tan \theta = -\frac{1}{2}$	$-\frac{17}{25}$ .
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a. Quadrants III and IV

b. Quadrants II and IV

c. Quadrants I and III

e. Quadrants II and III

a. 
$$\frac{-\sqrt{3}}{2}$$

b.  $\frac{-1}{2}$ 

c.  $\frac{1}{2}$ 

e.  $\frac{-\sqrt{2}}{2}$ 

12. The point (8,15) is on the terminal side of an angle in standard position. Determine the exact value of  $\cot \theta$ .

\_\_\_\_ 13. Find 
$$\sin \theta$$
 if  $\csc \theta = \frac{-37}{31}$ .

a. 
$$\frac{6}{37}$$

b. <u>- 6</u>

c.  $\frac{-31}{37}$ 

e.  $\frac{31}{37}$ 

\_\_\_\_\_ 14. Find 
$$\tan \theta$$
 if  $\sec \theta = \frac{\sqrt{410}}{11}$  and  $\csc \theta = \frac{\sqrt{410}}{17}$ .

a.  $\frac{410}{187}$ 

b. <u>187</u> 410

c.  $-\frac{11}{17}$ 

d. 
$$\frac{17}{11}$$

e. <u>11</u>

15. Multiply; then use fundamental identities to simplify the expression below and determine which of the following is *not* equivalent.

$$(2-2\cos x)(2+2\cos x)$$

a. 
$$4 - \cos^2 x$$

b. 
$$4 - 4\cos^2 x$$
c.  $4\sin^2 x$ 

c. 
$$4\sin^2 x$$

e. 
$$\frac{4}{1 + \cot^2 x}$$

\_\_\_\_ 16. If  $\sin \theta = \frac{-8}{\sqrt{113}}$  and  $\theta$  terminates in QIII, find  $\cos \theta$ .

a. 
$$\frac{-7}{\sqrt{113}}$$

b. 
$$\frac{-7}{8}$$

c. 
$$\frac{7}{8}$$

$$\sqrt{113}$$

d. 
$$\frac{7}{\sqrt{113}}$$
 e.  $\frac{-\sqrt{113}}{49}$ 

\_\_\_\_ 17. Suppose  $\csc \theta = 9$  and  $\theta$  terminates in QII. Find the remaining trigonometric ratios of  $\theta$ .

a. 
$$\sin \theta = \frac{1}{9}$$

$$\cos\theta = \frac{-4\sqrt{5}}{9}$$

$$\tan \theta = -4\sqrt{5}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = \frac{-1}{4\sqrt{5}}$$

b. 
$$\sin \theta = \frac{-4\sqrt{5}}{9}$$

$$\cos \theta = \frac{1}{9}$$

$$\tan\theta = \frac{-1}{4\sqrt{5}}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = -4\sqrt{5}$$

c. 
$$\sin \theta = \frac{-4\sqrt{5}}{9}$$

$$\cos\theta = \frac{1}{9}$$

$$\tan \theta = -4\sqrt{5}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = \frac{-1}{4\sqrt{5}}$$

d. 
$$\sin \theta = \frac{1}{9}$$

$$\cos\theta = \frac{4\sqrt{5}}{9}$$

$$\tan\theta = \frac{1}{4\sqrt{5}}$$

$$\sec \theta = \frac{9}{4\sqrt{5}}$$

$$\cot \theta = 4\sqrt{5}$$

e. 
$$\sin \theta = \frac{1}{9}$$

$$\cos\theta = \frac{-4\sqrt{5}}{9}$$

$$\tan \theta = \frac{-1}{4\sqrt{5}}$$

$$\sec \theta = \frac{-9}{4\sqrt{5}}$$

$$\cot \theta = -4\sqrt{5}$$

\_\_\_\_ 18. If  $\csc \theta = -11$ , find  $\csc^3 \theta$ .

- a. -33 b. <u>-1</u> 33
- c.  $\frac{-1}{1331}$

- d. -1,331
- e. 1,331

- \_\_\_\_ 19. Find the length of the shorter sides of a 45° 45° 90° triangle if the length of the hypotenuse is 19.

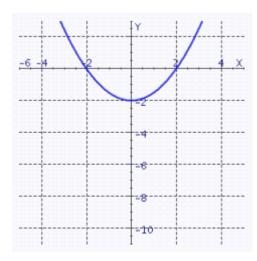
  - a.  $\frac{19\sqrt{3}}{2}$ b.  $\frac{19\sqrt{3}}{3}$ c.  $\frac{19\sqrt{2}}{2}$

- e.  $\frac{19\sqrt{2}}{4}$

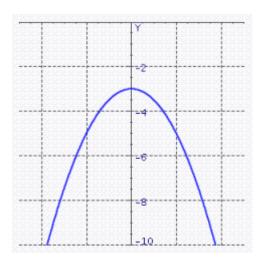
20. Graph the following parabola.

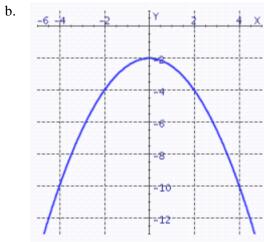
$$f(x) = -\frac{1}{2}x^2 - 2$$

a.

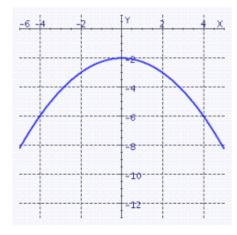


d.





None of the above.



21. Given  $\sin 30^\circ = \frac{1}{2}$  and  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ , determine the following: tan 30°

- 22. Find the distance between the two points (9, 4) and (49, 79).

  - b. 85
  - c. 82
  - d. 255
  - e. 167
- 23. Simplify the expression  $\sqrt{x^2 + 10}$  as much as possible after substituting  $\sqrt{10} \tan \theta$  for x.
  - a.  $\sqrt{10} |\sec \theta|$ b.  $\sqrt{10} |\sin \theta|$

d. 10|csc *θ*|

e. 10|sec *θ*|

- c.  $\sqrt{10} |\cos \theta|$
- 24. Simplify the expression  $\sqrt{30-6x^2}$  as much as possible after substituting  $\sqrt{5} \sin \theta$  for x.
  - a. 30|csc *θ*|

b.  $\sqrt{30} |\csc \theta|$ c.  $\sqrt{30} |\tan \theta|$ 

d.  $30|\cos\theta|$ e.  $\sqrt{30}|\cos\theta|$ 

- 25. Which of the following is equivalent to the given expression?

$$\frac{\sin^2 x}{1 - \cos x}$$

- a. tan x + sin x
- b.  $1 + \cos x$
- c. cscx + cotx
- d. tan x cot x cos x
- e.  $\cot x \sin x + \tan x$

#### **Answer Section**

- 1. D
- 2. B
- 3. E
- 4. B
- 5. A
- 6. 267°, 93°
- 7. E
- 8. A
- 9.  $\sin \theta = -\frac{4}{5}$
- 10. B
- 11. A
- 12.  $\cot \theta = \frac{8}{15}$
- 13. C
- 14. D
- 15. A
- 16. A
- 17. E
- 18. D
- 19. C
- 20. B

21. 
$$\tan 30^\circ = \frac{\sqrt{3}}{3}$$

- 22. B
- 23. A
- 24. E
- 25. B

#### **Multiple Choice**

Identify the choice that best completes the statement or answers the question.

\_\_\_\_ 1. Use fundamental identities to simplify the expression below and then determine which of the following is *not* equivalent.

 $\cot \beta \sec \beta$ 

- a.  $\frac{1}{\sin \beta}$
- b.  $\frac{\sec \beta}{\tan \beta}$
- c.  $\frac{1}{\cos \beta \tan \beta}$
- d.  $\sec \beta$
- e. csc β
- 2. Find the complement and supplement of the angle 55°.
  - a. Complement: 45°
  - Supplement: 145° b. Complement: 125°
  - Supplement: 35°
  - c. Complement: 145° Supplement: 235°

- d. Complement: 35° Supplement: 125°
- e. Complement: 125° Supplement: 305°
- 3. Determine which of the following points is located in quadrant 4.
  - a. (-5, -6)
    - (6-5)
  - c. (5, 6)

- d. (-6, 5)
- e. (-5, 6)
- 4. Which of the following points lies on the unit circle?
  - a.  $\left(\frac{-5}{7}, \frac{2\sqrt{6}}{7}\right)$
  - b.  $\left(\frac{-5}{9}, \frac{-2\sqrt{6}}{9}\right)$
  - c.  $\left(\frac{3}{7}, \frac{2\sqrt{6}}{7}\right)$
  - d.  $\left(\frac{-3}{11}, \frac{2\sqrt{6}}{11}\right)$
  - e. None of the above.

5. Determine two coterminal angles (one positive and one negative) for  $\theta = -526^{\circ}$ .

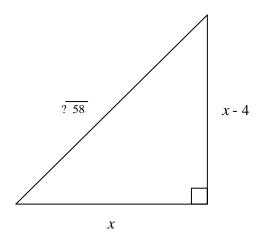
6. Let triangle ABC be a right triangle with  $C = 90^{\circ}$ . If c = 19 and a = 6, find b.

a. 
$$\sqrt{13}$$

d. 
$$5\sqrt{13}$$

d.  $5\sqrt{13}$  e. None of the above.

7. Solve for x in the following right triangle:



b. 9

e. 10

8. Find the lengths of the shortest two sides of a  $30^{\circ} - 60^{\circ} - 90^{\circ}$  triangle, if the length of the longest side is 16.

b. 4,  $4\sqrt{3}$  c. 8,  $\frac{8}{\sqrt{3}}$ 

d.  $4, \frac{4}{\sqrt{3}}$ 

e. 8,  $8\sqrt{3}$ 

 9.	Indicate the two quadrants $\theta$	could terminate in if $\tan \theta = -$	13 23

a. Quadrants I and III

b. Quadrants III and IVc. Quadrants II and III

d. Quadrants I and IV

e. Quadrants II and IV

a. 
$$\frac{-1}{2}$$

b.  $\frac{1}{2}$ 

c.  $\frac{\sqrt{3}}{2}$ 

d. 
$$\frac{-\sqrt{2}}{2}$$

e.  $\frac{-\sqrt{3}}{2}$ 

11. The point (7,24) is on the terminal side of an angle in standard position. Determine the exact value of  $\csc \theta$ .

\_\_\_\_ 12. Find 
$$\sin \theta$$
 if  $\csc \theta = \frac{-17}{13}$ .

a. 
$$\frac{-13}{17}$$

b.  $\frac{4}{13}$ 

c.  $\frac{4}{17}$ 

d. 
$$\frac{13}{15}$$

e.  $\frac{-4}{17}$ 

\_\_\_\_ 13. Find 
$$\tan \theta$$
 if  $\sec \theta = \frac{\sqrt{410}}{11}$  and  $\csc \theta = \frac{\sqrt{410}}{17}$ .

a. 
$$\frac{11}{17}$$

b.  $\frac{17}{11}$ 

c.  $-\frac{11}{17}$ 

e. 410 187

\_\_\_\_ 14. Multiply; then use fundamental identities to simplify the expression below and determine which of the following is *not* equivalent.

$$(\tan x + 1)^2$$

a. 
$$tan^2x + 1$$

b. 
$$\sec^2 x + 2\tan x$$

b. 
$$\sec^2 x + 2\tan x$$
  
c.  $\frac{1 + 2\sin x \cos x}{\cos^2 x}$   
d.  $\tan^2 x + 2\tan x + 1$   
e.  $\sec^2 x(1 + 2\sin x \cos x)$ 

d. 
$$tan^2x + 2tanx + 1$$

e. 
$$\sec^2 x (1 + 2\sin x \cos x)$$

\_\_\_\_ 15. If  $\sin \theta = \frac{-6}{\sqrt{157}}$  and  $\theta$  terminates in QIII, find  $\cos \theta$ .

a. 
$$\frac{11}{\sqrt{157}}$$

d. 
$$\frac{-6}{11}$$

b. 
$$\frac{-\sqrt{157}}{121}$$

c. 
$$\frac{-11}{\sqrt{157}}$$

16. Suppose  $\csc \theta = 7$  and  $\theta$  terminates in QII. Find the remaining trigonometric ratios of  $\theta$ .

a. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{-4\sqrt{3}}{7}$$

$$\tan \theta = -4\sqrt{3}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = \frac{-1}{4\sqrt{3}}$$

b. 
$$\sin \theta = \frac{-4\sqrt{3}}{7}$$

$$\cos \theta = \frac{1}{7}$$

$$\tan\theta = -4\sqrt{3}$$

$$\sec\theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = \frac{-1}{4\sqrt{3}}$$

c. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{4\sqrt{3}}{7}$$

$$\tan\theta = \frac{1}{4\sqrt{3}}$$

$$\sec \theta = \frac{7}{4\sqrt{3}}$$

$$\cot \theta = 4\sqrt{3}$$

d. 
$$\sin \theta = \frac{1}{7}$$

$$\cos\theta = \frac{-4\sqrt{3}}{7}$$

$$\tan\theta = \frac{-1}{4\sqrt{3}}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = -4\sqrt{3}$$

e. 
$$\sin \theta = \frac{-4\sqrt{3}}{7}$$

$$\cos \theta = \frac{1}{7}$$

$$\tan \theta = \frac{-1}{4\sqrt{3}}$$

$$\sec \theta = \frac{-7}{4\sqrt{3}}$$

$$\cot \theta = -4\sqrt{3}$$

17. Given  $\sin 30^\circ = \frac{1}{2}$  and  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ , determine the following:  $\sec 30^\circ$ 

\_\_\_\_ 18. If 
$$\csc \theta = -11$$
, find  $\csc^3 \theta$ .

d. 
$$\frac{-1}{33}$$

b. 
$$\frac{-1}{1,331}$$

c. 
$$-1,331$$

 $\perp$  19. Find the length of the shorter sides of a  $45^{\circ} - 45^{\circ} - 90^{\circ}$  triangle if the length of the hypotenuse is 17.

a. 
$$\frac{17}{2}$$

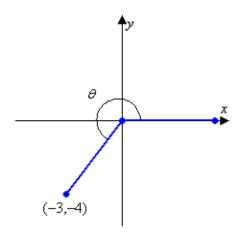
d. 
$$17\sqrt{3}$$

b. 
$$\frac{17\sqrt{3}}{3}$$

e. 
$$\frac{17\sqrt{2}}{2}$$

c. 
$$\frac{17\sqrt{2}}{4}$$

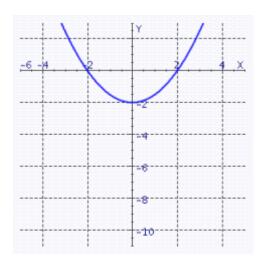
20. Given the figure below, determine the value of  $\sin \theta$ .



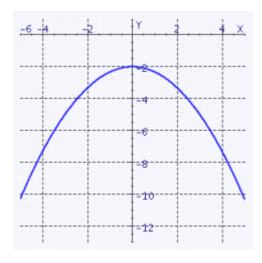
\_\_\_\_ 21. Graph the following parabola.

$$f(x) = -\frac{1}{2}x^2 - 2$$

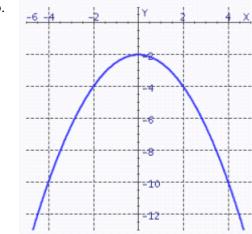
a.



d.

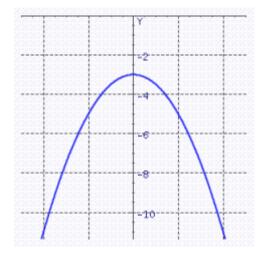


b.



e. None of the above.

c.



22. Find the distance between the two points (4, 2) and (10, 10).

- b. 10
- c. 7
- d. 30
- e. 17

23. Which of the following is equivalent to the given expression?

$$\frac{\cos^2 x}{1+\sin x}$$

- a. tan x + cos x
- b.  $1 \sin x$
- c.  $\csc x + \cot x$
- d.  $tan x \cot x \sin x$
- e.  $\cot x \cos x + \tan x$

24. Simplify the expression  $\sqrt{x^2 + 13}$  as much as possible after substituting  $\sqrt{13} \tan \theta$  for x.

a.  $\sqrt{13} \left| \csc \theta \right|$ 

d. 13|csc *θ*|

b.  $\sqrt{13} |\sin \theta|$ 

e. 13|sec *θ*|

c.  $\sqrt{13} |\sec \theta|$ 

25. Simplify the expression  $\sqrt{30-6x^2}$  as much as possible after substituting  $\sqrt{5} \sin \theta$  for x.

a.  $\sqrt{30} |\tan \theta|$ b.  $30|\csc \theta|$ c.  $\sqrt{30} |\cos \theta|$ 

d.  $\sqrt{30} |\csc \theta|$ e.  $30|\cos \theta|$ 

#### McKeague/Turner Trigonometry Chapter 2 Form F Answer Section

- 1. D
- 2. D
- 3. B
- 4. A
- 5. 194°, 166°
- 6. D
- 7. D
- 8. E
- 9. E
- 10. E
- 11.  $\csc \theta = \frac{25}{24}$
- 12. A
- 13. B
- 14. A
- 15. C
- 16. D

17. 
$$\sec 30^\circ = \frac{2\sqrt{3}}{3}$$

- 18. C
- 19. E

$$20. \sin \theta = -\frac{4}{5}$$

- 21. B
- 22. B
- 23. B
- 24. C
- 25. C